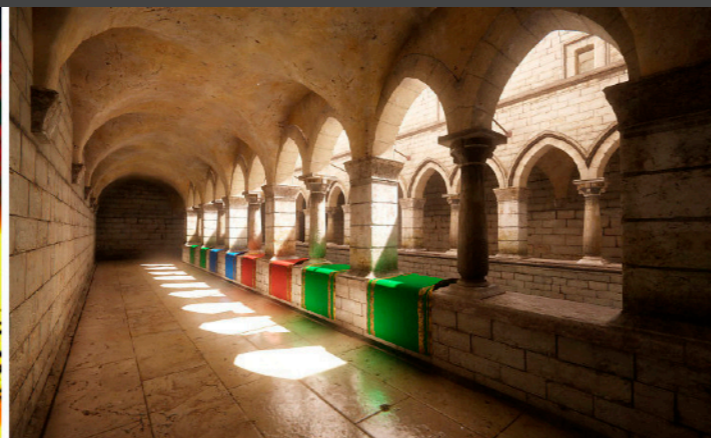


Real-Time High Quality Rendering

GAMES202, Lingqi Yan, UC Santa Barbara

Lecture 10: Real-Time Physically-Based Materials (surface models)



Announcements

- Correction: 2/3 contents covered after today's lecture!
- GAMES202 homework late submission is open now!
- GAMES101 graders
 - Now we have a few applications for graders!
 - Will soon reach out to get started!
- GAMES101 now has 599K views on Bilibili!

Last Lecture

- Real-Time Global Illumination (screen space cont.)
 - Screen Space Directional Occlusion (SSDO)
 - Screen Space Reflection (SSR)
- Real-Time Physically-Based Materials

Today

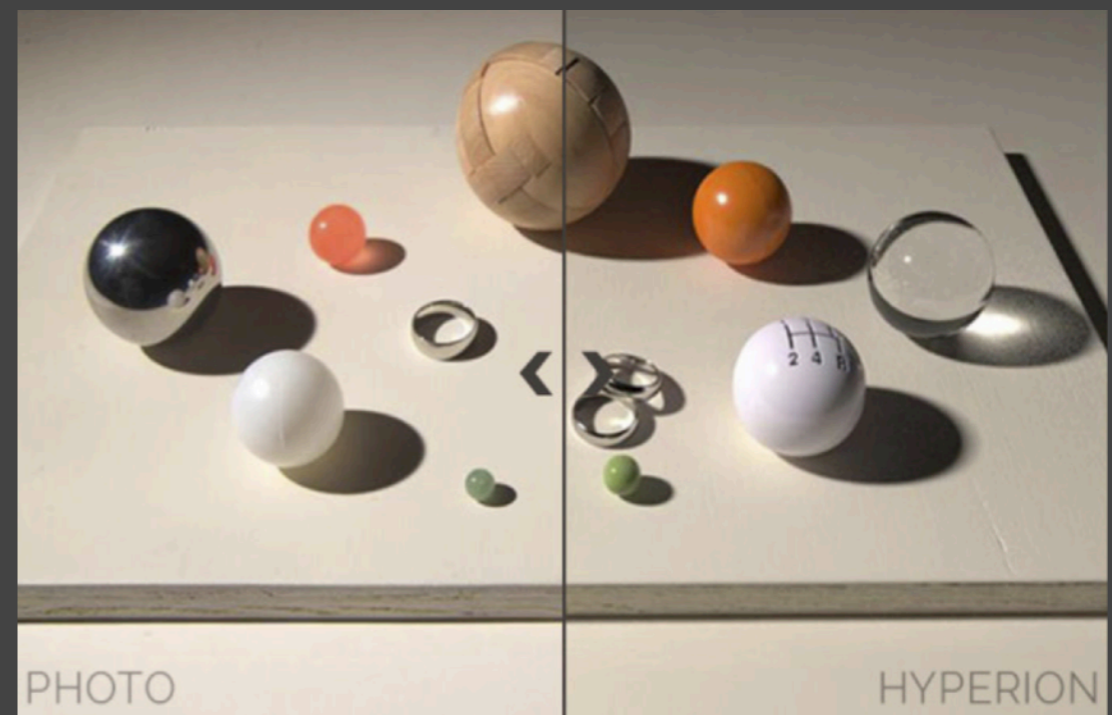
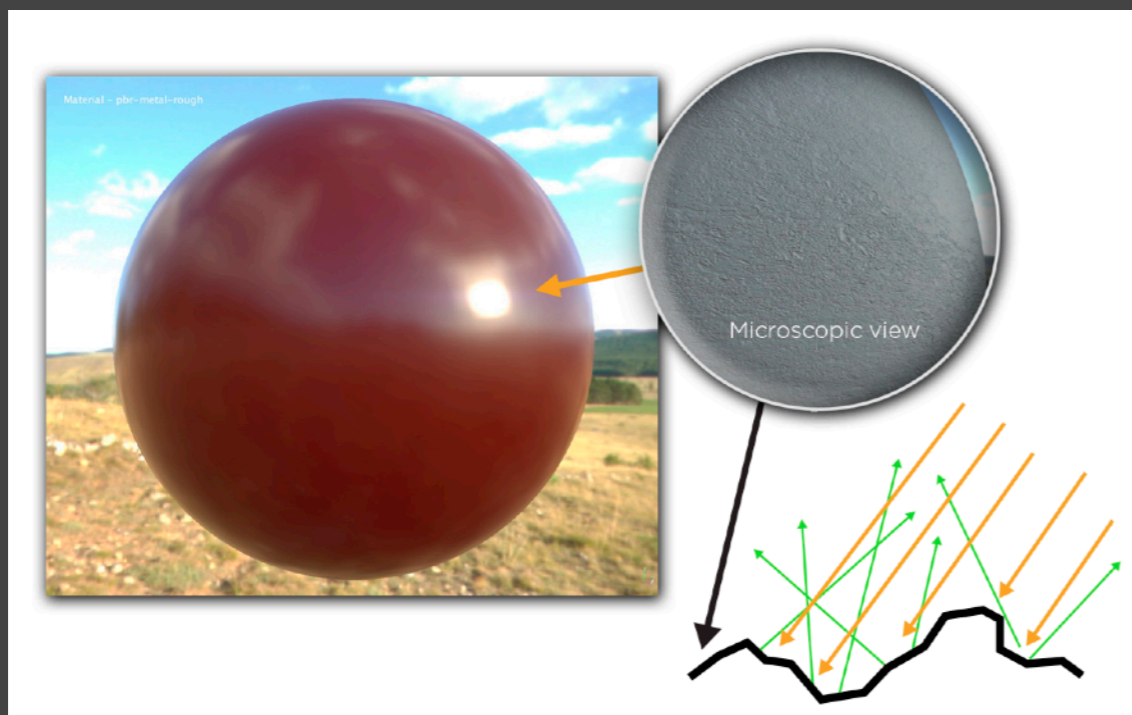
- Real-Time Physically-Based Materials
 - Microfacet BRDF
 - Disney principled BRDF
- Shading with microfacet BRDFs under polygonal lighting
 - Linearly Transformed Cosines (LTC)

PBR and PBR Materials

- Physically-Based Rendering (PBR)
 - Everything in rendering should be physically based
 - Materials, lighting, camera, light transport, etc.
 - Not just materials, but usually referred to as materials :)
- PBR materials in RTR
 - The RTR community is much behind the offline community
 - “PB” in RTR is usually not actually physically based :)

PBR Materials in RTR

- PBR materials in RTR
 - **For surfaces**, mostly just microfacet models (used wrong so not PBR) and Disney principled BRDFs (artist friendly but still not PBR)



PBR Materials in RTR

- PBR materials in RTR
 - **For surfaces**, mostly just microfacet models and Disney principled BRDFs
 - **For volumes**, mostly focused on fast and approximate single scattering and multiple scattering (for cloud, hair, skin, etc.)



[Lara Croft from the Tomb Raider series]

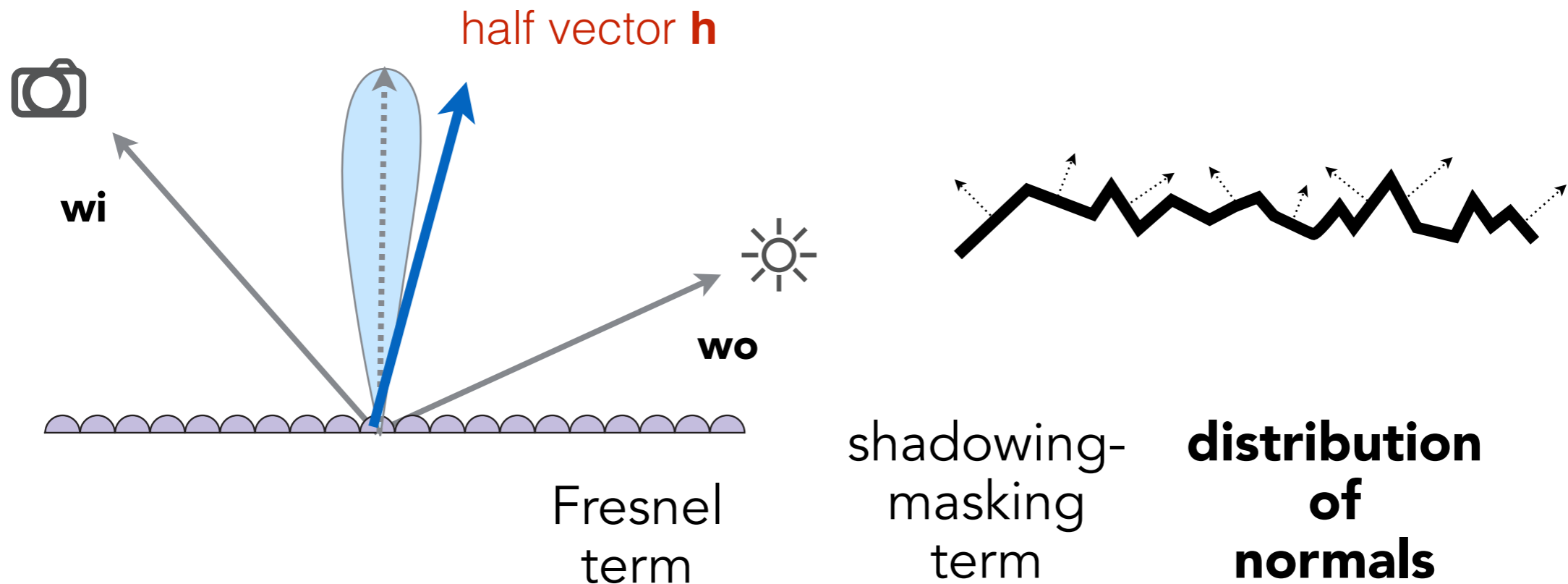
PBR Materials in RTR

- PBR materials in RTR
 - **For surfaces**, mostly just microfacet models (used wrong so not PBR) and Disney principled BRDFs (artist friendly but still not PBR)
 - **For volumes**, mostly focused on fast and approximate single scattering and multiple scattering (for cloud, hair, skin, etc.)
 - Usually not much new theory, but a lot of implementation hacks*
 - Still, performance (speed) is the key factor to consider

Recap: Microfacet BRDF

Microfacet BRDF

- What kind of microfacets reflect w_i to w_o ?
(hint: microfacets are mirrors)



$$f(\mathbf{i}, \mathbf{o}) = \frac{\mathbf{F}(\mathbf{i}, \mathbf{h}) \mathbf{G}(\mathbf{i}, \mathbf{o}, \mathbf{h}) \mathbf{D}(\mathbf{h})}{4(\mathbf{n}, \mathbf{i})(\mathbf{n}, \mathbf{o})}$$

The Fresnel Term

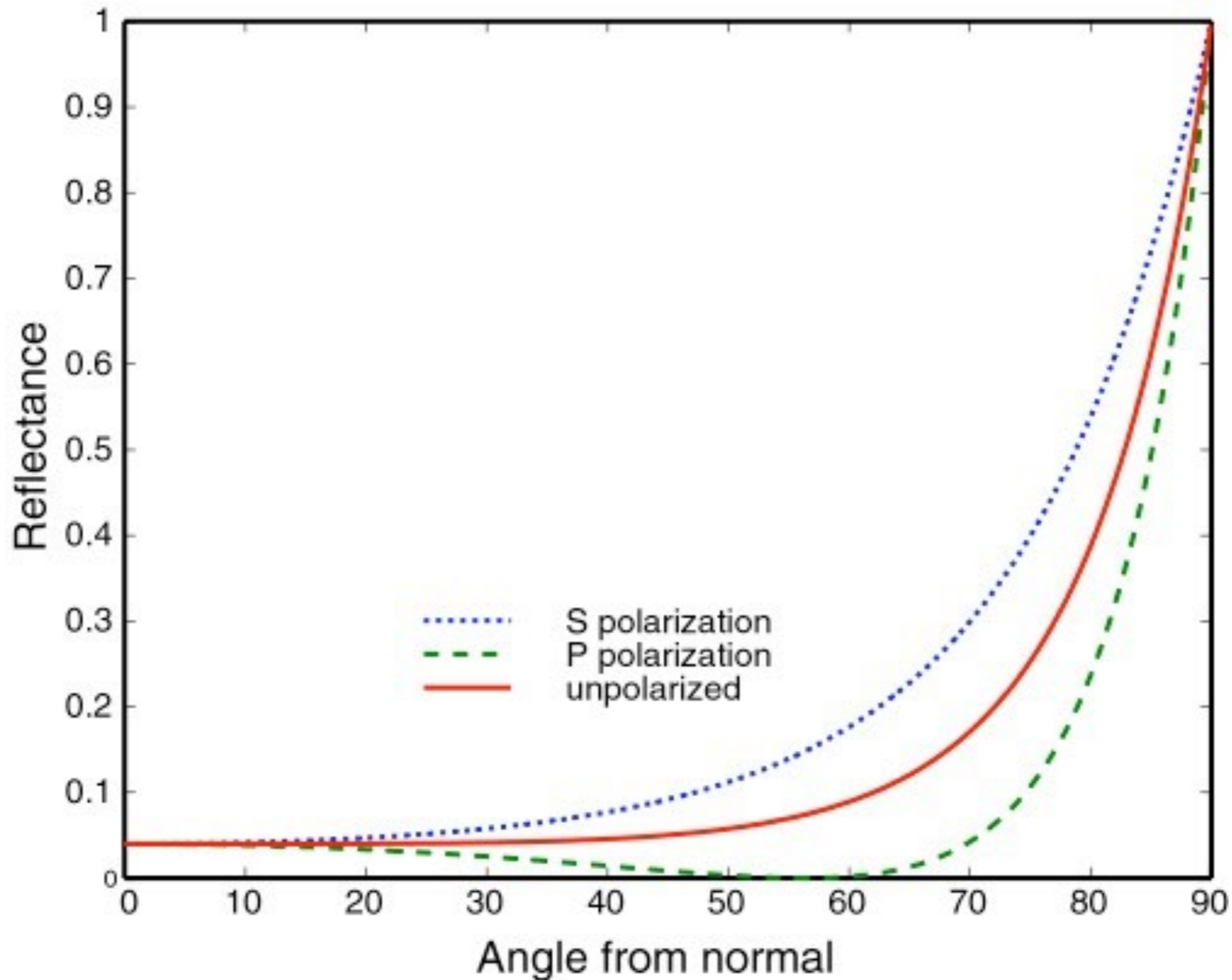
Reflectance depends on incident angle (and polarization of light)



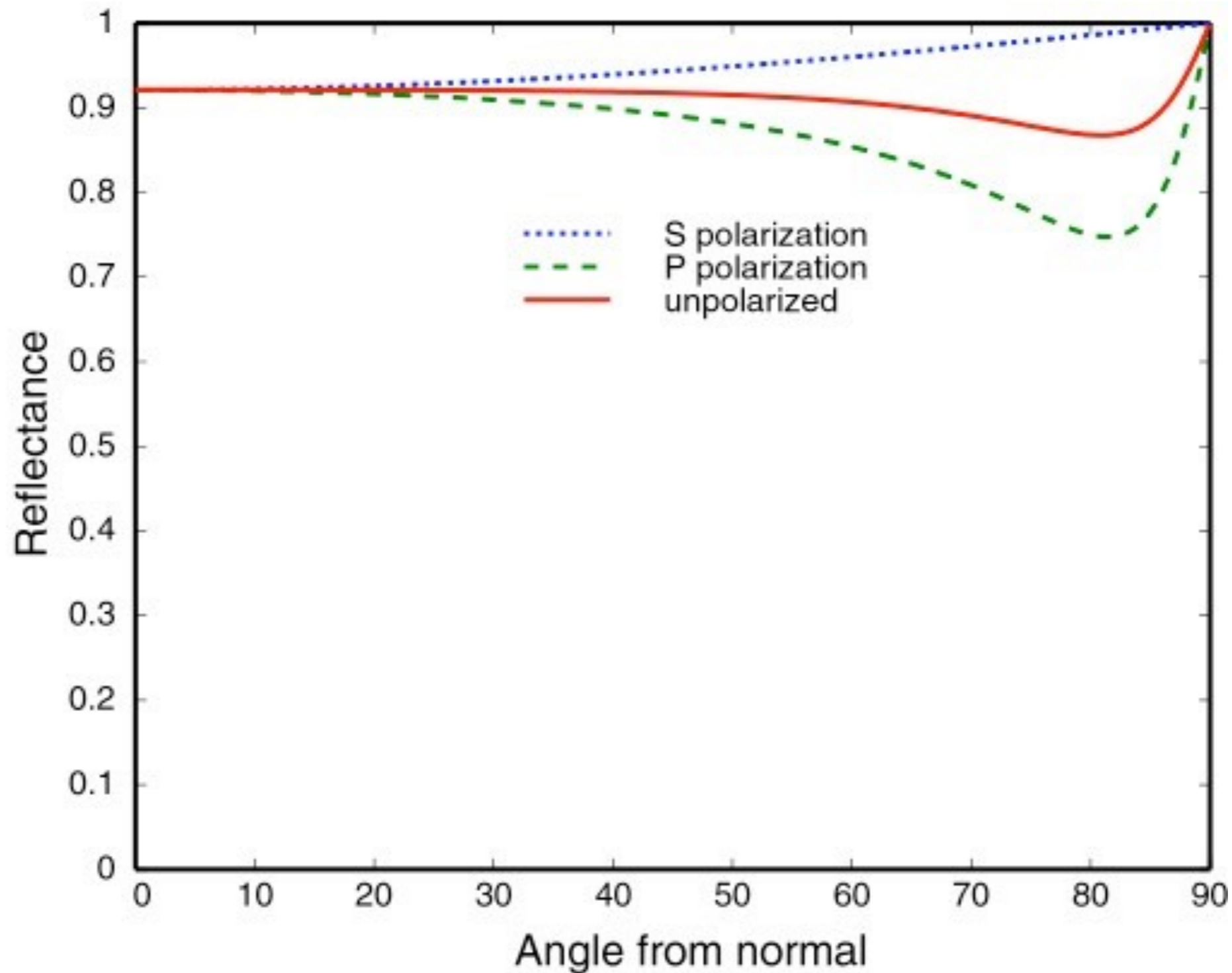
This example: reflectance increases with grazing angle

[Lafortune et al. 1997]

Fresnel Term (Dielectric, $\eta=1.5$)



Fresnel Term (Conductor)



Fresnel Term — Formulae

Accurate: need to consider polarization

$$R_s = \left| \frac{n_1 \cos \theta_i - n_2 \cos \theta_t}{n_1 \cos \theta_i + n_2 \cos \theta_t} \right|^2 = \left| \frac{n_1 \cos \theta_i - n_2 \sqrt{1 - \left(\frac{n_1}{n_2} \sin \theta_i\right)^2}}{n_1 \cos \theta_i + n_2 \sqrt{1 - \left(\frac{n_1}{n_2} \sin \theta_i\right)^2}} \right|^2,$$
$$R_p = \left| \frac{n_1 \cos \theta_t - n_2 \cos \theta_i}{n_1 \cos \theta_t + n_2 \cos \theta_i} \right|^2 = \left| \frac{n_1 \sqrt{1 - \left(\frac{n_1}{n_2} \sin \theta_i\right)^2} - n_2 \cos \theta_i}{n_1 \sqrt{1 - \left(\frac{n_1}{n_2} \sin \theta_i\right)^2} + n_2 \cos \theta_i} \right|^2.$$

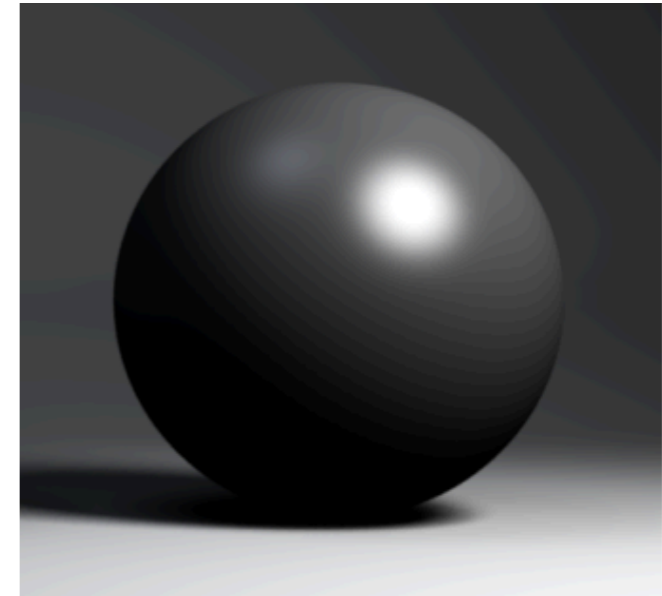
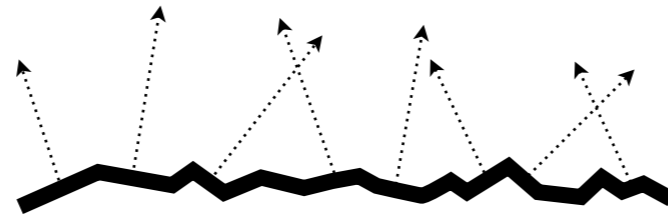
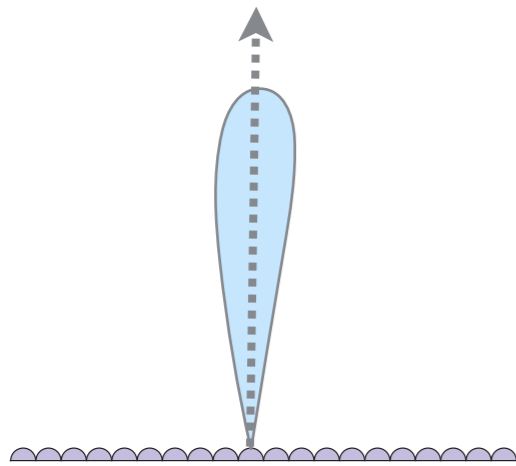
$$R_{\text{eff}} = \frac{1}{2} (R_s + R_p).$$

Approximate: Schlick's approximation

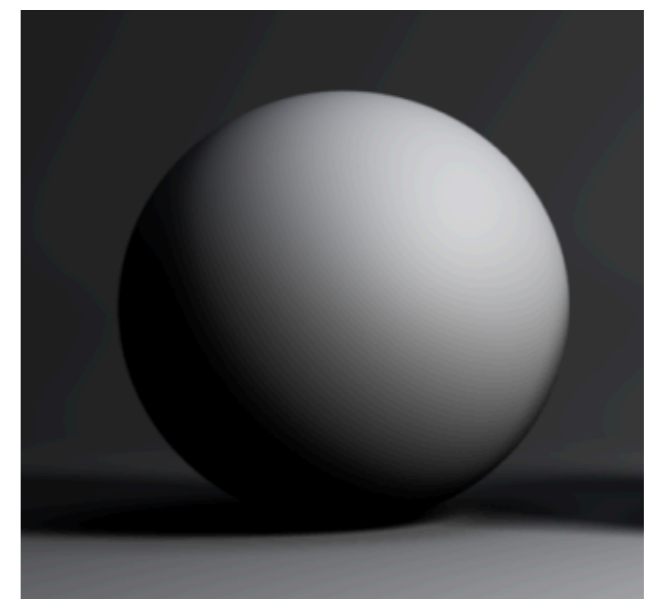
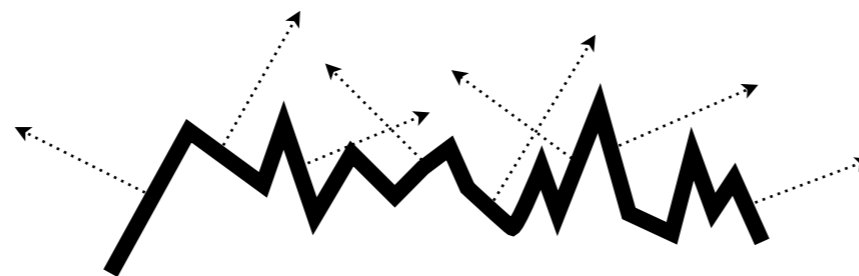
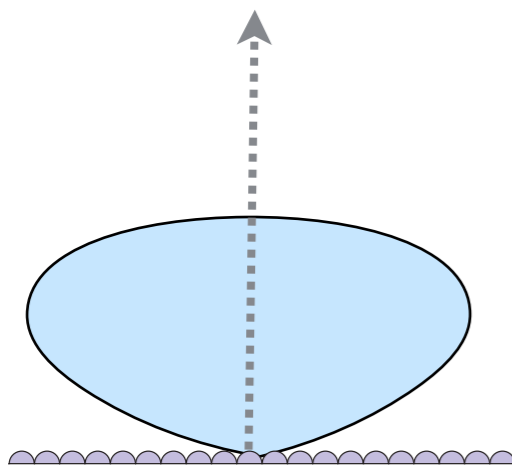
$$R(\theta) = R_0 + (1 - R_0)(1 - \cos \theta)^5$$
$$R_0 = \left(\frac{n_1 - n_2}{n_1 + n_2} \right)^2$$

Normal Distribution Function (NDF)

- Key: the **distribution** of microfacets' normals
 - Concentrated \iff glossy

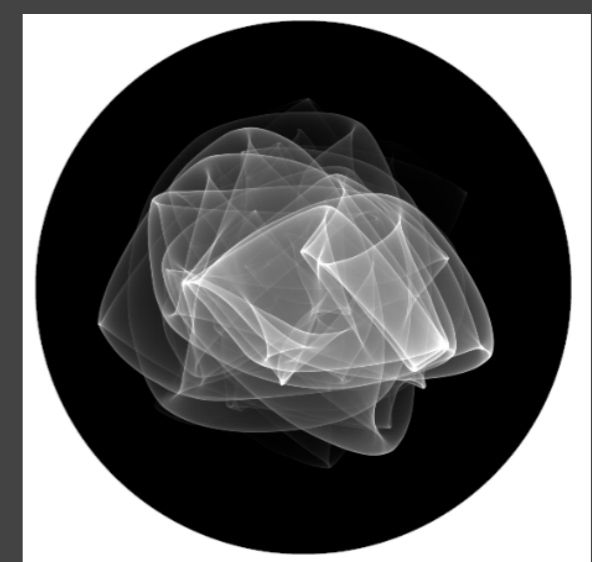
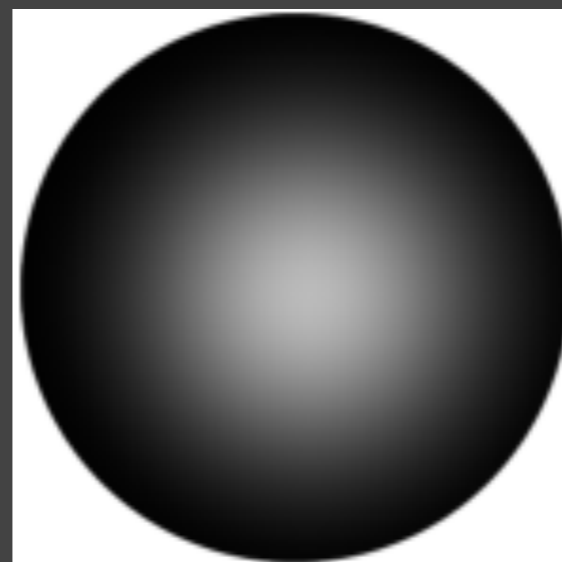
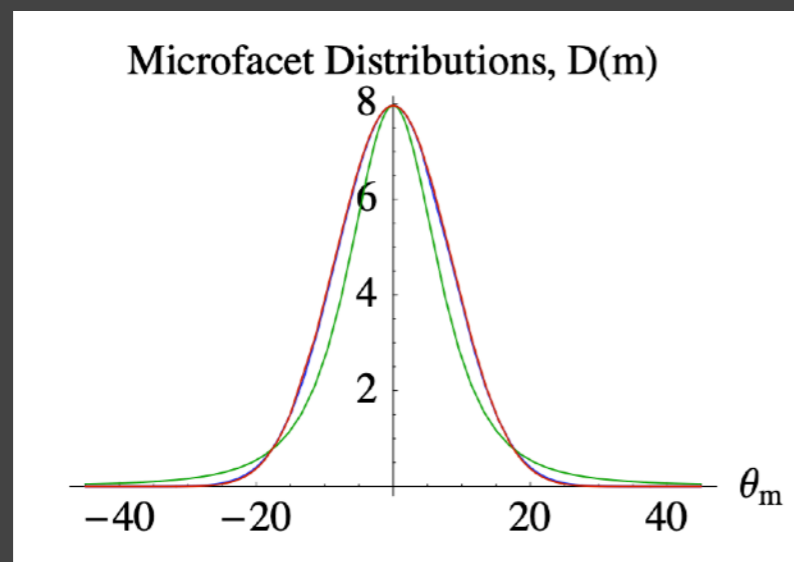


- Spread \iff diffuse



Normal Distribution Function (NDF)

- The Normal Distribution Function (NDF)
 - Note: has nothing to do with the normal distribution in stats
 - Various models to describe it
 - Beckmann, GGX, etc.
 - Detailed models [Yan 2014, 2016, 2018, ...]



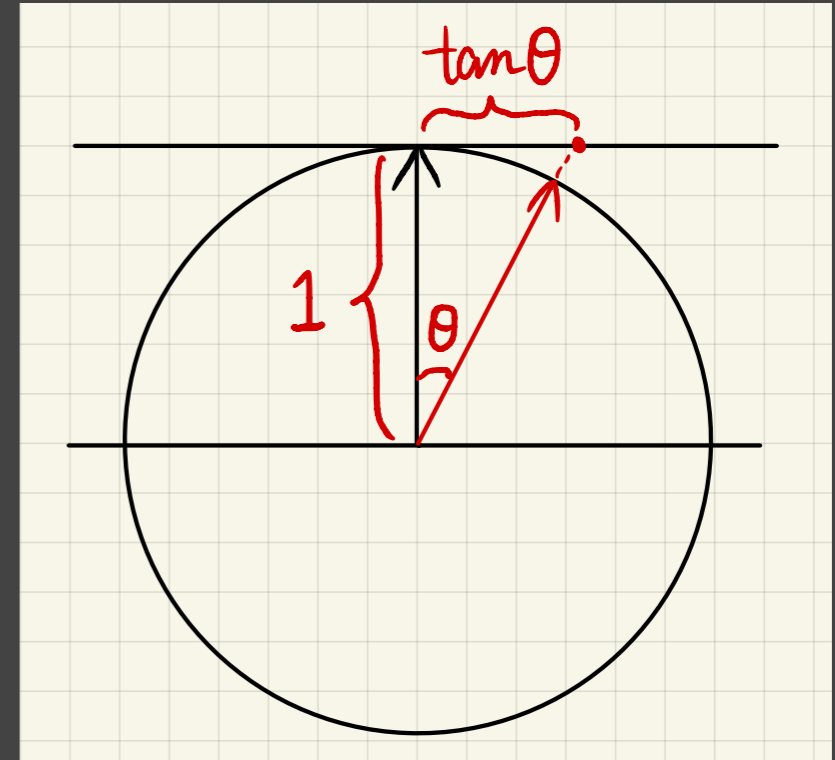
Normal Distribution Function (NDF)

- Beckmann NDF
 - Similar to a Gaussian
 - But defined on the **slope space**

$$D(h) = \frac{e^{-\frac{\tan^2 \theta_h}{\alpha^2}}}{\pi \alpha^2 \cos^4 \theta_h}$$

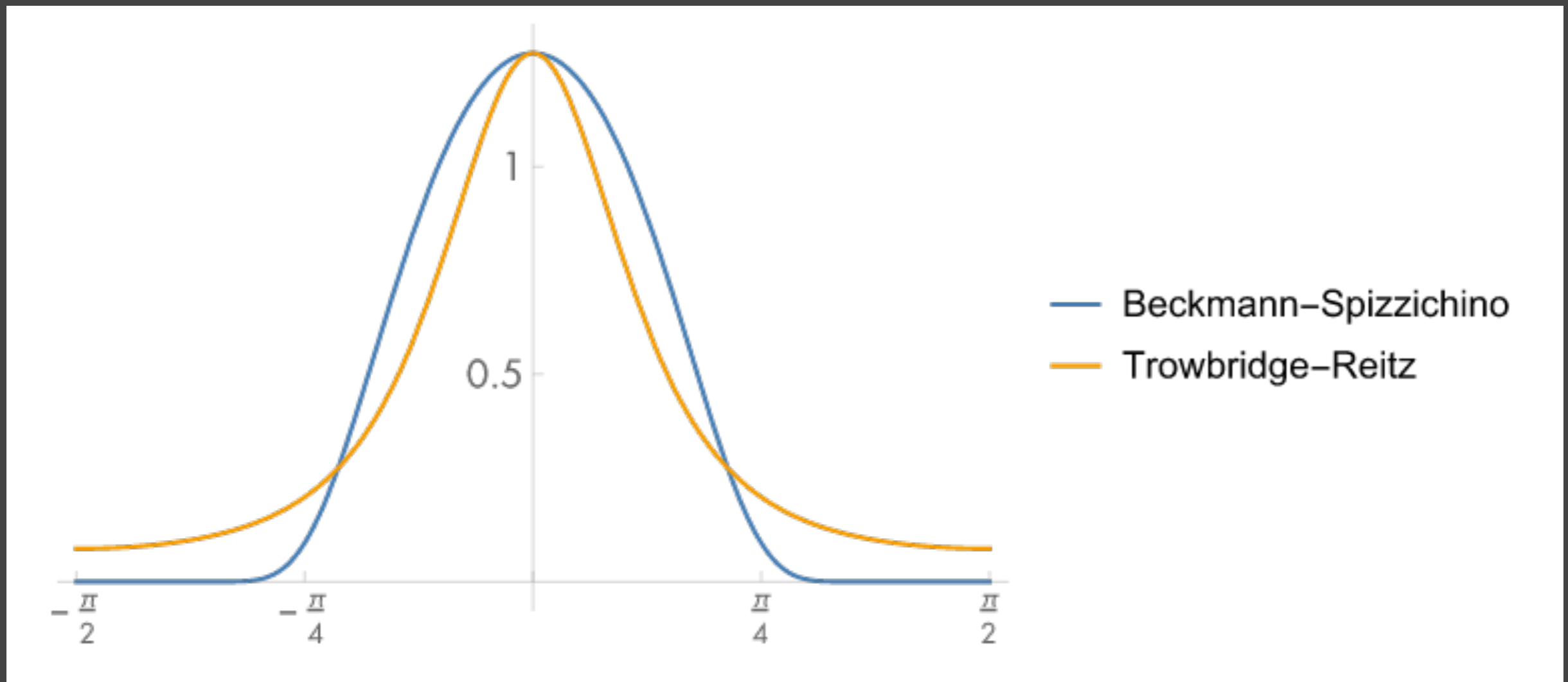
α : roughness of the surface (the smaller, the more like mirror/specular)

θ_h : angle between half vector h and normal n



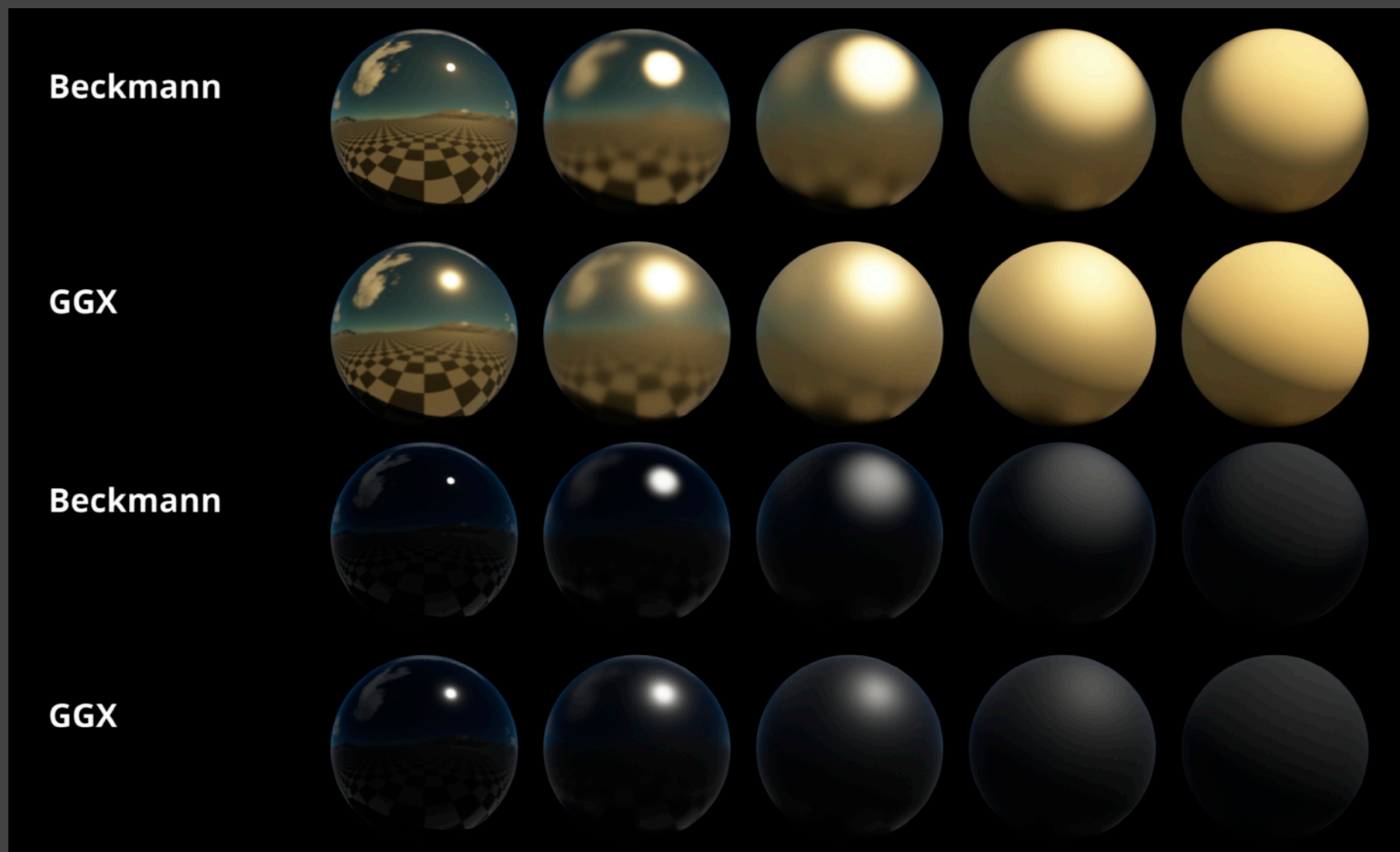
Normal Distribution Function (NDF)

- GGX (or Trowbridge-Reitz) [Walter et al. 2007]
 - Typical characteristic: **long tail!**



Normal Distribution Function (NDF)

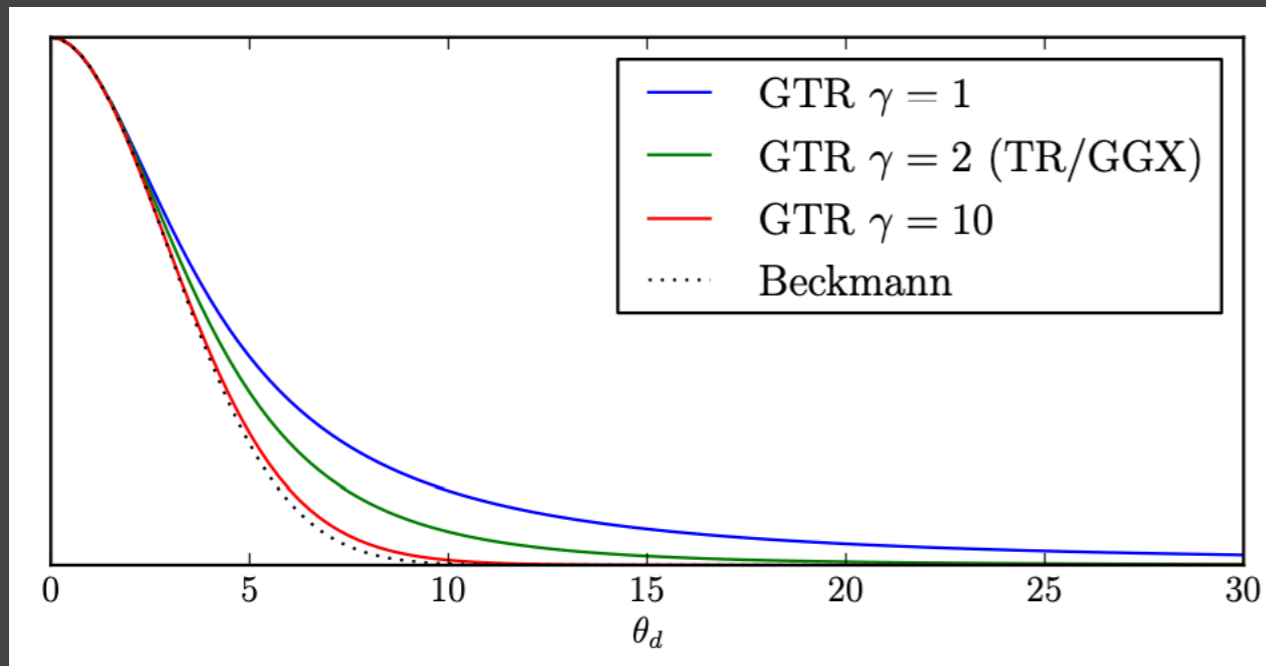
- Comparison: Beckmann vs. GGX



<https://planetside.co.uk/news/terrigen-4-5-release/>

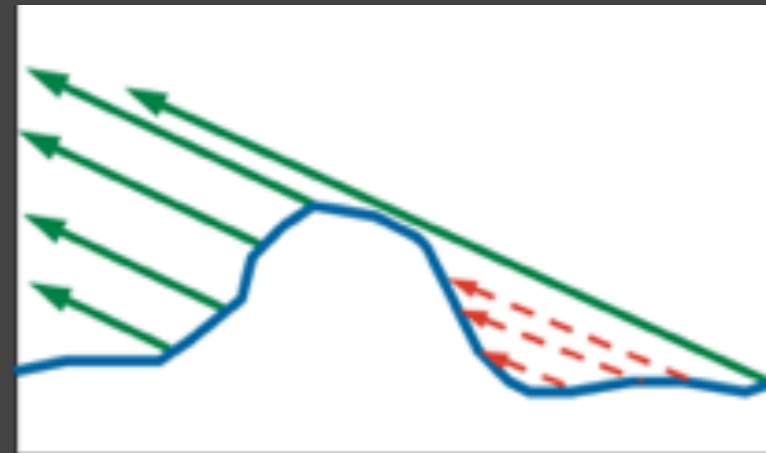
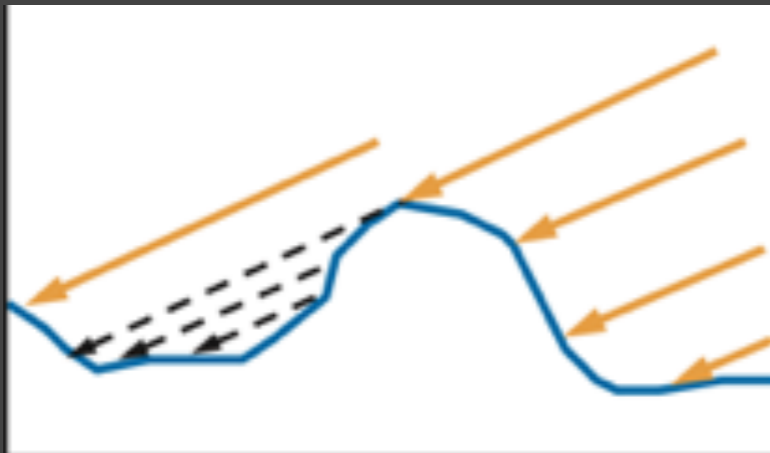
Normal Distribution Function (NDF)

- Extending GGX [by Brent Burley from WDAS]
 - GTR (Generalized Trowbridge-Reitz)
 - Even longer tails



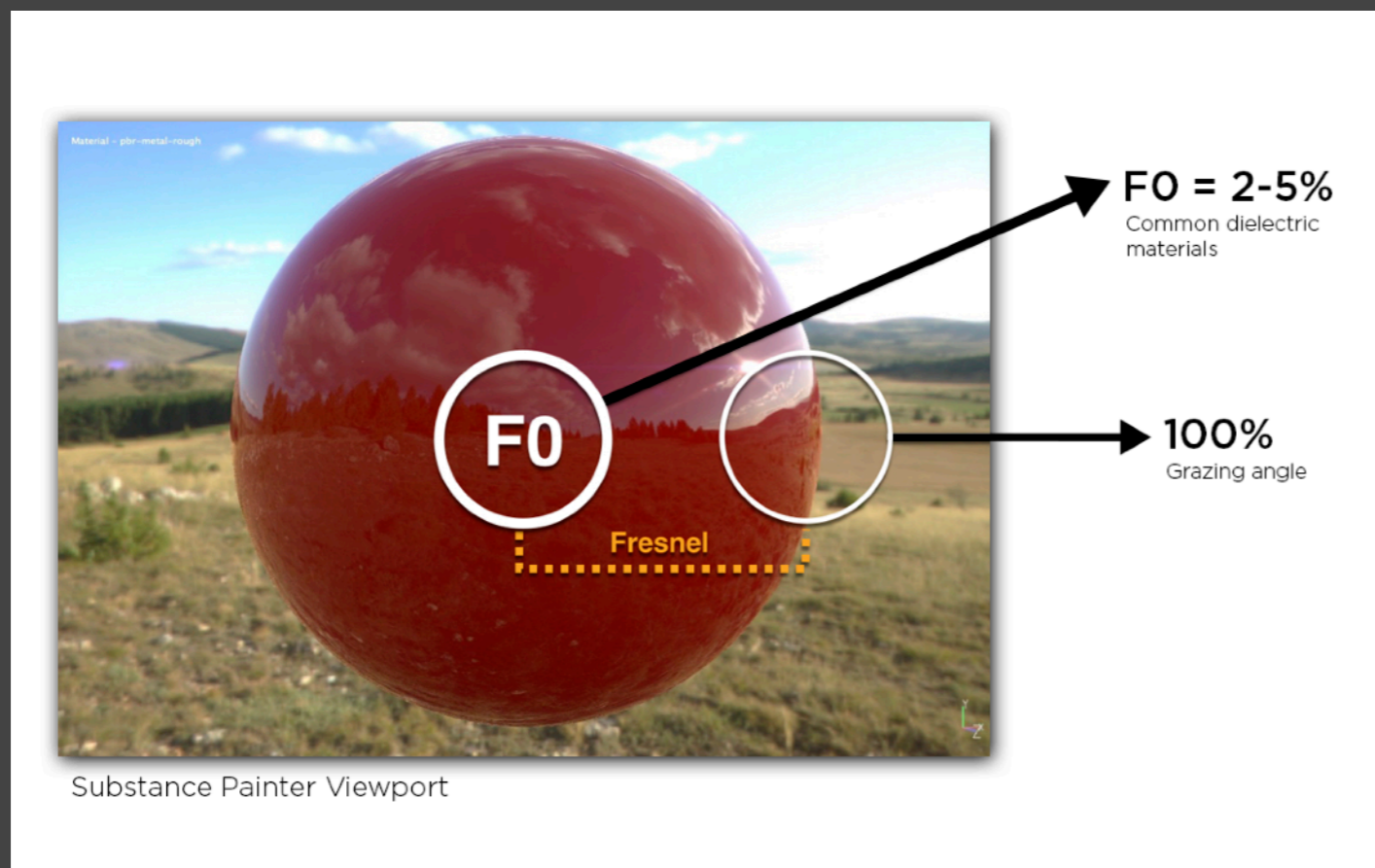
Shadowing-Masking Term

- Or, the geometry term G
$$f(i, o) = \frac{F(i, h)G(i, o, h)D(h)}{4(n, i)(n, o)}$$
 - Account for self-occlusion of microfacets
 - Shadowing — light, masking — eye
 - Provide darkening esp. around grazing angles



Shadowing-Masking Term

- Why is it important?
 - Suppose no G term, what will happen when the incident / outgoing is from grazing angle?



$$f(i, o) = \frac{F(i, h)G(i, o, h)D(h)}{4(n, i)(n, o)}$$

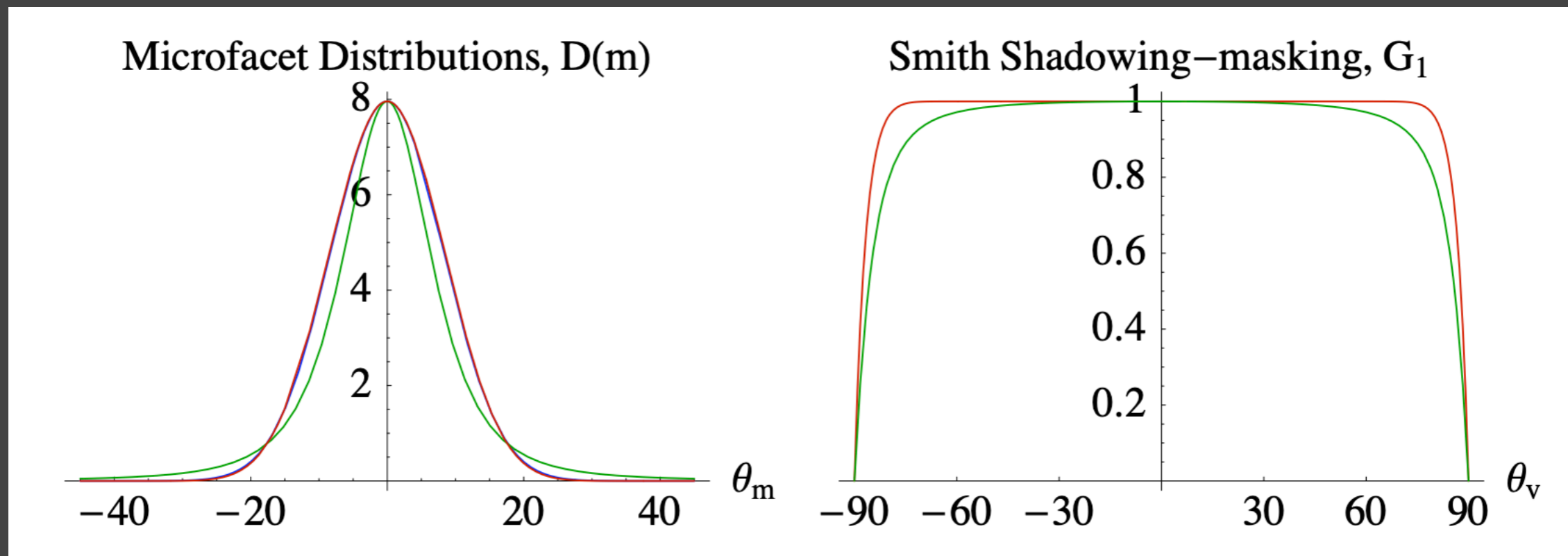


Can be arbitrarily bright around grazing angles!

Shadowing-Masking Term

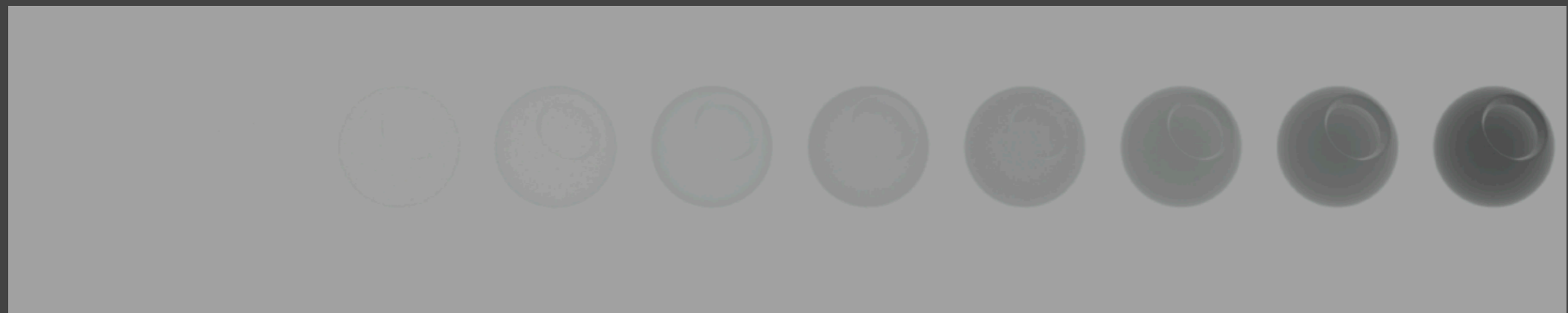
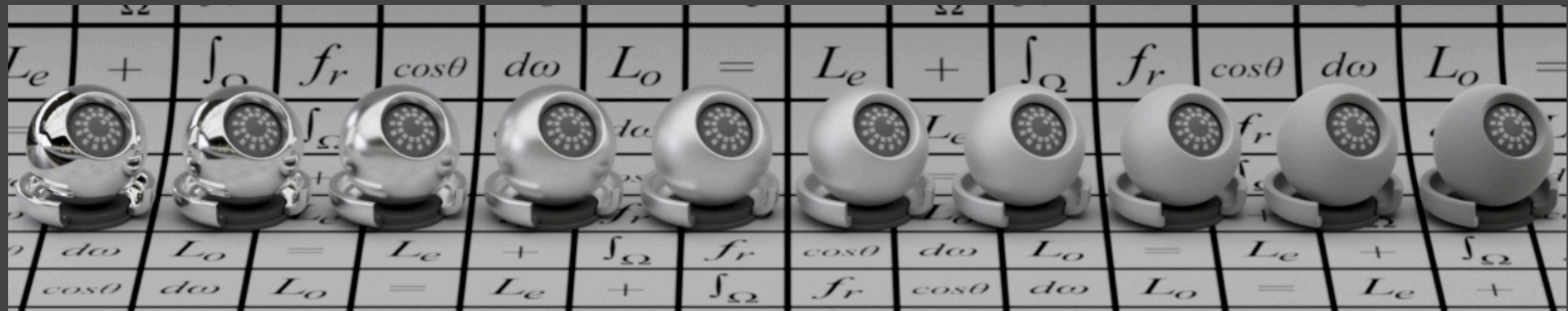
- A commonly used shadowing-masking term
 - The Smith shadowing-masking term
 - Decoupling shadowing and masking

$$G(\mathbf{i}, \mathbf{o}, \mathbf{m}) \approx G_1(\mathbf{i}, \mathbf{m})G_1(\mathbf{o}, \mathbf{m})$$



Multiple Bounces

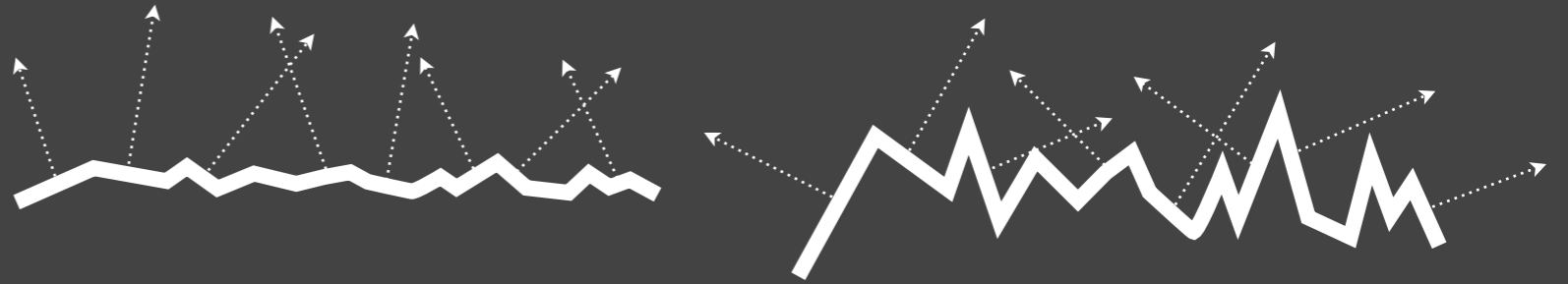
- Missing energy!
 - Especially prominent when roughness is high (why?)



https://fpsunflower.github.io/ckulla/data/s2017_pbs_imageworks_slides_v2.pdf

Multiple Bounces

- Missing energy!



- Adding back the missing energy?
 - Accurate methods exist [Heitz et al. 2016]
 - But can be too slow for RTR
- Basic idea
 - Being occluded == next bounce happening

The Kulla-Conty Approximation

- What's the overall energy of an outgoing 2D BRDF lobe?

$$E(\mu_o) = \int_0^{2\pi} \int_0^1 f(\mu_o, \mu_i, \phi) \mu_i d\mu_i d\phi$$

Note: $\mu = \sin \theta$

- Key idea
 - We can design an additional lobe that integrates to $1 - E(\mu_o)$
 - The outgoing BRDF lobe can be different for different incident dir.
 - Consider reciprocity, it should be* of the form $c(1 - E(\mu_i))(1 - E(\mu_o))$

The Kulla-Conty Approximation

- Therefore,

$$f_{\text{ms}}(\mu_o, \mu_i) = \frac{(1 - E(\mu_o))(1 - E(\mu_i))}{\pi(1 - E_{\text{avg}})}, E_{\text{avg}} = 2 \int_0^1 E(\mu) \mu d\mu$$

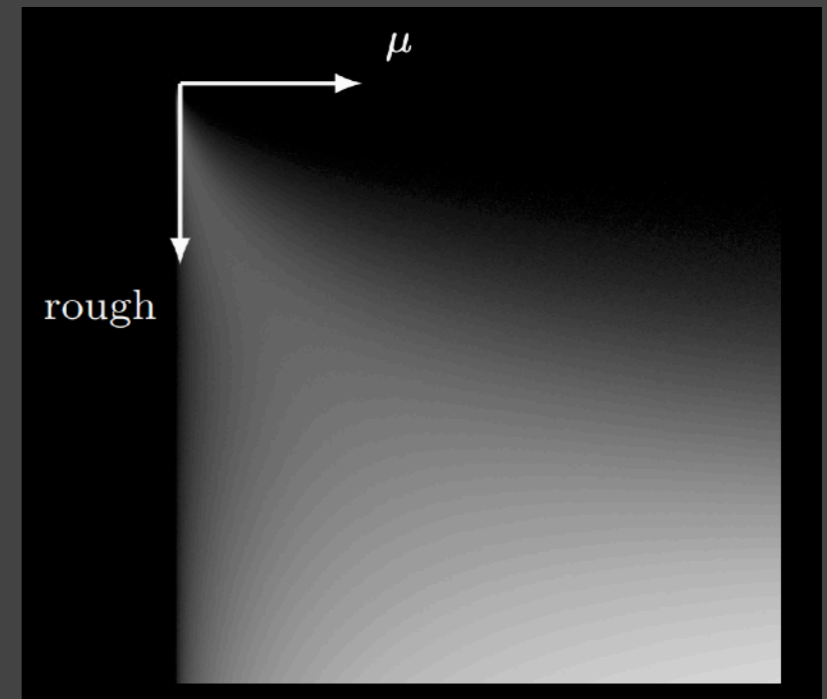
- FYI, validation:

$$\begin{aligned} E_{\text{ms}}(\mu_o) &= \int_0^{2\pi} \int_0^1 f_{\text{ms}}(\mu_o, \mu_i, \phi) \mu_i d\mu_i d\phi \\ &= 2\pi \int_0^1 \frac{(1 - E(\mu_o))(1 - E(\mu_i))}{\pi(1 - E_{\text{avg}})} \mu_i d\mu_i \\ &= 2 \frac{1 - E(\mu_o)}{1 - E_{\text{avg}}} \int_0^1 (1 - E(\mu_i)) \mu_i d\mu_i \\ &= \frac{1 - E(\mu_o)}{1 - E_{\text{avg}}} (1 - E_{\text{avg}}) \\ &= 1 - E(\mu_o) \end{aligned}$$

https://fpsunflower.github.io/ckulla/data/s2017_pbs_imageworks_slides_v2.pdf

The Kulla-Conty Approximation

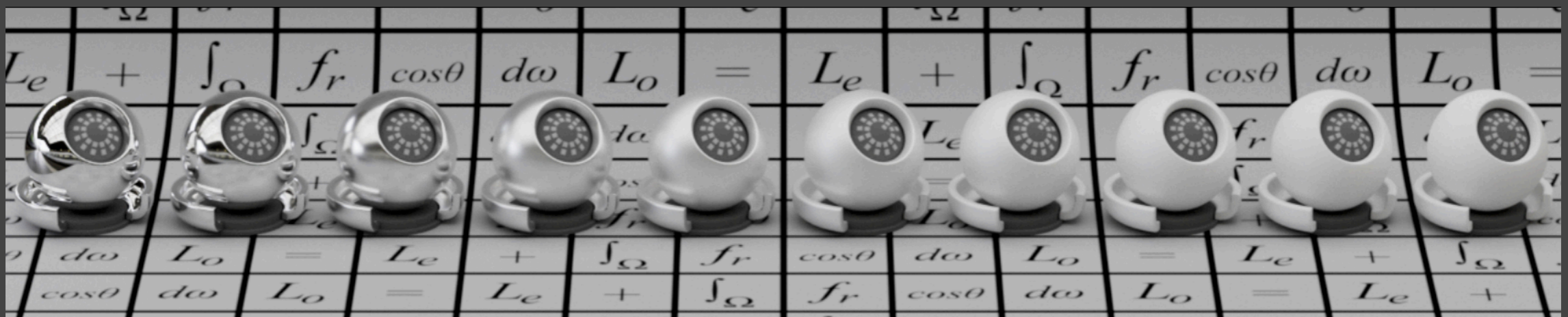
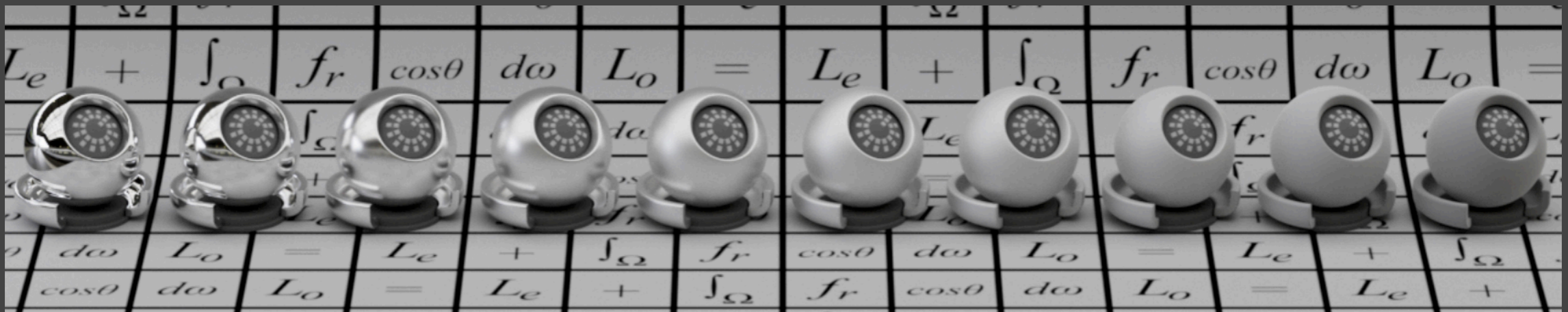
- But neither $E(\mu)$ nor $E_{avg} = 2 \int_0^1 E(\mu)\mu \, d\mu$ are analytic
- But we already know what to do!
 - Hint: in split sum, how do we deal with a difficult integral?
 - Precompute / tabulate!
- Dimension / parameters of $E(\mu)$ and E_{avg} ?
 - $E(\mu)$: roughness & μ [therefore, a 2D table]
 - E_{avg} : just roughness [therefore, a 1D table]



Precomputed table for $E(\mu)$

The Kulla-Conty Approximation

- Results



https://fpsunflower.github.io/ckulla/data/s2017_pbs_imageworks_slides_v2.pdf

The Kulla-Conty Approximation

- What if the BRDF has color?
 - Color == absorption == energy loss (as it should)
 - So we'll just need to compute the overall energy loss
- Define the average Fresnel (how much energy is reflected)

$$F_{avg} = \frac{\int_0^1 F(\mu) \mu \, d\mu}{\int_0^1 \mu \, d\mu} = 2 \int_0^1 F(\mu) \mu \, d\mu \quad \text{[Therefore, just a number]}$$

- And recall that E_{avg} is how much energy that you can see (i.e., will **NOT participate** in further bounces)

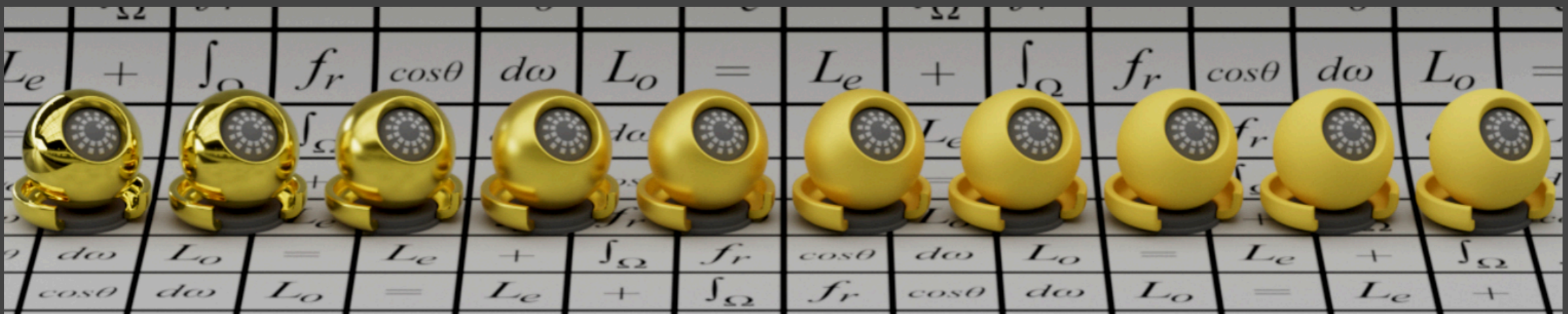
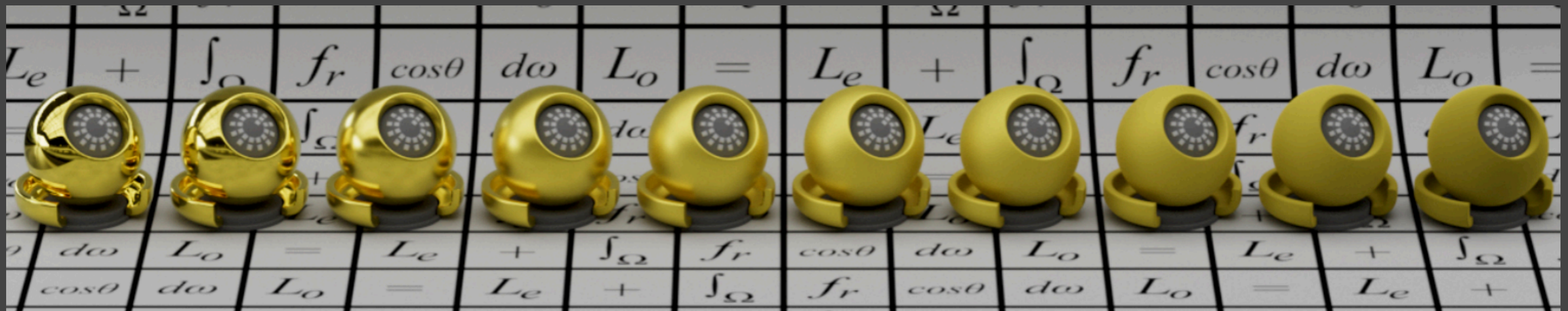
The Kulla-Conty Approximation

- Therefore, the proportion of energy (color) that
 - You can directly see: $F_{avg}E_{avg}$
 - After one bounce then be seen: $F_{avg}(1 - E_{avg}) \cdot F_{avg}E_{avg}$
 - ...
 - After k bounces then be seen: $F_{avg}^k(1 - E_{avg})^k \cdot F_{avg}E_{avg}$
- Adding everything up, we have the color term
 - Which will be directly multiplied on the **uncolored additional BRDF**

$$\frac{F_{avg}E_{avg}}{1 - F_{avg}(1 - E_{avg})}$$

The Kulla-Conty Approximation

- Results



https://fpsunflower.github.io/ckulla/data/s2017_pbs_imageworks_slides_v2.pdf

However, An Undesirable Hack

- Combining a Microfacet BRDF with a **diffuse** lobe
 - Pervasively used in computer vision for material recognition
 - COMPLETELY WRONG
 - COULDN'T BE WORSE
 - I NEVER TAUGHT YOU SO
- Issues
 - Physically incorrect
 - Not energy preserving
(fixed in Kulla-Conty)
(can also be fixed in other ways)



Questions?

Disney's Principled BRDF

Why is it needed?

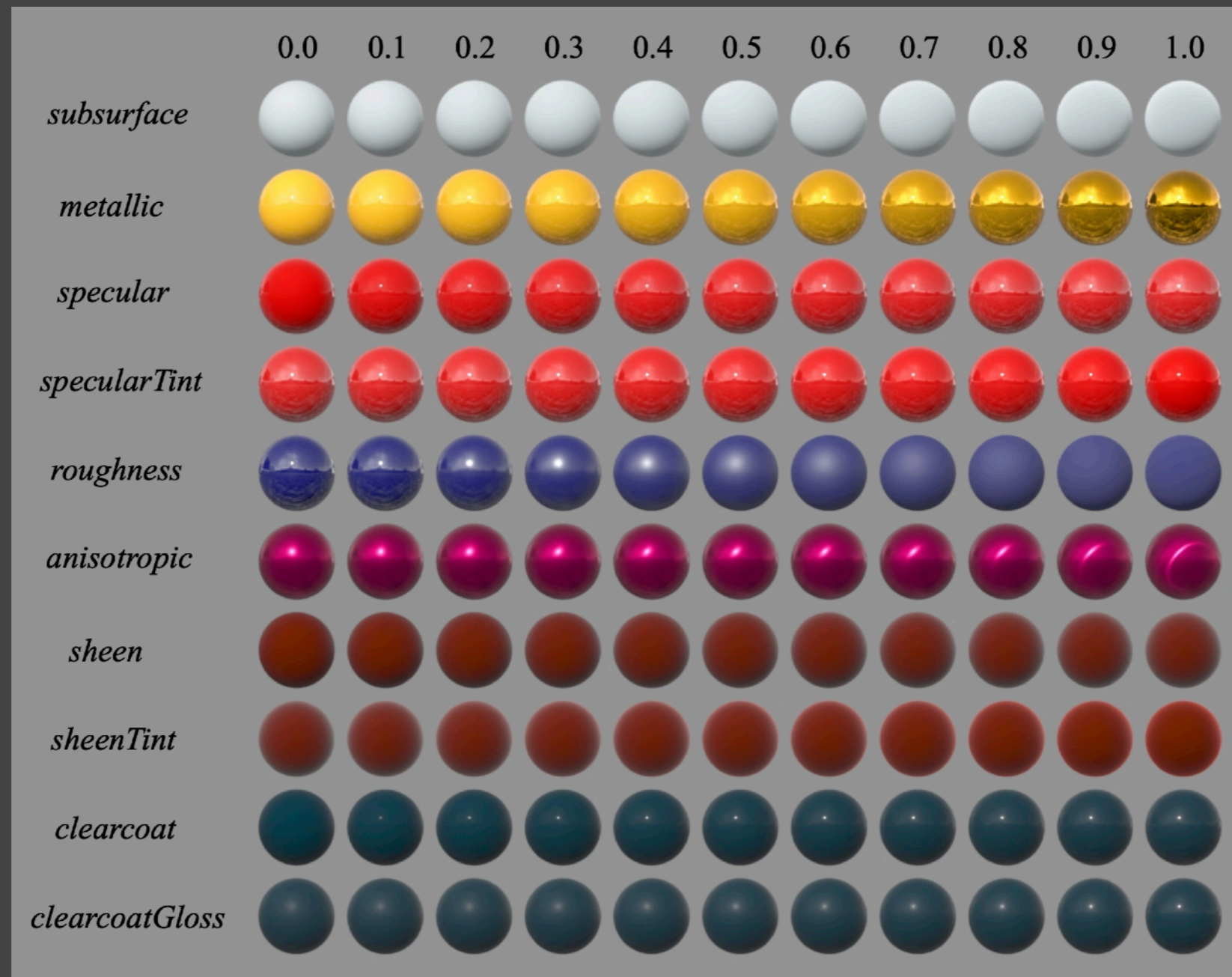
- Motivation
 - No physically-based materials are good at rep. all real materials
 - e.g. lacking diffuse term in most microfacet models
 - Physically-based materials are not artist friendly
 - e.g. “the complex index of refraction $n-ik$ ”
- High level design goal
 - Art directable, not necessarily physically correct
 - But again, referred to as PBR in real-time rendering...

What is “principled”?

- The BRDF is designed with a few important principles
 - Intuitive rather than physical parameters should be used.
 - There should be as few parameters as possible.
 - Parameters should be zero to one over their plausible range.
 - Parameters should be allowed to be pushed beyond their plausible range where it makes sense.
 - All combinations of parameters should be as robust and plausible as possible.

How does it work?

- A table showing the effects of **individual** parameters



Pros and Cons

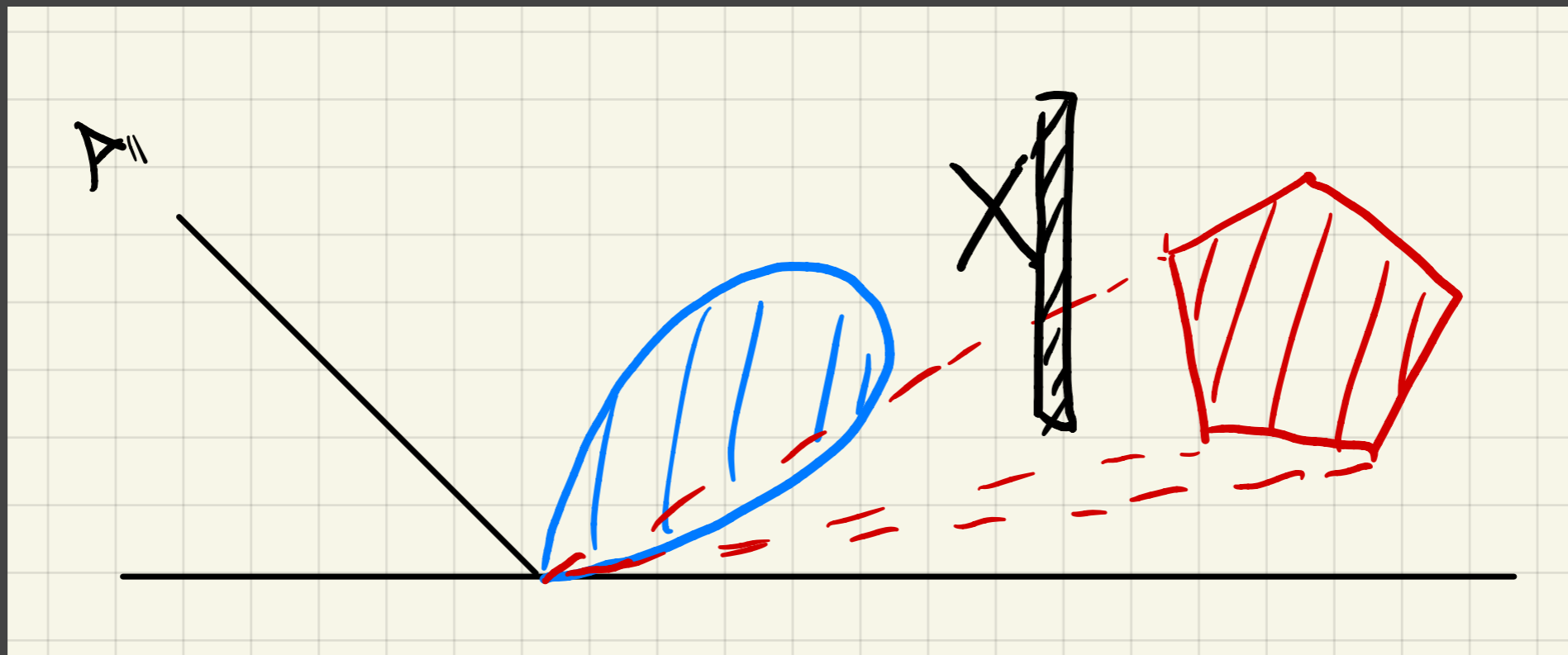
- Easy-to-understand / control
- A wide range of materials in a single model
- Open source implementation is available
- Not physically based
 - But is it a big problem?
 - Academia vs. industry
- Huge parameter space

Questions?

Shading Microfacet Models using Linearly Transformed Cosines (LTC)

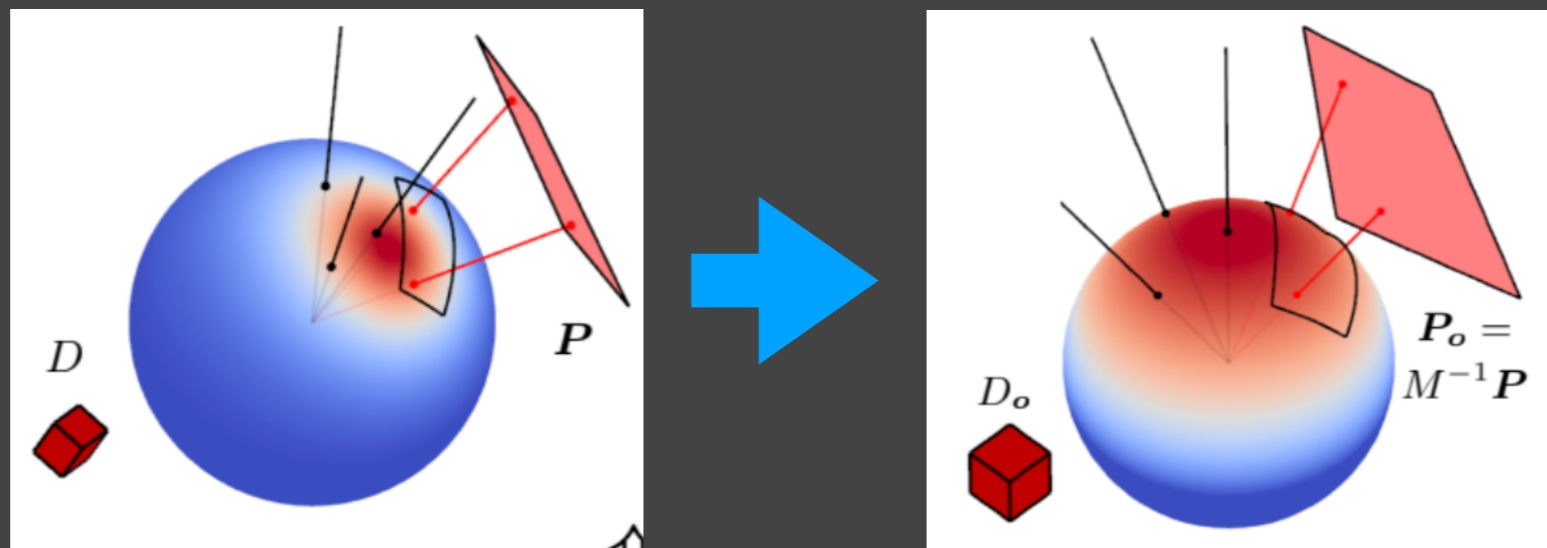
Linearly Transformed Cosines

- Solves the shading of microfacet models
 - Mainly on GGX, though others are also fine
 - No shadows
 - Under polygon shaped light



Linearly Transformed Cosines

- Key idea
 - Given the viewing direction, any outgoing 2D BRDF lobe can be transformed to a cosine
 - The shape of the light can also be transformed along
 - Integrating the transformed light on a cosine lobe can be **analytical**



Next Lecture

- More Real-Time Physically-Based Materials!



<https://www.wired.com/story/cloud-gaming-infrastructure-arms-race/>

Thank you!