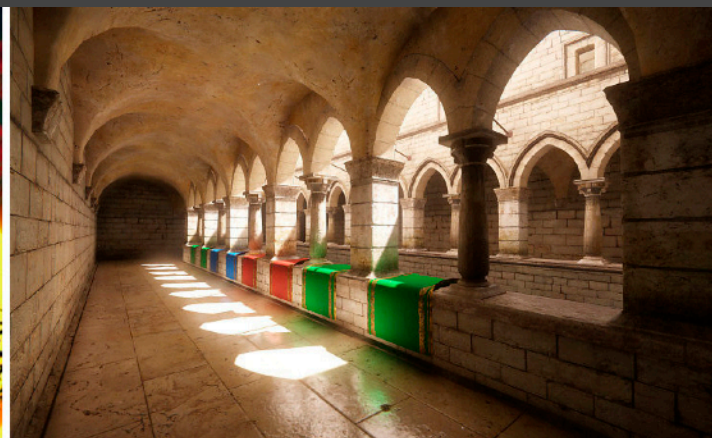


Real-Time High Quality Rendering

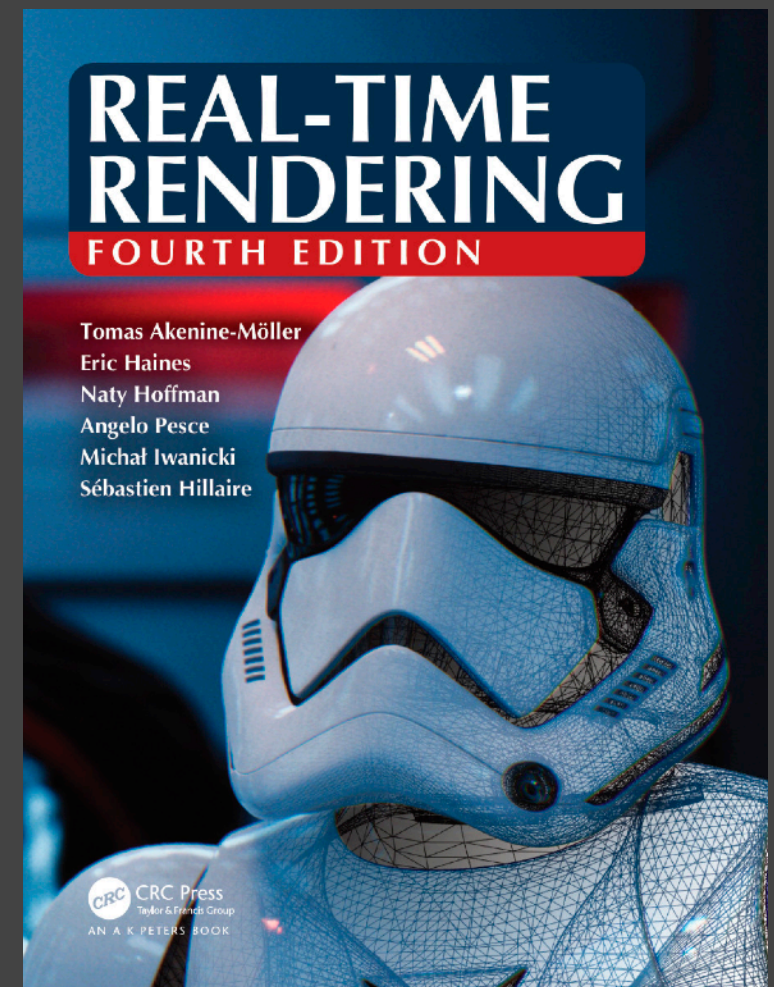
GAMES202, Lingqi Yan, UC Santa Barbara

Lecture 3: Real-Time Shadows 1



Announcement

- Enjoying assignment 0?
- Assignment 1 will be released this week
 - Ideally together with Lecture 4
- Adjusted orders of some contents
- The RTR book



Last Lecture

- Recap of CG Basics
 - Basic GPU hardware pipeline
 - OpenGL
 - OpenGL Shading Language (GLSL)
 - The Rendering Equation
 - Calculus

Today

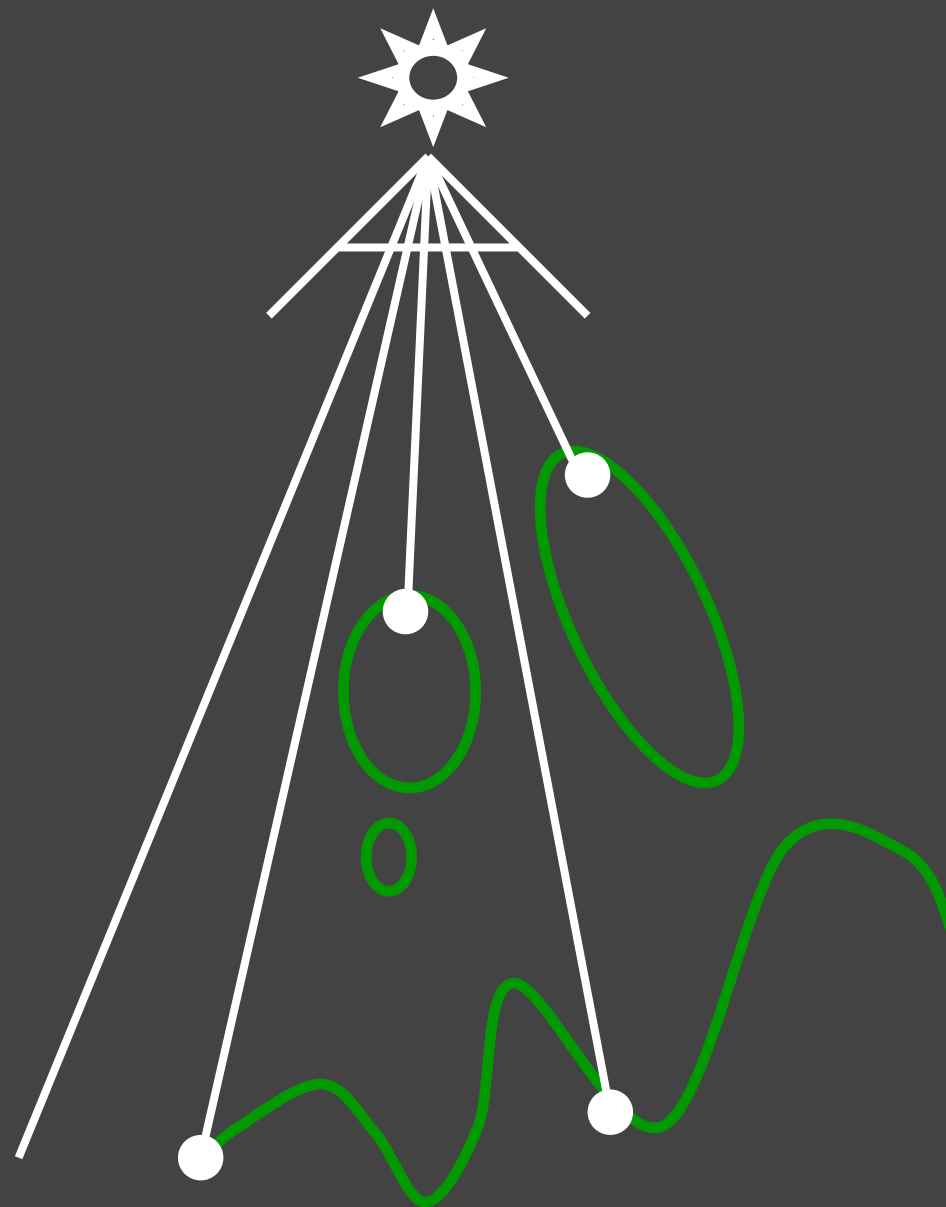
- **Recap: shadow mapping**
[slides courtesy of Prof. Ravi Ramamoorthi]
 - Issues from shadow mapping and solutions
- The math behind shadow mapping
- Percentage closer soft shadows
- Basic filtering techniques

Shadow Mapping

- A 2-Pass Algorithm
 - The light pass generates the SM
 - The camera pass uses the SM (recall last lecture)
- An image-space algorithm
 - Pro: no knowledge of scene's geometry is required
 - Con: causing self occlusion and aliasing issues
- Well known shadow rendering technique
 - Basic shadowing technique even for early offline renderings, e.g., Toy Story

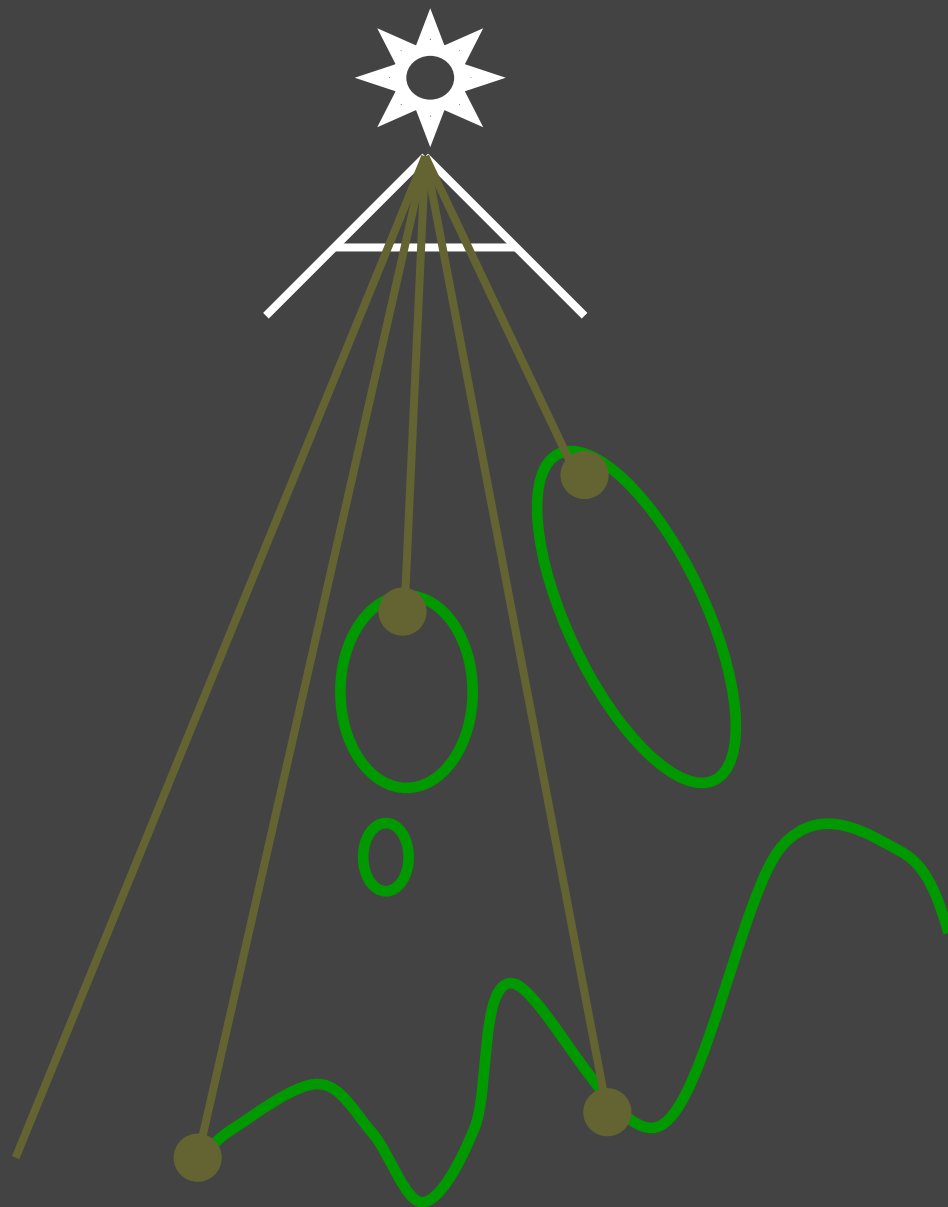
Pass 1: Render from Light

- Output a “depth texture” from the light source



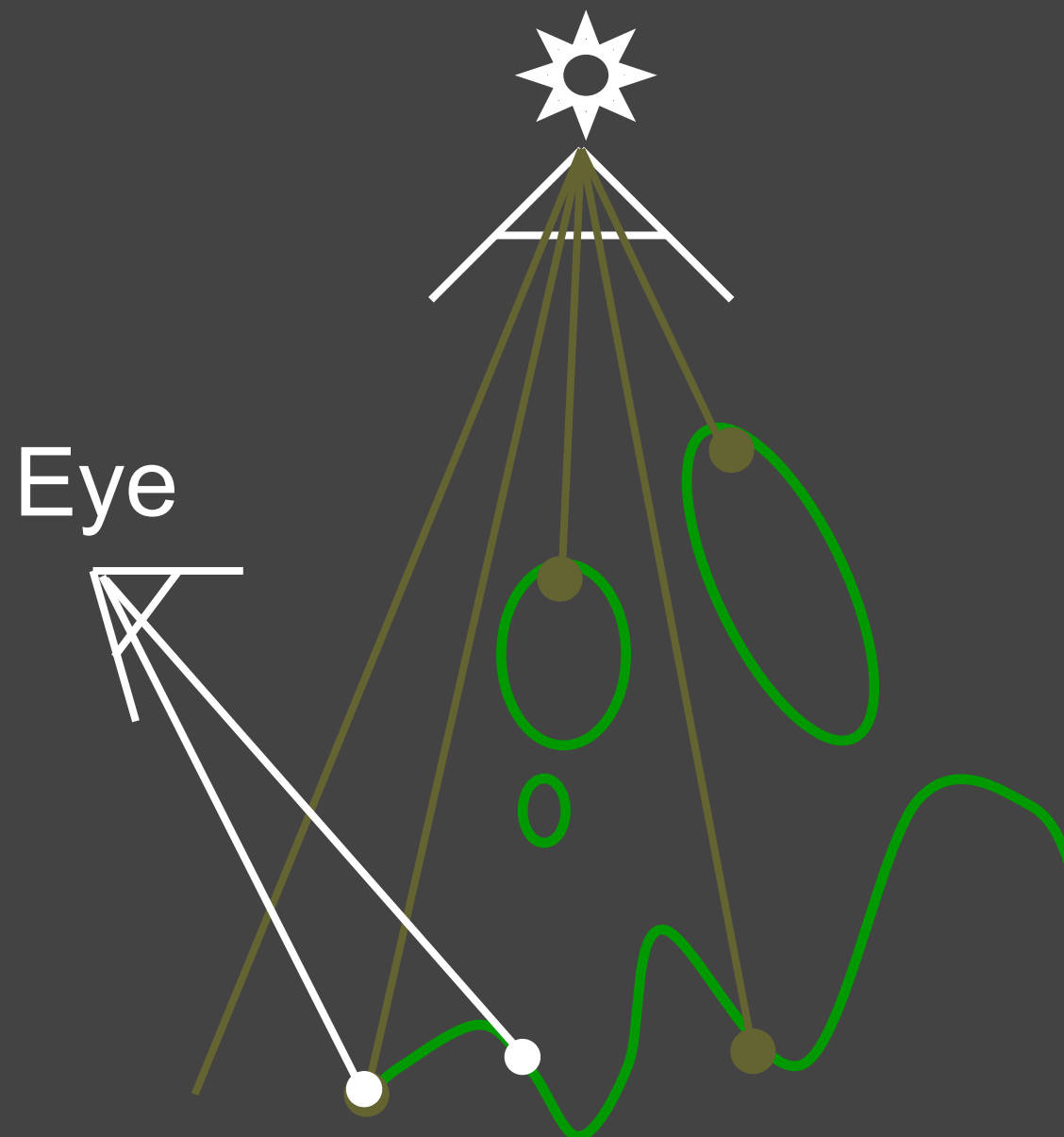
Pass 1: Render from Light

- Output a “depth texture” from the light source



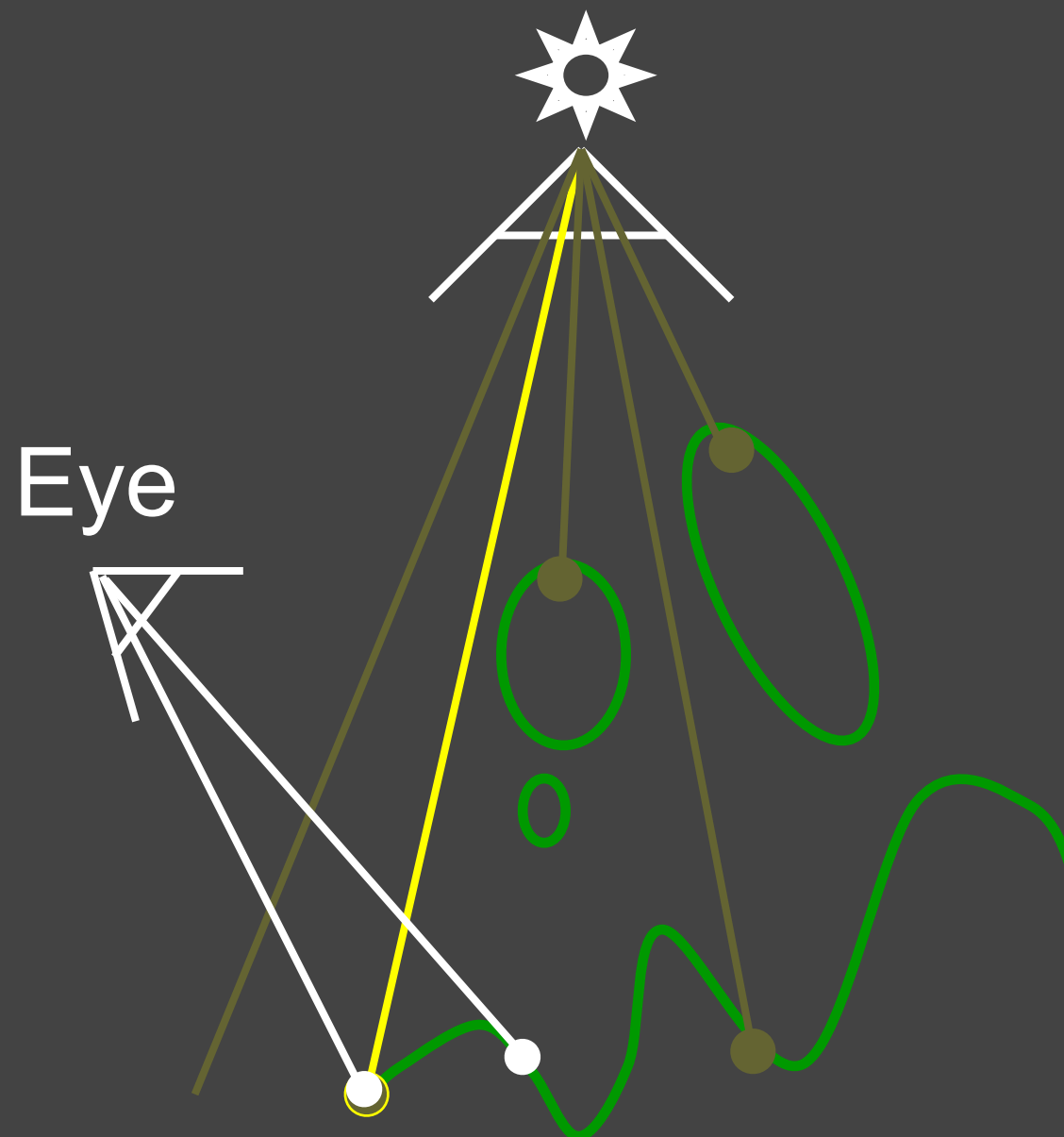
Pass 2: Render from Eye

- Render a standard image from the eye



Pass 2: Project to light for shadows

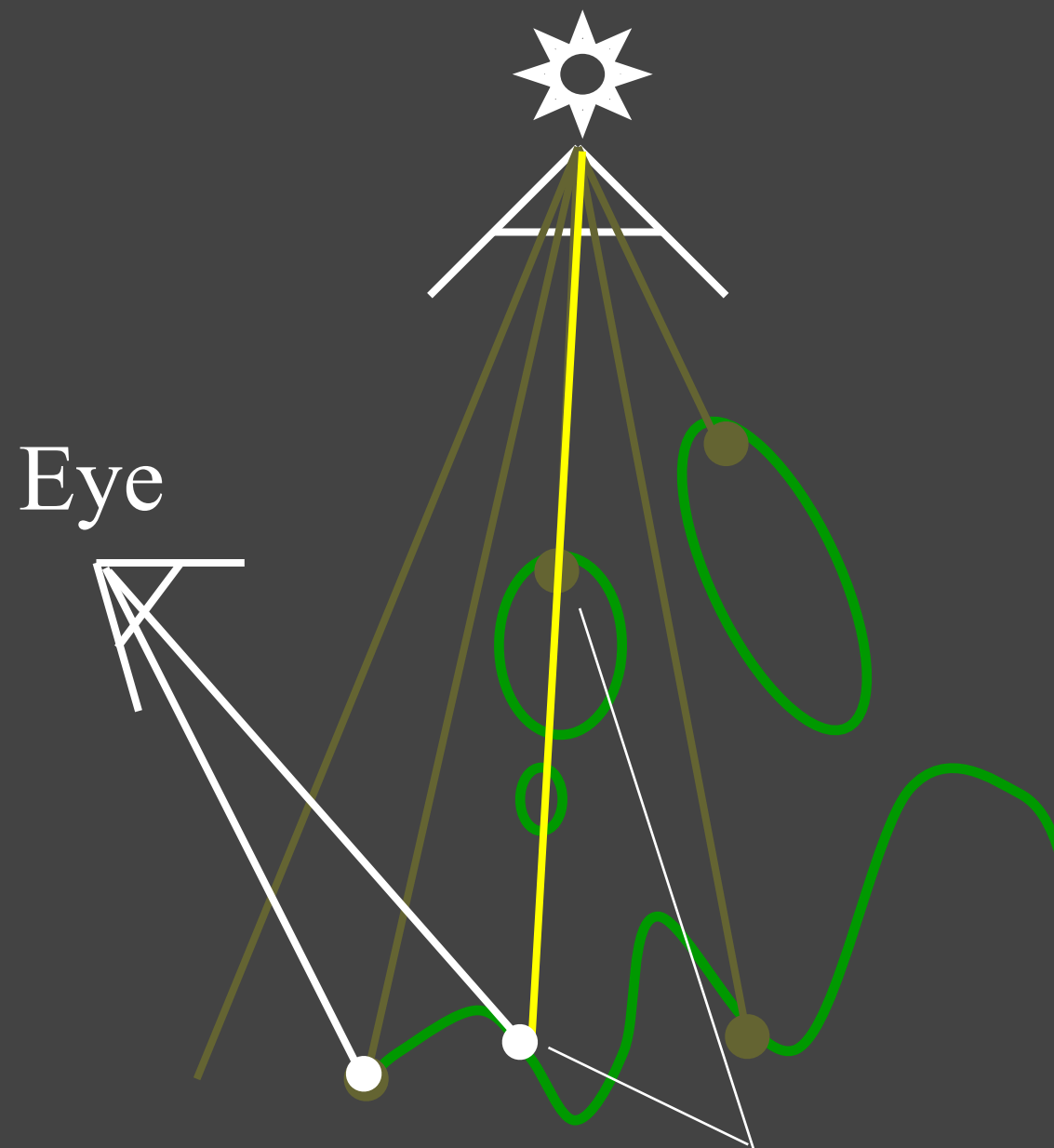
- Project visible points in eye view back to light source



(Reprojected) depths match for light and eye. **VISIBLE**

Pass 2: Project to light for shadows

- Project visible points in eye view back to light source

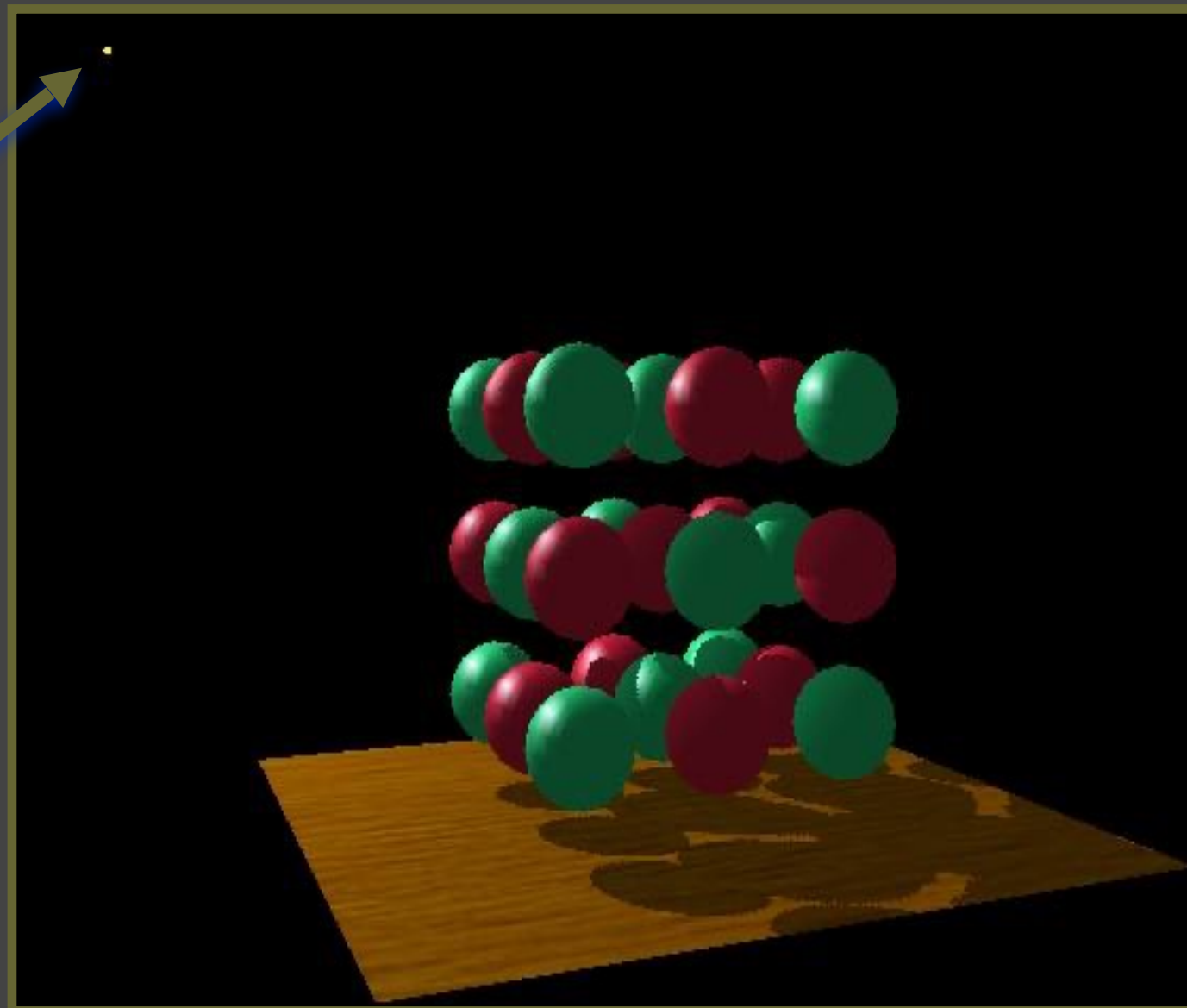


(Reprojected) depths from light, eye not the same. **BLOCKED!!**

Shadow Mapping Results

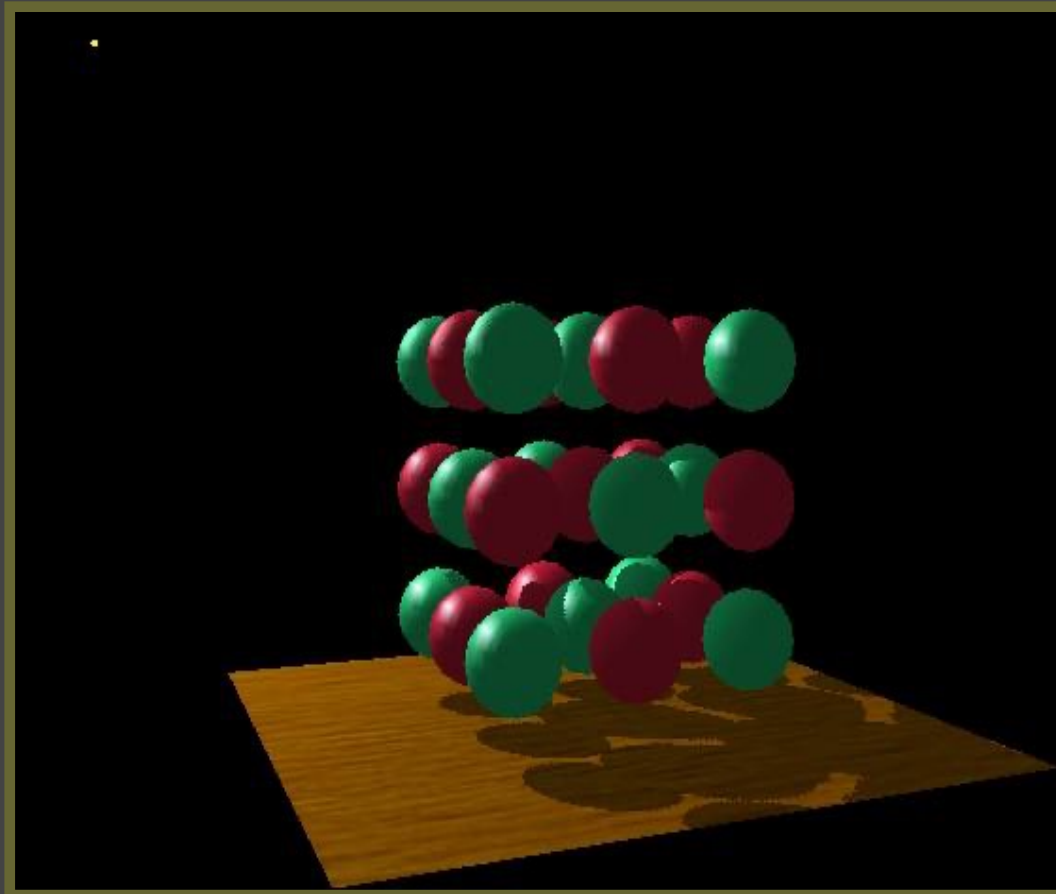
- A fairly complex scene with shadows

*the point
light source*

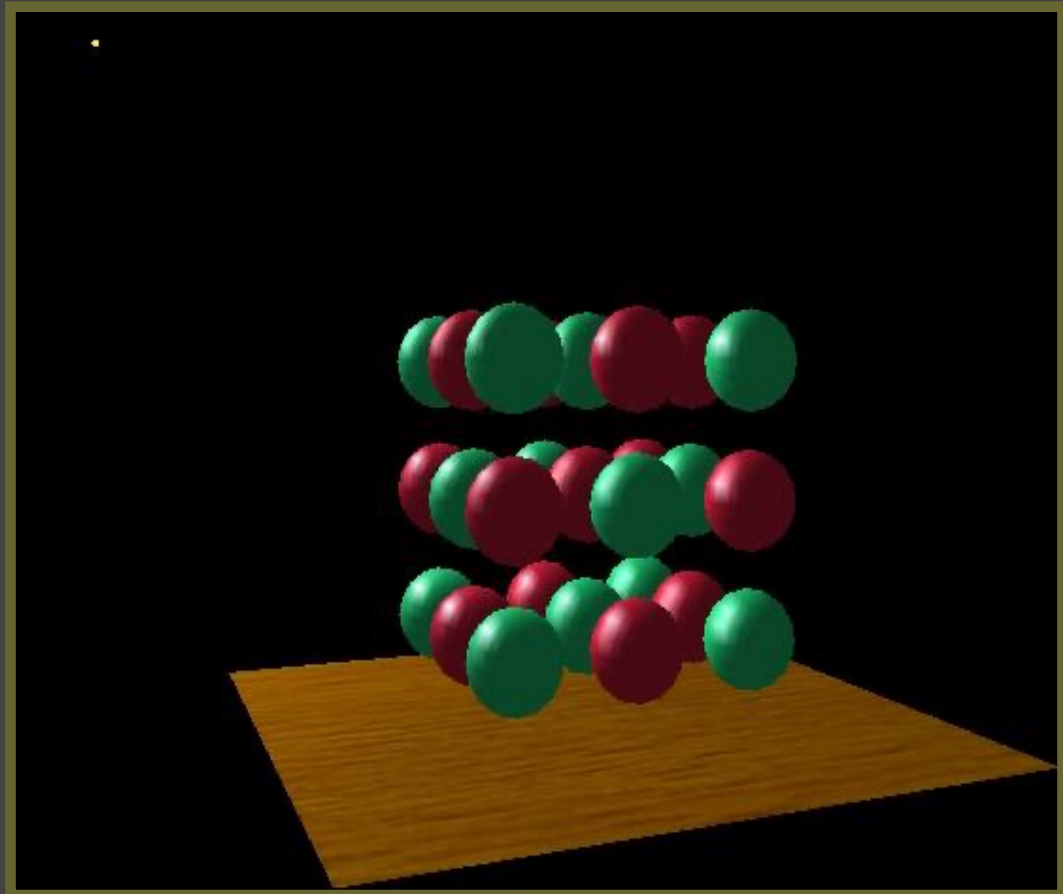


Shadow Mapping Results

- Compare with and without shadows



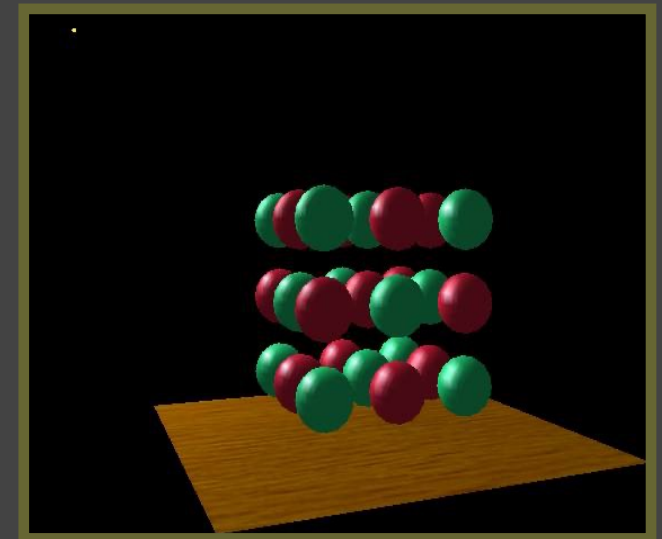
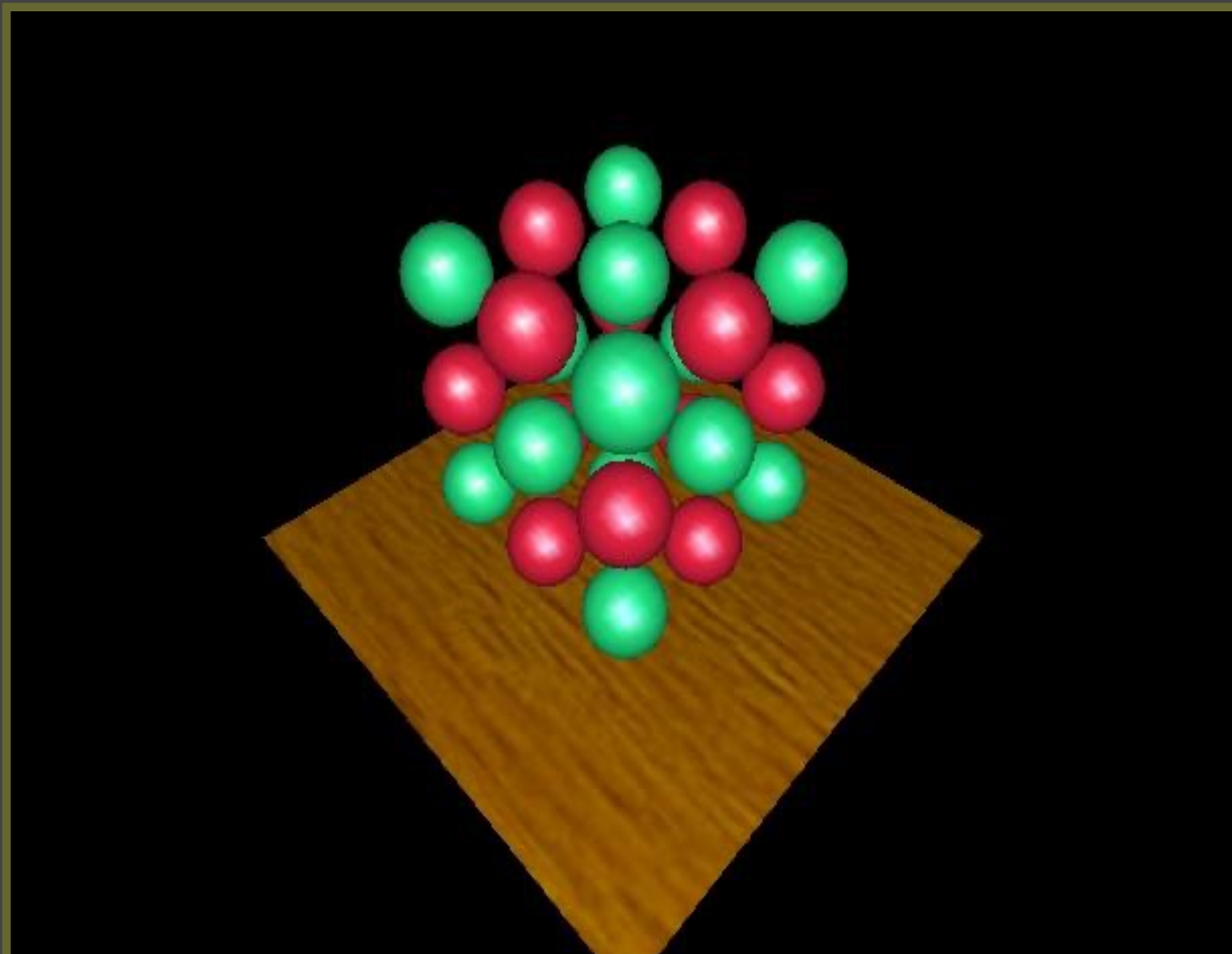
with shadows



without shadows

Visualizing Shadow Mapping

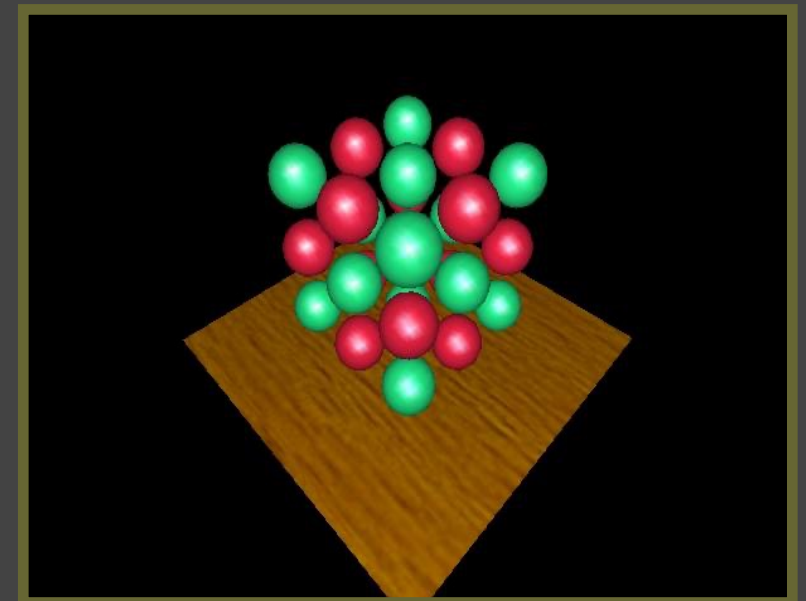
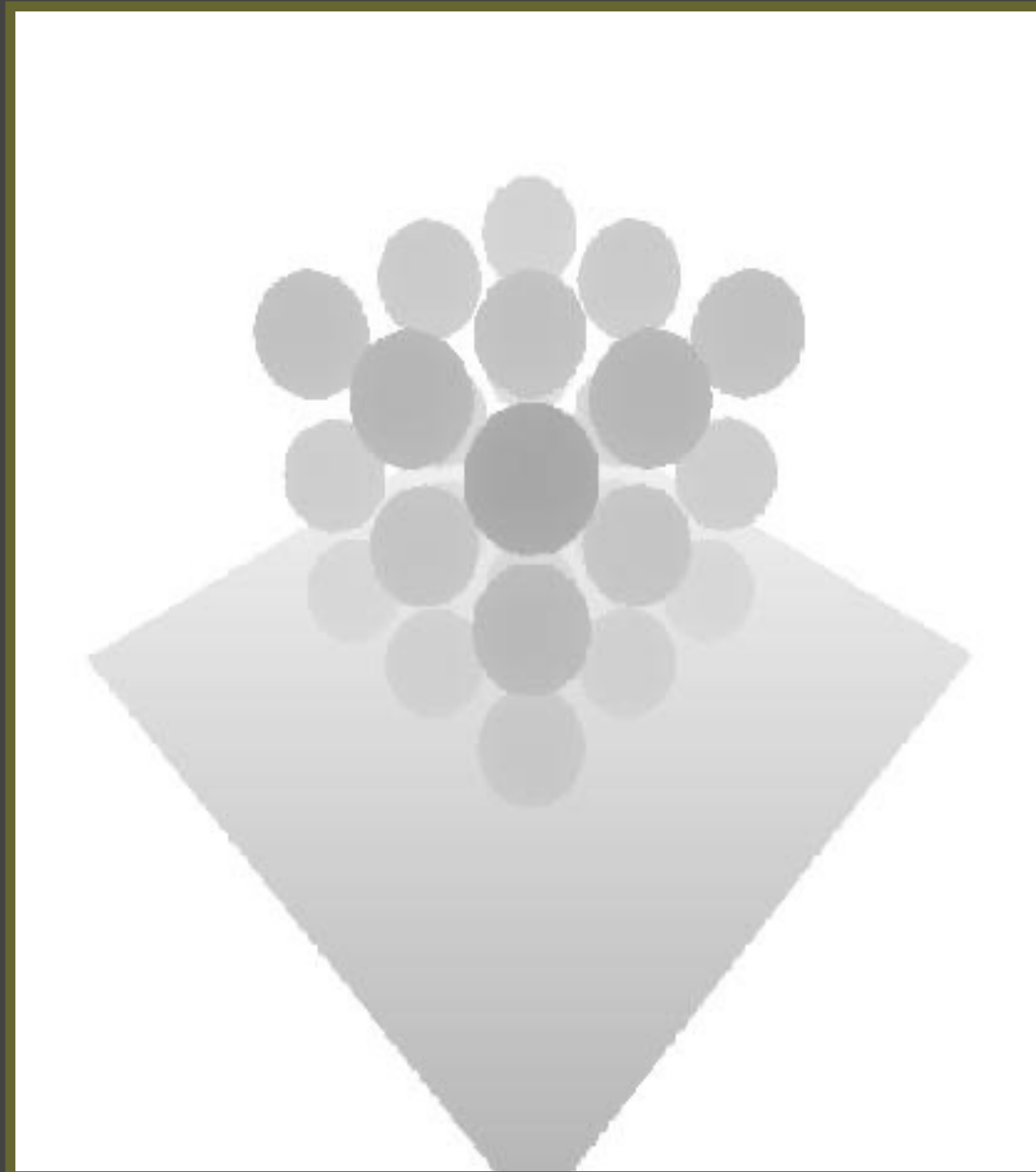
- The scene from the light's point-of-view



FYI: from the eye's point-of-view again

Visualizing Shadow Mapping

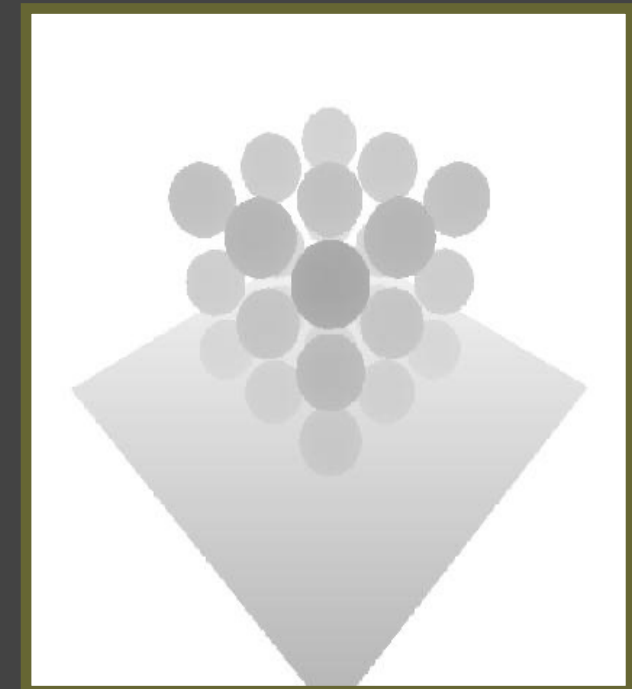
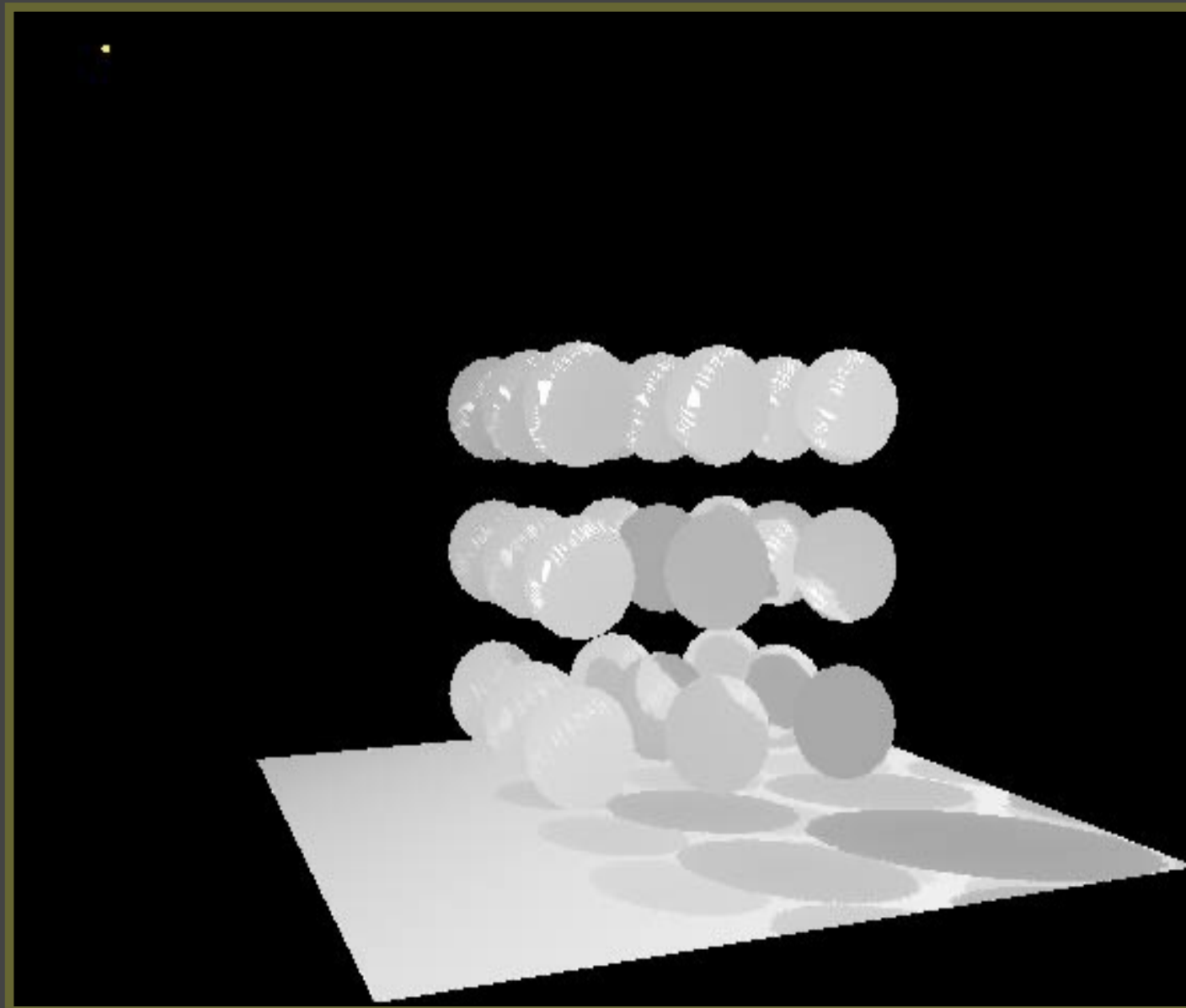
- The depth buffer from the light's point-of-view



FYI: from the light's point-of-view again

Visualizing Shadow Mapping

- Projecting the depth map onto the eye's view

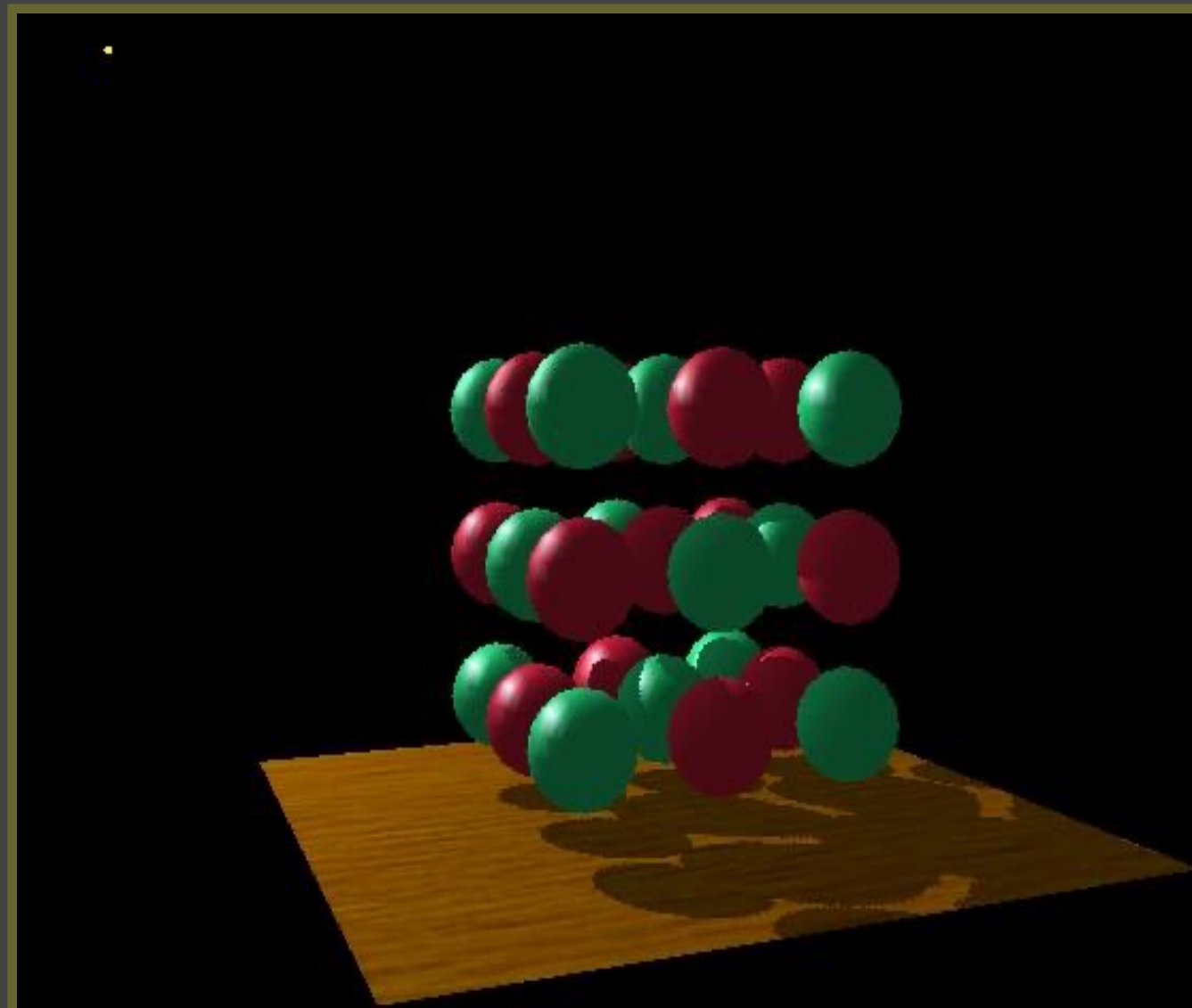


FYI: depth map for light's point-of-view again

Visualizing Shadow Mapping

- Scene with shadows

Notice how specular highlights never appear in shadows



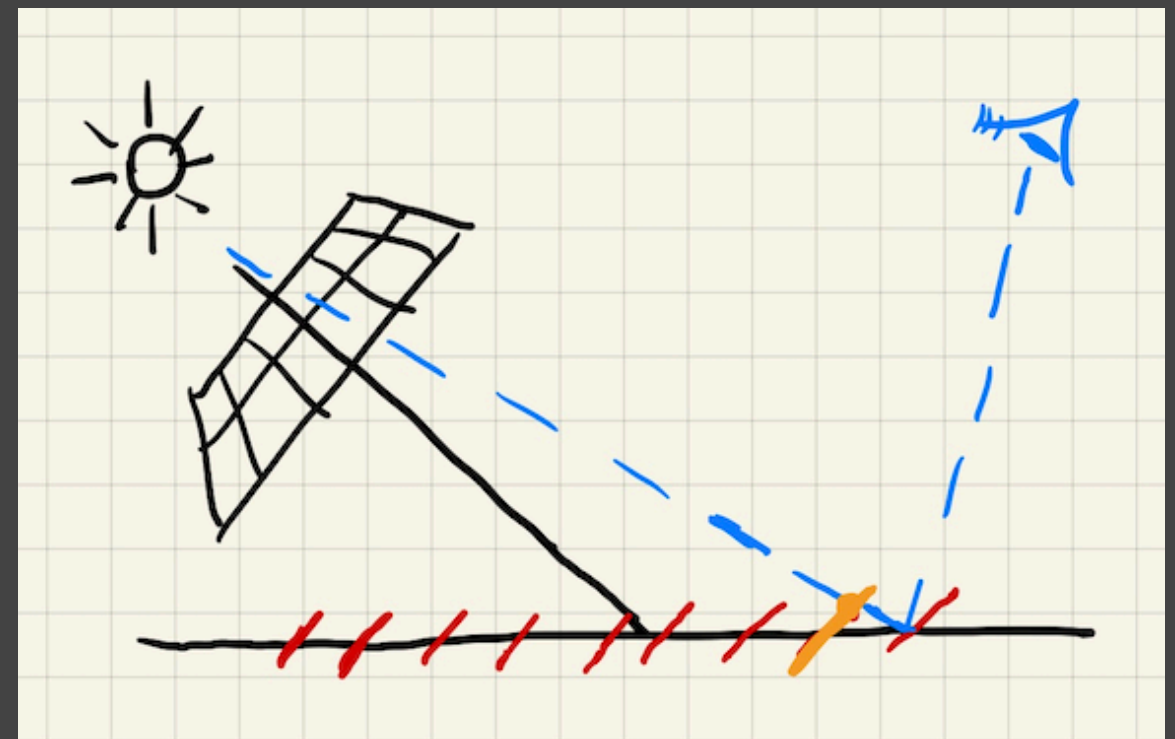
Notice how curved surfaces cast shadows on each other

Issues in Shadow Mapping

- Self occlusion
 - When is it most severe?



[Image from RTR4]

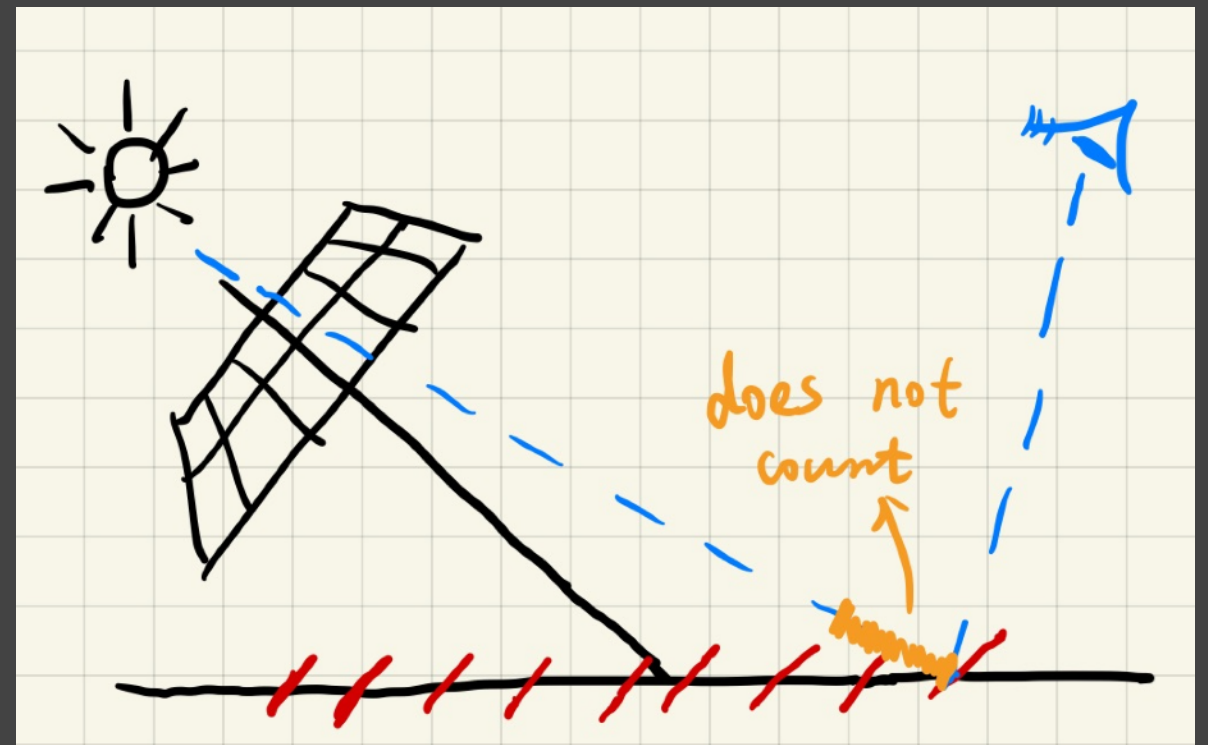


Issues in Shadow Mapping

- Adding a (variable) bias to reduce self occlusion
 - But introducing detached shadow issue

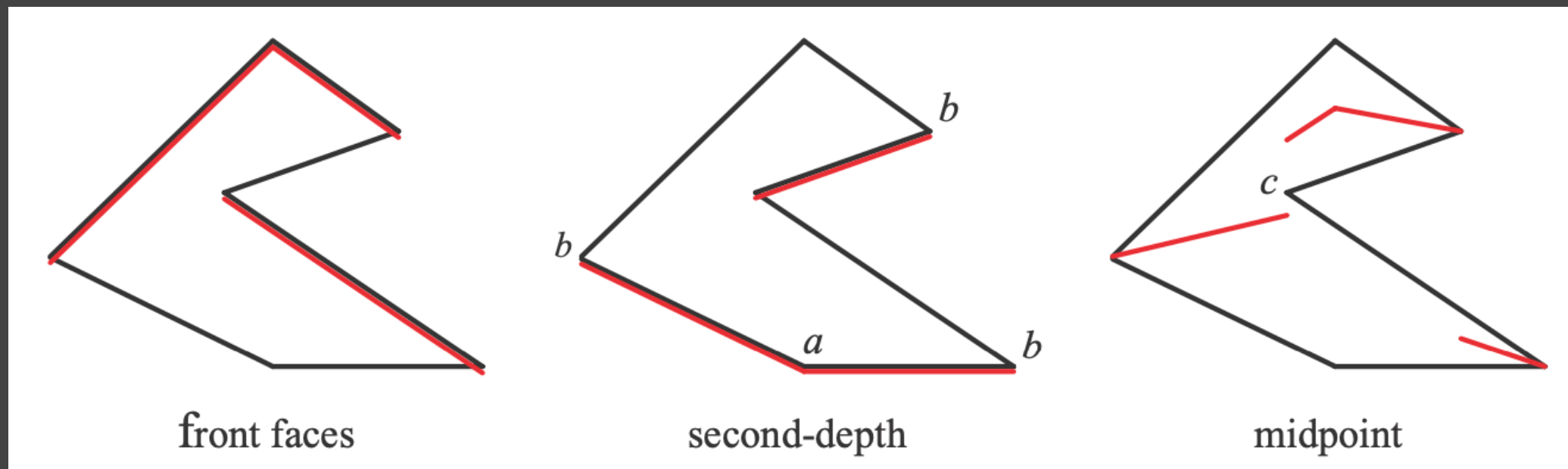


[Image from RTR4]



Issues in Shadow Mapping

- Second-depth shadow mapping*
 - Using the midpoint between first and second depths in SM
 - Unfortunately, requires objects to be watertight
 - And the overhead may not worth it

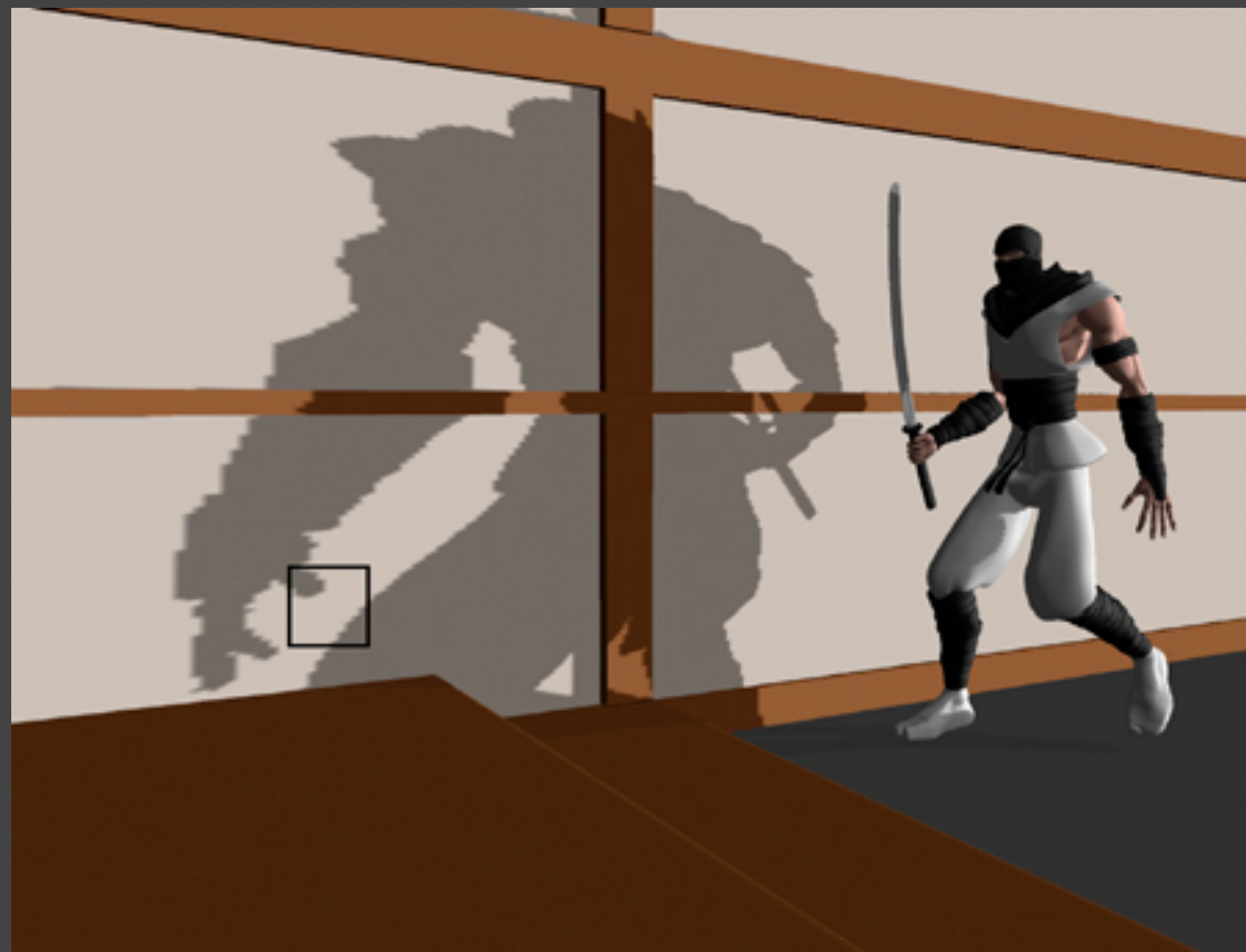


[Image from RTR4]

RTR does not trust in
COMPLEXITY

Issues in Shadow Mapping

- Aliasing



[https://developer.download.nvidia.com/books/HTML/gpugems/gpugems_ch11.html]

Questions?

Today

- Recap: shadow mapping
 - Issues from shadow mapping and solutions
- The math behind shadow mapping
- Percentage closer soft shadows
- Basic filtering techniques

Inequalities in Calculus

- There are a lot of useful inequalities in calculus

12. 设 $f(x)$ 和 $g(x)$ 在 $[a, b]$ 上都可积, 证明不等式:

(1) (Schwarz 不等式) $\left[\int_a^b f(x)g(x)dx \right]^2 \leq \int_a^b f^2(x)dx \cdot \int_a^b g^2(x)dx;$

(2) (Minkowski 不等式) <http://blog.csdn.net/>

$$\left\{ \int_a^b [f(x) + g(x)]^2 dx \right\}^{\frac{1}{2}} \leq \left\{ \int_a^b f^2(x) dx \right\}^{\frac{1}{2}} + \left\{ \int_a^b g^2(x) dx \right\}^{\frac{1}{2}}.$$

Approximation in RTR

- But in RTR, we care more about “approximately equal”
- An important approximation throughout RTR

$$\int_{\Omega} f(x)g(x) dx \approx \frac{\int_{\Omega} f(x) dx}{\int_{\Omega} dx} \cdot \int_{\Omega} g(x) dx$$

- When is it (more) accurate?

In Shadow Mapping

- Recall: the rendering equation with explicit visibility

$$L_o(\mathbf{p}, \omega_o) = \int_{\Omega^+} L_i(\mathbf{p}, \omega_i) f_r(\mathbf{p}, \omega_i, \omega_o) \cos \theta_i V(\mathbf{p}, \omega_i) d\omega_i$$

- Approximated as

$$L_o(\mathbf{p}, \omega_o) \approx \frac{\int_{\Omega^+} V(\mathbf{p}, \omega_i) d\omega_i}{\int_{\Omega^+} d\omega_i} \cdot \int_{\Omega^+} L_i(\mathbf{p}, \omega_i) f_r(\mathbf{p}, \omega_i, \omega_o) \cos \theta_i d\omega_i$$

In Shadow Mapping

$$L_o(\mathbf{p}, \omega_o) \approx \frac{\int_{\Omega^+} V(\mathbf{p}, \omega_i) d\omega_i}{\int_{\Omega^+} d\omega_i} \cdot \int_{\Omega^+} L_i(\mathbf{p}, \omega_i) f_r(\mathbf{p}, \omega_i, \omega_o) \cos \theta_i d\omega_i$$

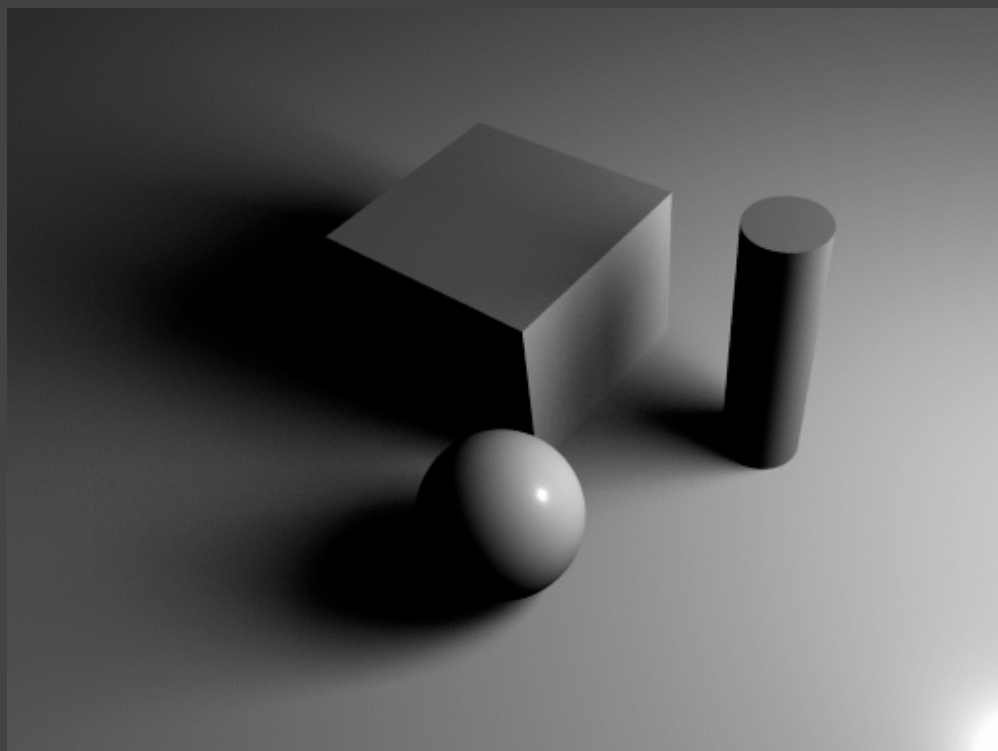
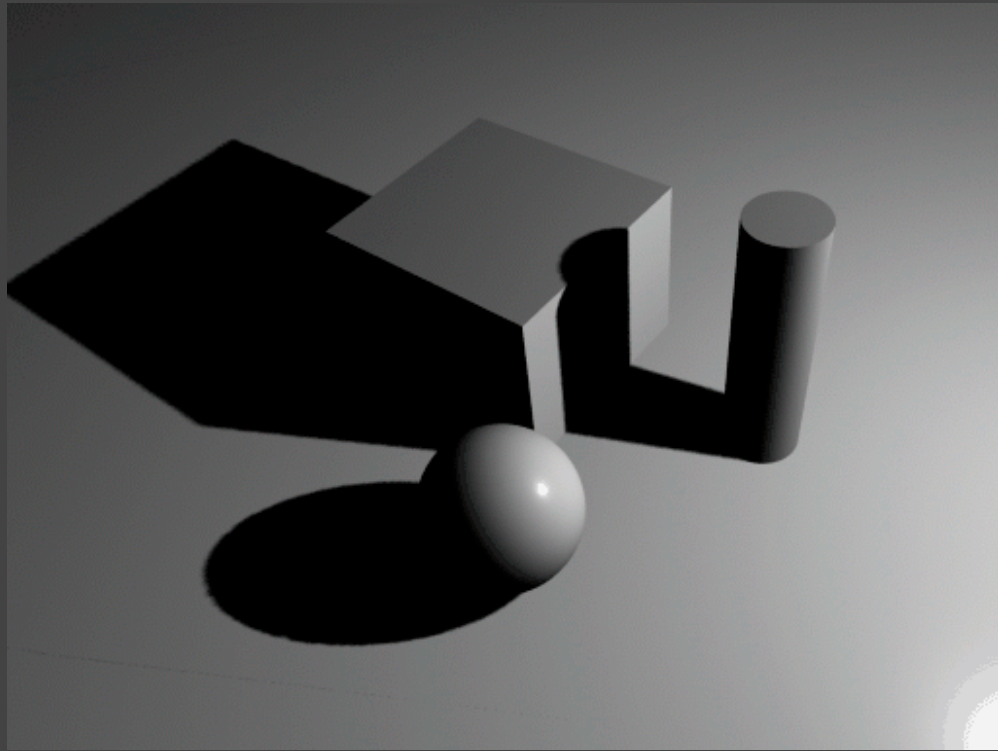
- When is it accurate?
 - Small support
(point / directional lighting)
 - Smooth integrand
(diffuse bsdf / constant radiance area lighting)
- We'll see it again in Ambient Occlusions, etc.

Questions?

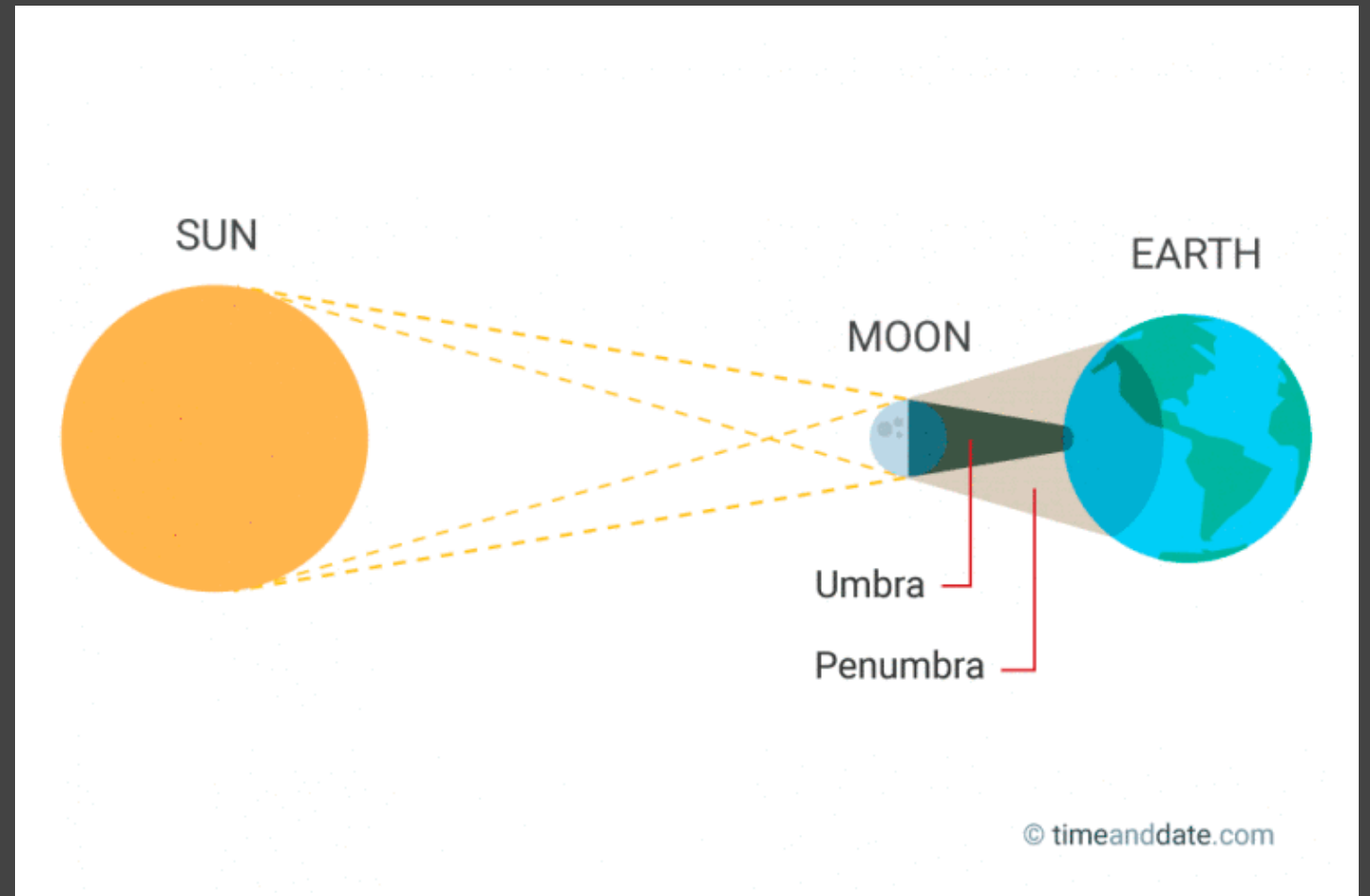
Today

- Recap: shadow mapping
 - Issues from shadow mapping and solutions
- The math behind shadow mapping
- Percentage closer soft shadows
- Basic filtering techniques

From Hard Shadows to Soft Shadows



[RenderMan]



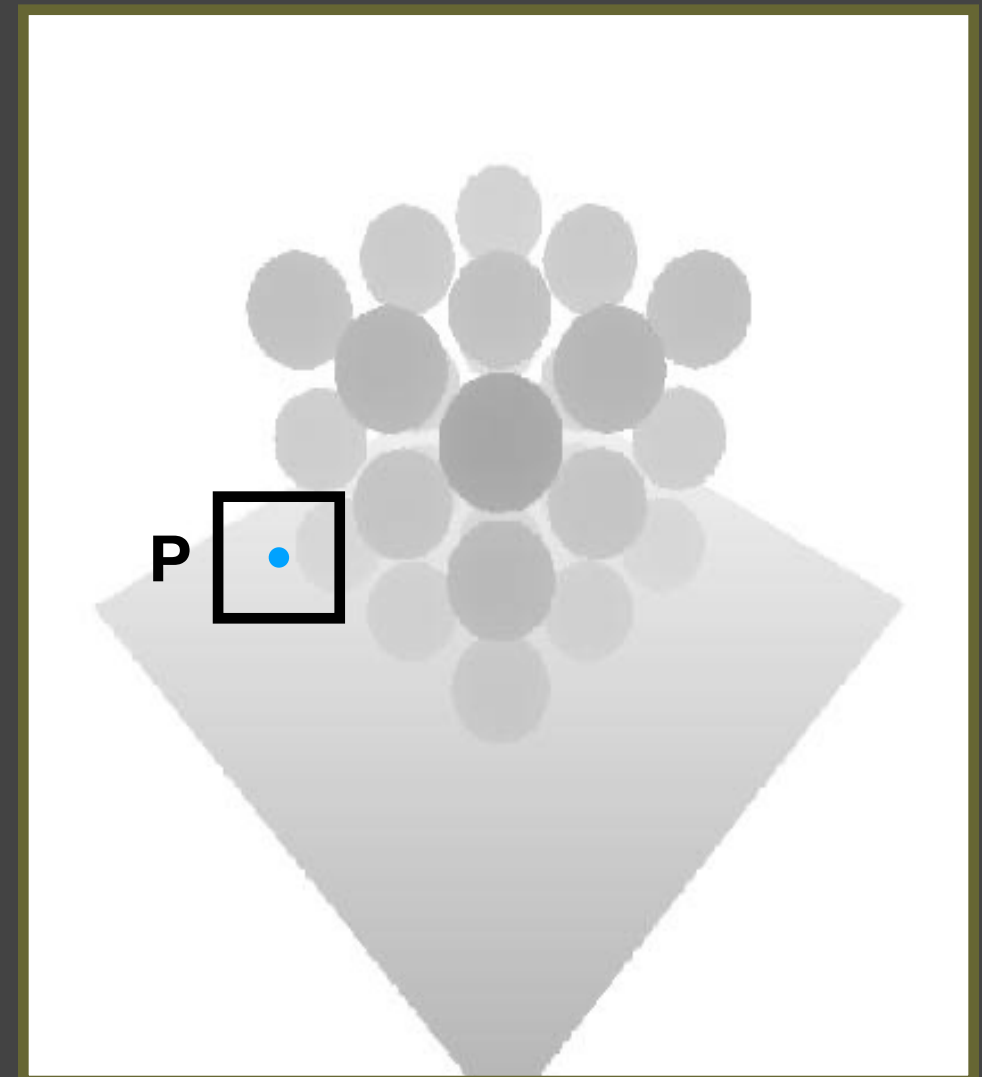
[<https://www.timeanddate.com/eclipse/umbra-shadow.html>]

Percentage Closer Filtering (PCF)

- Provides **anti-aliasing** at shadows' edges
 - Not for soft shadows (PCSS is, introducing later)
 - **Filtering the results of shadow comparisons**
- Why not filtering the shadow map?
 - Texture filtering just averages color components, i.e. you'll get blurred shadow map first
 - Averaging depth values, then comparing, you still get a **binary** visibility

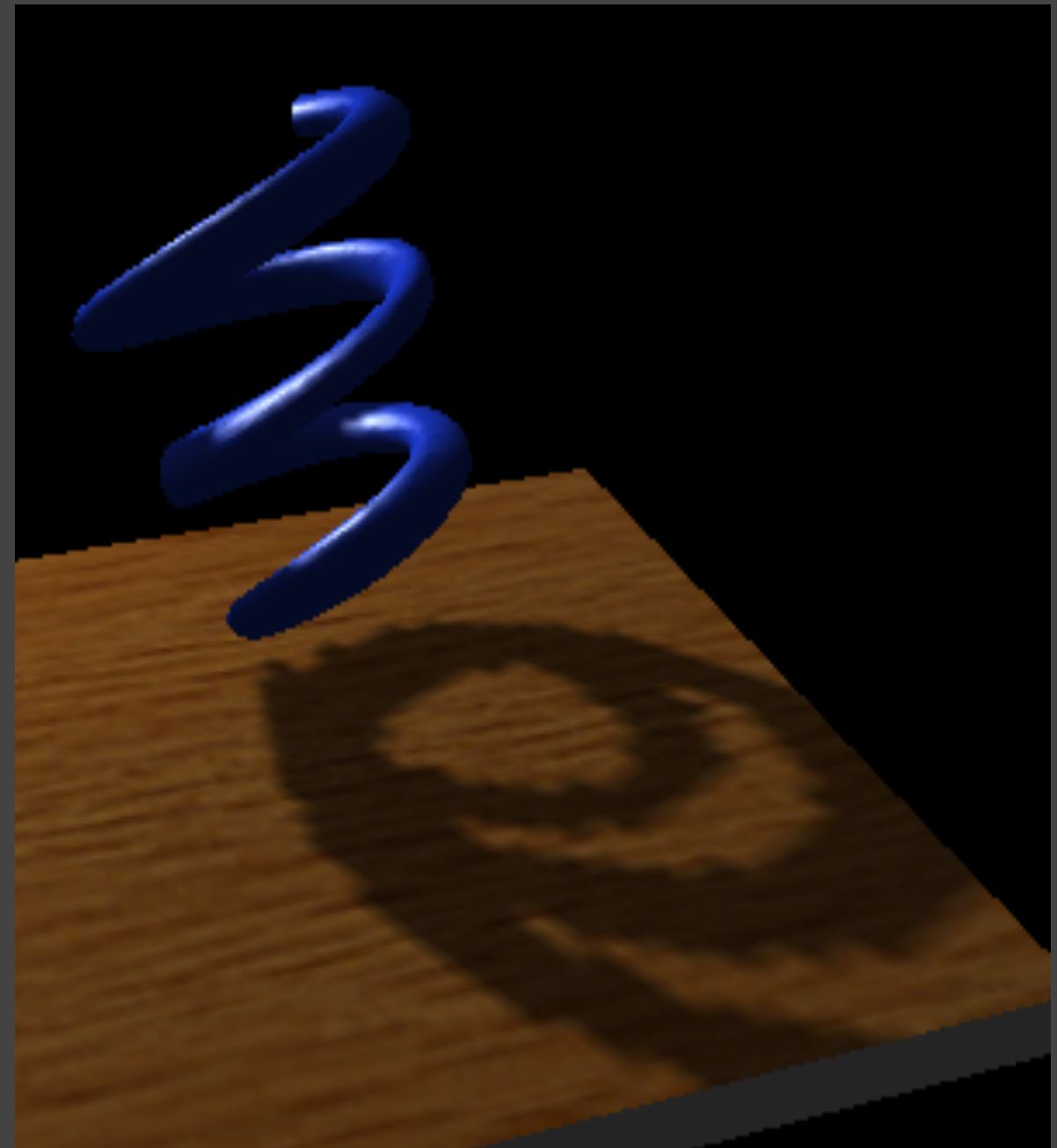
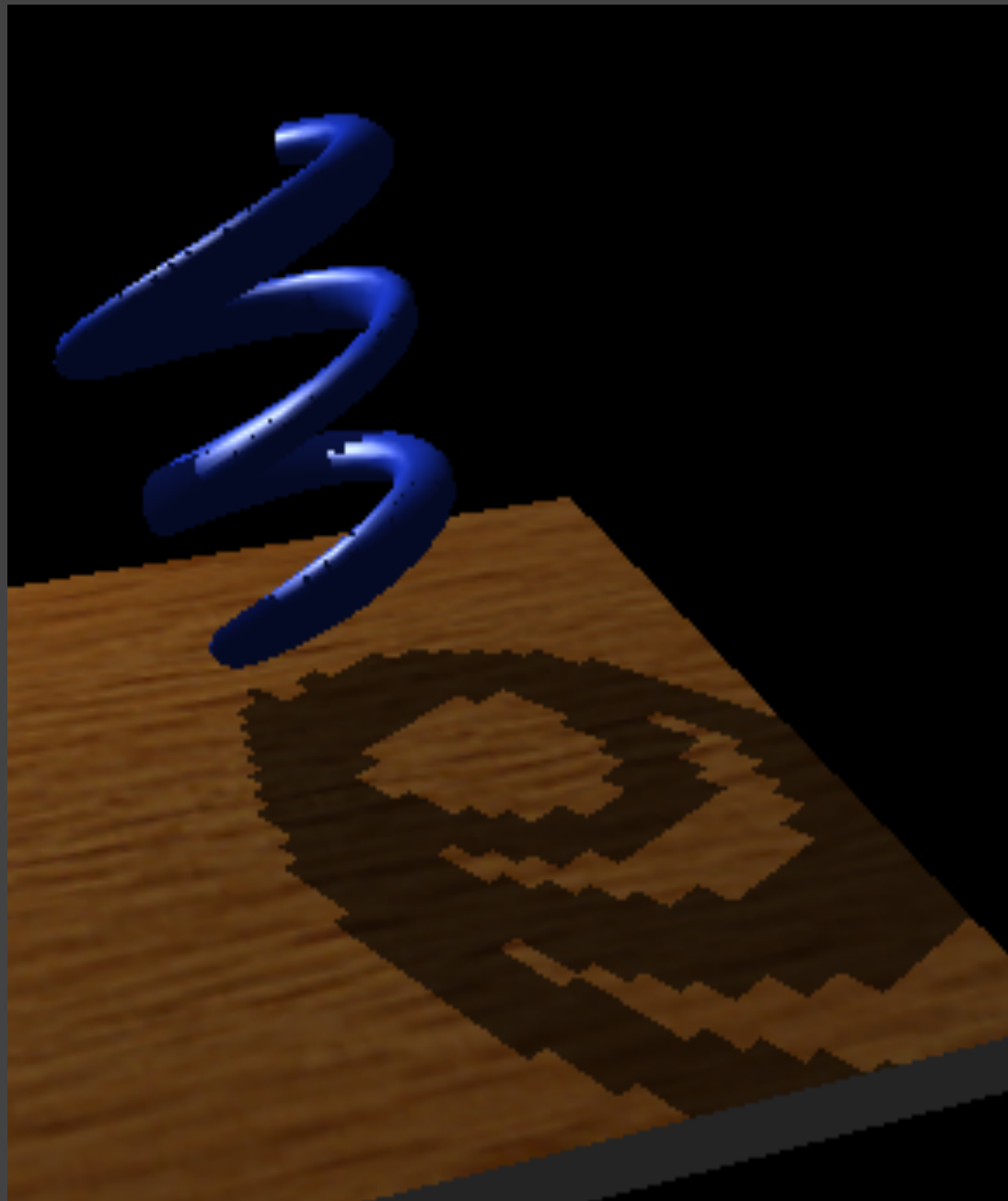
Percentage Closer Filtering (PCF)

- Solution [Reeves, SIGGRAPH 87]
 - Perform multiple (e.g. 7x7) depth comparisons for each fragment
 - Then, averages **results of** comparisons
 - e.g. for point P on the floor,
 - (1) compare its depth with all pixels in the red box, e.g. 3x3
 - (2) get the compared results, e.g.
1, 0, 1,
1, 0, 1,
1, 1, 0,
 - (3) take avg. to get visibility, e.g. 0.667



Percentage Closer Filtering

Again, not soft shadows in the umbra/penumbra sense



Percentage Closer Filtering



Percentage Closer Filtering

- Does filtering size matter?
 - Small -> sharper
 - Large -> softer
- Can we use PCF to achieve soft shadow effects?
- Key thoughts
 - From hard shadows to soft shadows
 - What's the **correct size** to filter?
 - Is it uniform?

Percentage Closer Soft Shadows

- Key observation [Fernando et al.]
 - Where is sharper? Where is softer?

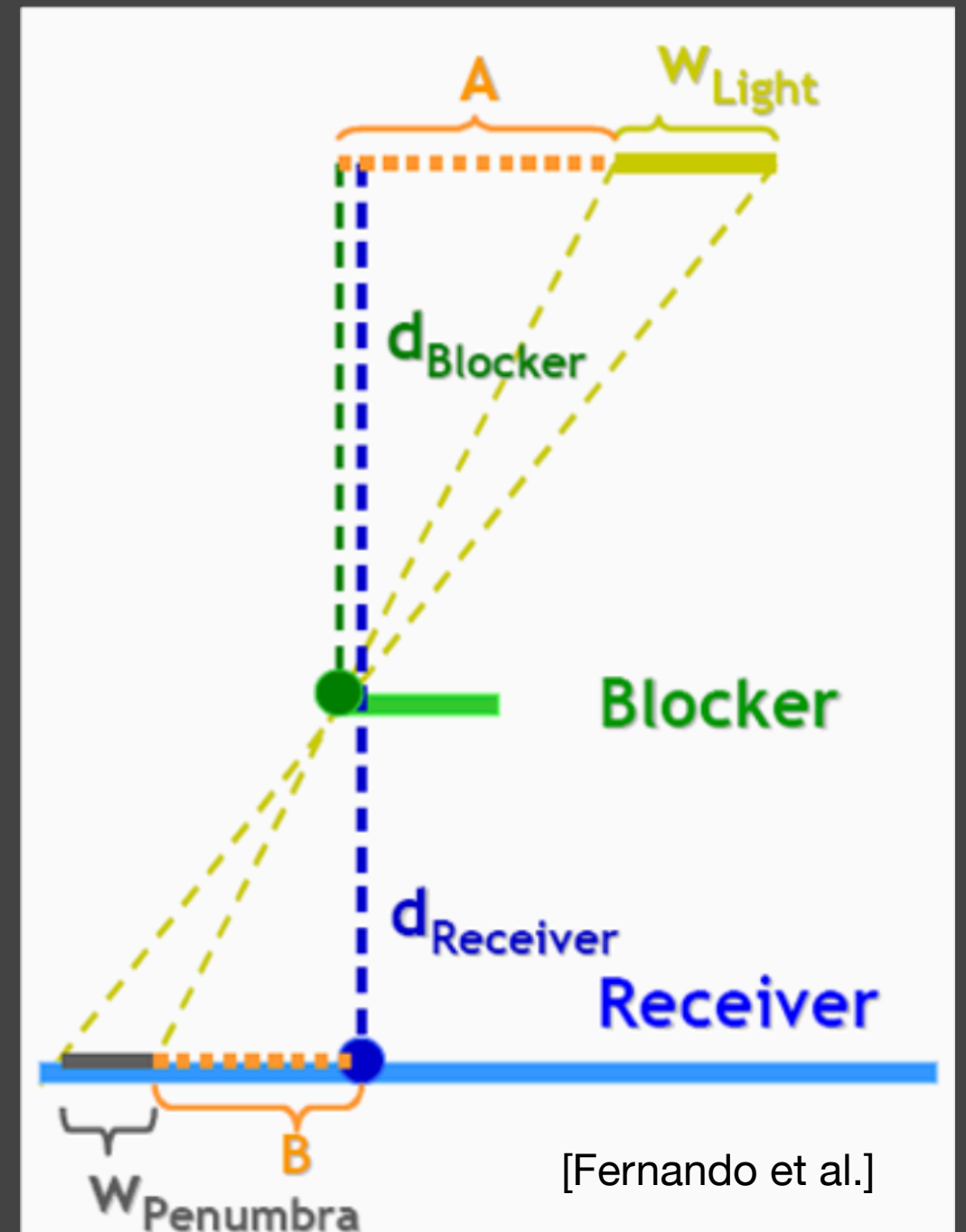


[<https://graphicdesign.stackexchange.com/questions/71734/transfer-the-shadow-of-an-object-on-white-paper-to-ruled-paper>]

Percentage Closer Soft Shadows

- Key conclusion
 - Filter size \leftrightarrow blocker distance
 - More accurately, **relative average** projected blocker depth!
- A mathematical “translation”

$$w_{Penumbra} = (d_{Receiver} - d_{Blocker}) \cdot w_{Light} / d_{Blocker}$$

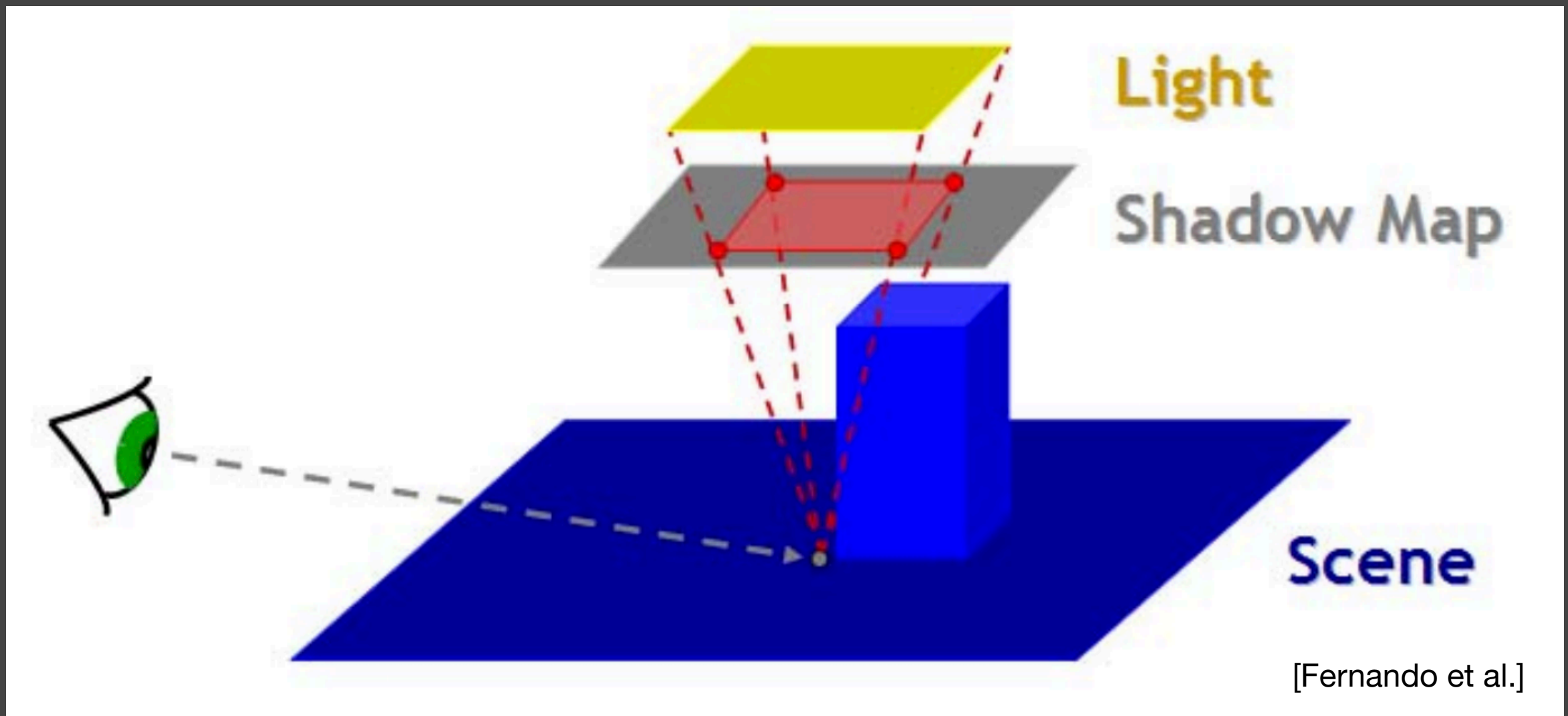


Percentage Closer Soft Shadows

- Now the only question:
 - What's the blocker depth d_{Blocker}
- The complete algorithm of PCSS
 - Step 1: Blocker search
(getting the average blocker depth **in a certain region**)
 - Step 2: Penumbra estimation
(use the average blocker depth to determine filter size)
 - Step 3: Percentage Closer Filtering
- Which region to perform blocker search?
 - Can be set constant (e.g. 5x5), but can be better with heuristics

Percentage Closer Soft Shadows

- Which region (on the shadow map) to perform blocker search?
 - depends on the light size
 - and receiver's distance from the light



Percentage Closer Soft Shadows

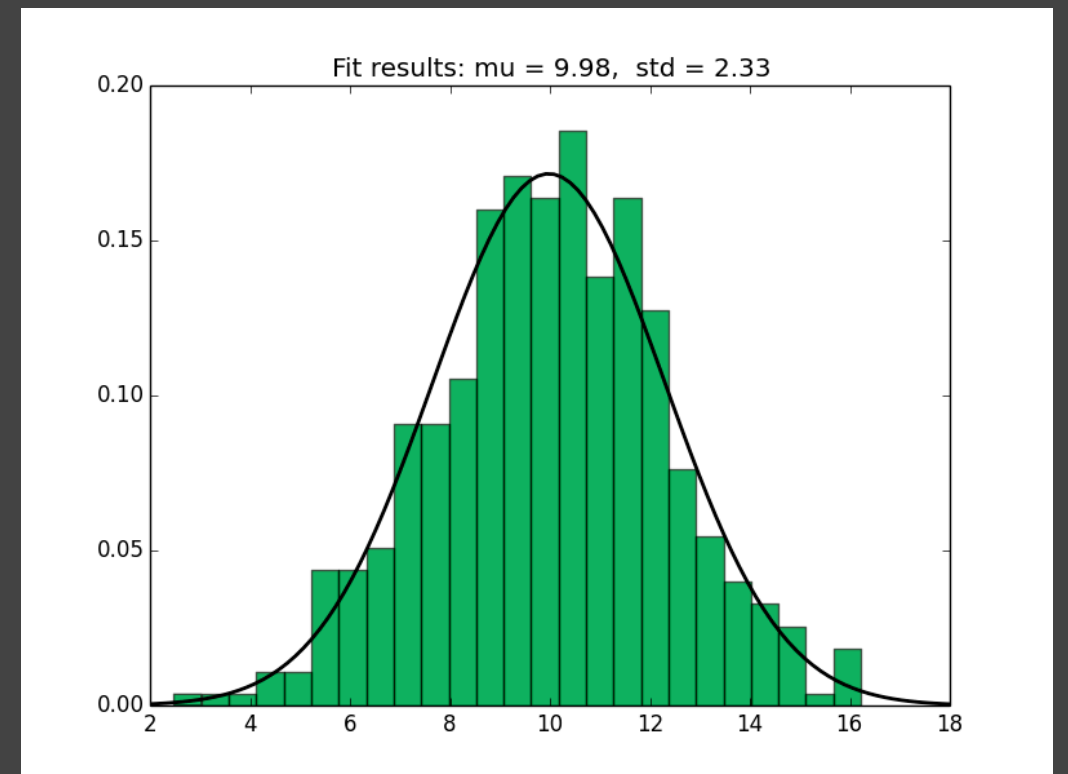


Video game: Dying Light

Questions?

Next Lecture

- Basic filtering techniques
- Variance soft shadow mapping
- MIPMAP and Summed-Area Variance Shadow Maps
- Moment shadow mapping



Thank you!