Parallel Modeling of Fish Interaction

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Abstract

This paper summarizes our work on a parallel algorithm for an interacting particle model, derived from the model by Czirok, Vicsek, et. al. [14, 5, 6, 15, 16]. Our model is particularly geared toward simulating the behavior of fish in large shoals. In this paper, the background and motivation for the problem are given, as well as an introduction to the mathematical model. A discussion of implementing this model in MATLAB and C++ follows. The parallel implementation is discussed with challenges particular to this mathematical model and how the authors addressed these challenges. Load balancing was performed and is discussed. Finally, a performance analysis follows, using a performance metric to compare the MATLAB, C++, and parallelized code.

1. Introduction

The capelin is a species of pelagic fish that lives in the northern oceans. There are several stocks in the North Atlantic ocean; we are particularly interested in the stock that migrates in the seas around and north of Iceland. These fish form large shoals off the northern coast of Iceland generally made up of billions of individuals. Each year, the mature portion of this stock undertakes an extensive migration to feed on zooplankton whose population swells during the vernal phytoplankton bloom to the northeast of Jan Mayen [17, 18]. In the fall, the fish return to the northern coast of Iceland and the portion of the stock which undertook the feeding migration swims around Iceland to the southern coast. The fish then spawn and the adults die. The young drift with the tidal current to mature off the northern coast.

The goal of our work is to model the life cycle and migration route of this particular stock of capelin with schools of up to a million individuals. The Icelandic fishing industry needs an accurate model of the migration of this stock because the capelin are important both economically and ecologically. The fishing industry fishes the stock for export, but this stock is also one of the main food sources for many of the larger, more economically valuable fish in the vicinity. Hence, it is important that the stock not be overfished. Because the migration route of the capelin seems to be highly dependent on ocean temperature and currents, it is difficult to find the stock at a given time and therefore difficult to gauge the number of capelin during a given year [2]. Stocks of fish in other oceans have been catastrophically depleted due to overestimation of the population. It is therefore extremely important to keep careful track of the location of the various parts of the stock of the capelin to avoid similar catastrophes in this region.

Other groups have also worked on numerical simulations to reproduce this migration, see [10, 11, 12]. These groups have obtained reasonable spawning migrations using a comparatively small number of interacting particles representing super-individuals. Their models include currents, temperature gradients, and a forcing term that simulates a homing instinct to draw the fish to the feeding and spawning grounds at the correct times. We are interested in simulating the migration with a quantitatively accurate number of fish and without these forcing terms. This paper addresses necessary architecture for such a simulation.

One obstacle common to particle systems is the computational expense of simulating a suitably large number of particles. Simulating many particles is important, however, because local information can become global information via local interaction if there are sufficiently many particles. In this paper, we address one possible solution to this problem. Our model is based on the model de-
scribed in [1], which in turn is derived from the model in [10]. In this paper, we discuss transitioning the code from the MATLAB implementation discussed in [1] to C++ using MPI for parallel processing. We discuss the various challenges in parallelizing the code and the strategies we used to address these challenges, including geographic division of our space, ghost fish, shadow oceans, and load balancing.

This paper is organized as follows. In Section 2, we present the necessary background on the fish interaction schemes and describe the mathematical model for the problem. In Section 3, we describe our implementation of the mathematical model, including the serial code in MATLAB and C++, as well as the parallel code in MPI. Section 4 describes our approach to the load balancing problem. We quantify the performance of our model in Section 5 and conclude the paper in the following section.

2. Background

2.1. Fish Interaction

In our model, fish interact with each other locally. All fish are identical, and no fish are designated as “leaders,” i.e., having more information or behaving differently from the other fish. Each fish interacts only with fish within a certain finite region and ignores information from all other fish. In general, each fish heads away from fish that are too close, aligns with fish that are reasonably close, and head toward fish that are too far away. Avoiding fish which are too close averts collisions, aligning with neighbors allows the fish to form cohesive schools to help avoid predation and offer hydrodynamic advantages, and getting closer to fish which are far away helps fish avoid being alone and encourages the formation of schools [13]. This type of behavior was observed in schooling fish by biologists and has been shown to be motivated by vision and the lateral line, a sense organ which detects pressure changes and runs down the side of many fish species including the capelin [14].

2.2. Zones of Interaction

We simulate these effects using the zones of interaction shown in Figure 1. Three zones are defined by three concentric circles around every fish: the zone of repulsion, the zone of orientation, and the zone of attraction. The smallest circle is the zone of repulsion of the fish, at the center of the diagram. The annulus between the zone of repulsion and the larger circle is the zone of orientation, and the annulus outside the zone of repulsion and inside the largest circle is the zone of attraction. Fish try to head toward fish in their zone of attraction, try to align in speed and direction with fish in their zone of orientation, and try to head away from fish in their zone of repulsion. They do this by taking an average of all these (often conflicting) desires; for details, see Section 2.3. Many interacting particle models employ similar zones of interaction, see for example [3, 7]. In our implementation, each zone is given equal weighting and the radii of the different zones are parameters which can be adjusted to create individual variation among the fish.

2.3. Mathematical Model

Our model is derived from the interacting particle model first presented by Czirók, Vicsek, et al., see [4, 5, 6, 15, 16], and later adapted by [10] and then [1]. Fish change their directional heading and speed at each time step by reacting to nearby fish through the zones of interaction described in Section 2.2. The algorithm for updating the $k$th fish’s speed is

$$v_k(t + \Delta t) = \frac{1}{N} \sum_{i=1}^{N} v_i(t)$$

(1)

where there are $N$ fish inside the zone of orientation of fish $k$. Letting $\phi_k$ be the directional heading of the $k$th fish, we update its directional heading at each time step according to the rules specified by equations (2) and (3).

Here, $R$, $N$, and $A$ are the number of fish in the $k$th fish’s zone of repulsion, orientation, and attraction, respectively. The indices $r$, $n$, and $a$ run through all the fish in each respective zone. The algorithm uses the speed and directional heading from these calculations to move each fish according to its velocity as follows:

$$\begin{bmatrix} x_k(t) \\ y_k(t) \end{bmatrix} = \begin{bmatrix} x_k(t - \Delta t) \\ y_k(t - \Delta t) \end{bmatrix} + v_k(t) \begin{bmatrix} \cos(\phi_k(t)) \\ \sin(\phi_k(t)) \end{bmatrix} \Delta t.$$
\[
\cos(\phi_k(t + \Delta t)) = \frac{1}{R + N + A} \left( \sum_{r=1}^{R} \frac{x_k(t) - x_r(t)}{(x_k(t) - x_r(t))^2 + (y_k(t) - y_r(t))^2} + \sum_{n=1}^{N} \cos(\phi_n(t)) \right) \\
+ \sum_{a=1}^{A} \frac{x_a(t) - x_k(t)}{(x_a(t) - x_k(t))^2 + (y_a(t) - y_k(t))^2} \\
\sin(\phi_k(t + \Delta t)) = \frac{1}{R + N + A} \left( \sum_{r=1}^{R} \frac{y_k(t) - y_r(t)}{(x_k(t) - x_r(t))^2 + (y_k(t) - y_r(t))^2} + \sum_{n=1}^{N} \sin(\phi_n(t)) \right) \\
+ \sum_{a=1}^{A} \frac{y_a(t) - y_k(t)}{(x_a(t) - x_k(t))^2 + (y_a(t) - y_k(t))^2}
\]

3. Interaction Simulation Model

3.1. MATLAB and C++ Models

In [1], the authors implement the model described in Section 2.3 in MATLAB. For completeness, we began our analysis with this implementation. In this code, there is no sorting of the fish, and every fish computes its distance to every other fish at every time step to see if it needs to react to the other fish. This slows the code significantly as the number of fish increases, making it prohibitively expensive to model the number of individuals necessary for realistic simulations of shoals of the capelin. It is therefore necessary to move the code to another platform such as C++ and to improve the algorithm itself.

3.1.1. Class Architecture

Our model consists of three main classes: Fish, Ocean and World. The Fish class stores coordinate and velocity data for a fish, the Ocean class is meant to represent a single body of water, whereas a World class is a bigger body of water composed of several connected oceans. Each fish stores an x and y coordinate for its location in the world. A fish stores its velocity as the cosine and sine of its direction angle together with a non-negative speed. The Ocean class has a member variable “fish” which is an array of Fish living in that ocean. For a performance improvement, we sort the list of fish in an ocean by x coordinate, and when fish in an ocean interact, they need only compare their positions with fish nearby in the sorted list. This saves us from an “all-to-all” comparison for proximity detection. The Ocean class has member functions which iterate through the fish, updates their velocities and moves them. The Ocean class does not handle any MPI communication. The World class contains a 2-dimensional array of oceans. Member functions of the World class iterate through the oceans and instruct each ocean to interact or move its fish. The World class handles communication of the fish between oceans both locally and over a network with MPI. In our implementation a flag in the World class determines whether the oceans in a world are either connected in a torus or not. If the torus flag is set to false, fish which traverse the boundary of the world disappear from the simulation. When the torus flag is set to true, the top edge of the world is identified with the bottom edge of the world and likewise left and right, so fish which traverse a boundary of the world teleport to its other side.

3.1.2. Local Communication

Even if a world is instantiated on a sequential machine, the oceans in that world do a network-style communication of fish. The motion and interaction of fish in a time step are computed one ocean at a time. Between time steps, the oceans inform each other of pertinent fish.

There are two phases of communication per time step:

1. Before the fish can interact, each ocean needs to be informed of sufficiently nearby fish in neighboring oceans. We do this by adding a copy of each fish in the neighboring ocean (provided it is within the largest radius of attraction of the boundary) with a flag set to indicate that the fish is a “ghost”. These fish need to be present to affect other fish, but in the interaction phase of computation, ghost fish need not have their velocities updated.

2. When fish migrate to an ocean from a neighboring ocean, they need to be removed from the source ocean’s list and added to the receiving ocean’s list.

In communication phase (1) where ghost fish are sent from ocean to ocean, we employ a trick that uses sorting to save computational effort. Each ocean needs to communicate ghost fish to its eight neighboring oceans in the 2-dimensional model, as shown in Figure 2. Due to the geometry, the sets of ghost fish destined for the various neighbors tend to intersect non-trivially. For instance, the ghost fish which need to be sent to the neighbor in the upper-right corner of an ocean also need to be sent to the ocean directly to the right. To avoid redundant computation, we first divide the ocean up into regions. We assign to each fish the
number of the region in which that fish is currently located. We then sort the entire array of fish by region number. Because of the ordering of the region numbers, the fish that must be sent to any neighboring ocean will be contiguous in the sorted list. In communication phase (2) when migrating fish are transported to their target oceans, we use a similar scheme by assigning a number to the fish according to its destination ocean.

3.2. Parallelization

When running in parallel each MPI-process instantiates one world the structure of which mimics the worlds on all other MPI-processes. To divide the work among MPI-processes, each MPI-process is assigned a connected set of oceans in this world to compute. On each process, the oceans in the world which are not assigned to that MPI-process still exist, but they begin each time step empty of fish. We call such an ocean a shadow ocean. Before the fish interact with each other to update their velocities, the oceans need to be informed of ghost fish. So, on each MPI-process, the world iterates through all oceans, and performs a local communication of ghost fish amongst oceans in its local world. Ghost fish spill into shadow oceans, so a network communication pass follows which sends the ghost fish in each shadow ocean into the identical ocean on the proper MPI-process.

Once all ghost fish are in place, the real fish can update their velocities. So at this point, we allow the fish in the world to interact, and then we move the fish according to the rules described in Section 2.3. Ghost fish are removed once the velocities have been updated. When moving fish, the process simply iterates through all its assigned oceans, and for each ocean advances every fish in that ocean by its velocity. This might move fish into the processor’s shadow oceans, so a second network communication pass follows which moves the fish in each of a processor’s shadow oceans into the identical ocean on the proper MPI-process.

By organizing the procedure in this way, we made a healthy barrier between the computation of fish motion and the MPI inter-process communication of fish. The movement and interaction code can run blind to the fact that network communication need be performed, and shadow oceans automatically do the job of accumulating ghost fish or migrant fish (depending on the phase of computation) into a list. All the communication code does is transmit the entire contents of each shadow ocean to the MPI-process to which that ocean belongs. In fact, transmission of the entire contents of an ocean from one MPI-process to another is exactly what our dynamic load balancing scheme requires, so the same code can be used for that as well, see Section 4.

4. Load Balancing

Distributing work among MPI-processes is a challenge in any parallel interacting particle simulation. Fish are attracted to each other and therefore distribute unevenly. To contend with this, we adopt a dynamic load balancing scheme. In some particle systems, it might be necessary to use a dynamic space partitioning data structure, like a BSP-tree. Our scheme does not use such a structure, making it simpler and easier to implement, yet it still yields a significant performance benefit.

Each MPI-process owns a number of oceans, and its workload is determined by the number of fish interacting inside those oceans and their total communication characteristics. For our initial configuration, we distribute the workload among MPI-processes by distributing the oceans between them equally. Oceans are distributed in groups to the processors in a snake-like pattern. This way each group of oceans is connected, and because fish are initially placed randomly, all MPI-processes have comparable portions of the total workload. In general, choosing an initial distribution reduces to a graph partitioning problem. The interested reader is directed to [8, 9].

Because of the interactions between the fish described in Section 2.2, the fish often gather into schools and then move through the world as schools. This means that in order to avoid overloading some processors while other processors remain idle, it is necessary to employ dynamic load balancing. Our goal for dynamic load balancing is for each processor to do a comparable amount of work during each iteration.

Our method for estimating the computational load of a process is based on the assumption that performance is
5. Performance Analysis

Real shoals contain billions of fish. The more fish we can simulate and the more iterations we can run, the more realistic and useful our model will be. Therefore, we measure total execution time of the simulation as a function of the total number of fish in the world and the number of iterations. Hence, we define a performance metric to reflect the time needed in seconds to simulate one fish per iteration. In this section, we show the impact of porting our implementation on execution time per fish per iteration between the MATLAB code, the C++ code and the MPI code with load balancing. Our sequential C++ code outperforms our sequential MATLAB code not only in raw running time, but also in observed asymptotic running time. The MPI code outperforms the sequential C++ code for a large enough number of fish whose interaction cost dominates communication cost. Our parallelization scheme is most effective when oceans sufficiently outnumber processors.

Sequential performance experiments were run on a dual-core Intel Pentium 4 (2.60 GHz per core, 512KB L2 cache, 1GB main memory). We also ran our C++ sequential code on DataStar, an IBM terascale machine at San Diego Supercomputing Center (SDSC). The machine has Power4 processors with pipelined 64-bit RISC chips with two floating-point units. Each Power4 runs at 1.5 GHz, has 16 GB of main memory, and a two-way L1 (32 KB) cache, and a four-way set associative L2 (0.75 MB). There is also an 8-way L3 cache on each node (16 MB per processor). Note that DataStar has a very different memory hierarchy from the Pentium 4 machine.

Our C++ code consistently outperforms our MATLAB code despite the compact size of the MATLAB code. Table 1 show the performance distinction. The figure consists of six sub-figures, each depicts time in seconds (on y-axis) as a function of the total number of fish (on x-axis). The three sub-figures in the top row show total execution time where as the three sub-figures in the bottom row show the execution time per fish per iteration. Furthermore, the three settings of our experiments were (a) MATLAB performance on Pentium 4 machine, (b) C++ sequential code on Pentium 4 machine, and (c) the C++ sequential code on the SDSC Datastar machine, and they are shown as the three different columns of the table. In addition, the red, blue and green curves in each sub-figure are for 10, 100 and 1000 iterations, as each sub-figure's legend reflects.

From Table 1, we observe that the MATLAB code ran about ten times slower than C++ code performance on both Pentium and DataStar machines. The eventual slopes of the curves suggest that the running time of our C++ code is \( O(n^{1.2}) \) while that of the MATLAB code is \( O(n^2) \). We further observe that the performance difference is consistent among different curves of iterations and number of fish. This reflects the fact that for this specific problem instance,
Table 1. The performance comparison between MATLAB and C++ implementation. The first column shows MATLAB performance on P4 machine, while the second and third columns show the C++ performance. The upper row shows the total time of execution of the codes as a function of number of fish in the world. The lower row illustrates the time in seconds per fish per iteration needed by different codes, as a function of the number of fish in the world.

Fish do not clump together, which in turn keeps the number of interaction between the fish constant even upon increase in the total number of iterations. Analysis of our C++ code using a profiler revealed that more than 80% of execution time is spent updating fish’s velocities. This happens because in order to update a fish’s velocity, it has to compare to all its neighbors.

Table 2 shows the performance of the MPI code with different number of MPI-processes and iterations. The subfigures in the first row show the total execution time of the simulation (on the y-axis) as a function of the total number of fish in the world, while the second row shows the time per fish per iteration as a function of the total number of fish in the world. The first, second and third columns of subfigures are the performance characteristics for 10, 100 and 1000 iterations respectively. For each of the subfigures, we show the performance using a different number of MPI-processes. In addition, the red, blue, green and purple curves demonstrate the performance of 2, 4, 8 and 16 MPI-processes. All parallel performance measurements were executed and collected on DataStar.

From Figure 2, we notice that the 16-processes performance lags behind the other curves, especially that the problem instance has 16 oceans (i.e., every MPI-process is executing one ocean). As the small number of fish and small number of oceans in the world are divided among the 16-processors, the computation time is very short relative to the time taken to communicate between the oceans. This imbalance results in the performance retardation, which is seen in the purple curve of the 16 processes. However, as the number of fish in the world increases, the computational load of every ocean on each processor increases, and slowly attains the balance between the communications and computational loads.

We also observe that the performance of the 2, 4 and 8 MPI-processes are similar, while performance for 16 MPI-processes has a longer execution time. This is explained by the architecture of DataStar, whose nodes have 8-cores each. To minimize the network traffic, DataStar middleware assigns up to 8 MPI-processes to the same physical node. In the case of 2, 4 and 8 MPI-processes simulation of our results, the code uses only one physical node and hence
Table 2. MPI performance curves using 2, 4, 8, and 16 MPI-processes for parallel simulation of the fish interaction. The sub-figures in the first column are the performance characteristics for 10 iterations of the simulation, while sub-figures in second and third columns show the performance for 100 and 1000 iterations respectively.

does not encounter much communication overhead. With 16 MPI-processes, however, communication costs more. As the number of fish and interactions increases, the communication overhead for the 16 MPI-processes simulations becomes dominated by the computational load of the processes. This also explains the brief decrease for very small numbers of fish. In addition, we have extended the total number of fish in simulation in the first column to see where the 16 MPI-processes simulation curve meet the other three curves. Although it is not apparent from the figure because of its log scale, the 16 MPI-processes simulation is faster than the other simulations for larger numbers of fish. For example, to simulate half a million fish for 10 iterations, the 16 MPI-processes simulations took 25 minutes while the 2 MPI-processes took 64 minutes. As the number of fish increase, the 16 MPI-processes becomes more efficient, and less impacted by the network overhead.

The lower row of sub-figures in Table 2 shows the time of execution per fish per iteration as a function of the total number of fish in the world. These curves show that the MPI code has a better scalability than the MATLAB and C++ codes. In addition, the curves have a “knee” before and after which the time of simulation per fish per iteration is higher. This happens for 2048, 1024 and 512 fish at 10, 100 and 100 iterations respectively. At these points, the simulation achieves the most balanced state between the computational load and communication load for this number of iterations. In addition, as the number of iterations increase, the balance point is achieved at a lower number of fish. This is also explained by the fact that the communication overhead increases as the number of iterations increases, and not at the same rate as the increase of the computational load. These characteristics are, however, architecture-specific as they depend on the latency of the network infrastructure of the machine.

6. Conclusions

We have implemented a parallel version of the model of fish schooling described in [1]. Some of the challenges addressed in this implementation were ways to divide the problem domain among processors for parallelization, how to communicate between processors effectively and at minimal cost, and how to distribute work dynamically without excessive communication overhead. Our load balan-
ing scheme is an compromise between fixed spatial allocation and completely variable-sized spatial allocation. Load balancing in the way described in Section 4 allows us to keep messages between processors simple, but also moves toward equalizing the work done by the processors. A series of tests gave us empirical results indicating that is our C++ implementation a pleasing improvement over the previous MATLAB implementation.

Our method has potential for further optimization. Different proportions of oceans, processors and fish could be exploited for an optimum. A space searching algorithm could be used within an ocean to avoid unnecessary comparisons between distant fish and might improve performance. Although our tests suggest our method is scalable, we have yet to test on fish populations of size comparable to the real capelin population. We are currently working on applying our scheme in a more detailed and realistic setting taking into account environmental variables such as temperature, currents and land masses.

References