
Relational String Verification Using Multi-track Automata

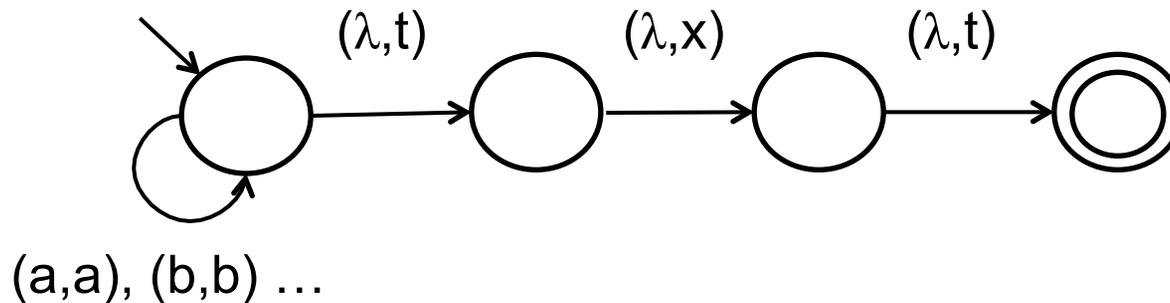
Relational String Analysis

- Earlier work on string analysis use multiple single-track DFAs during symbolic reachability analysis
 - One DFA per variable per program location
- Alternative approach: Use one multi-track DFA per program location
 - Each track represents the values of one string variable
- Using multi-track DFAs:
 - Identifies the relations among string variables
 - Improves the precision of the path-sensitive analysis
 - Can be used to prove properties that depend on relations among string variables, e.g., `$file = $usr.txt`

Multi-track Automata

- Let X (the first track), Y (the second track), be two string variables
- λ is the padding symbol
- A multi-track automaton that encodes the word equation:

$$Y = X.txt$$



Alignment

- To conduct relational string analysis, we need to compute union or intersection of multi-track automata
 - Intersection is closed under aligned multi-track automata
 - In an aligned multi-track automaton λ s are right justified in all tracks, e.g., $ab\lambda\lambda$ instead of $a\lambda b\lambda$
- However, there exist unaligned multi-track automata that are not equivalent to any aligned multi-track automata
 - Use an alignment algorithm that constructs aligned automata which over or under approximates unaligned ones
 - Over approximation: Generates an aligned multi-track automaton that accepts a super set of the language recognized by the unaligned multi-track automaton
 - Under approximation: Generates an aligned multi-track automaton that accepts a subset of the language recognized by the unaligned multi-track automaton

Symbolic Reachability Analysis

- Transitions and configurations of a string system can be represented using word equations
- Word equations can be represented/approximated using aligned multi-track automata which are closed under intersection, union, complement and projection
- Operations required for reachability analysis (such as equivalence checking) can be computed on DFAs

Word Equations

- Word equations: Equality of two expressions that consist of concatenation of a set of variables and constants
 - Example: $X = Y . \text{txt}$
- Word equations and their combinations (using Boolean connectives) can be expressed using only equations of the form $X = Y . c$, $X = c . Y$, $c = X . Y$, $X = Y . Z$, Boolean connectives and existential quantification
- Our goal:
 - Construct multi-track automata from basic word equations
 - The automata should accept tuples of strings that satisfy the equation
 - Boolean connectives can be handled using intersection, union and complement
 - Existential quantification can be handled using projection

Word Equations to Automata

- Basic equations $X = Y \cdot c$, $X = c \cdot Y$, $c = X \cdot Y$ and their Boolean combinations can be represented precisely using multi-track automata
- The size of the aligned multi-track automaton for $X = c \cdot Y$ is exponential in the length of c
- The nonlinear equation $X = Y \cdot Z$ cannot be represented precisely using an aligned multi-track automaton

Word Equations to Automata

- When we cannot represent an equation precisely, we can generate an over or under-approximation of it
 - Over-approximation: The automaton accepts all string tuples that satisfy the equation and possibly more
 - Under-approximation: The automaton accepts only the string tuples that satisfy the equation but possibly not all of them
- We can implement a function `CONSTRUCT(equation, sign)`
 - Which takes a word equation and a sign and creates a multi-track automata that over or under-approximation of the equation based on the input sign

Post condition computation

- During symbolic reachability analysis we compute the post-conditions of statements using the function CONSTRUCT

Given a multi-track automata M and
an assignment statement: $X := \text{sexp}$

$\text{Post}(M, X := \text{sexp})$ denotes the post-condition of $X := \text{sexp}$ with
respect to M

$$\begin{aligned} & \text{Post}(M, X := \text{sexp}) \\ &= (\exists X', M \cap \text{CONSTRUCT}(X' = \text{sexp}, +))[X/X'] \end{aligned}$$