



Searching a BST iteratively

- e.g., return pointer to node with "key" info:
- TreeNodePointer n = tree; /* aim at root */
 while (n != NULL && n->info != key)
 if (key < n->info) /* search left subtree */
 n = n->left;
 else /* search right subtree */
 n = n->right;
 return n; /* either NULL, or node with key info */
- Each iteration alignments half of severing and a
- Each iteration eliminates half of remaining nodes
 - So logarithmic complexity class
 - Similar result applies to many binary tree functions





Insert to a BST

- Same general strategy as find operation: if (info < current node) insert to left; else if (info > current node) insert to right; else - duplicate info - abort insert;
- Use either iterative or recursive approach
- 2 potential base cases for recursive version
 - Already in tree so return false; do not insert again
 - $-\,$ An empty tree where it should go $-\,$ so set parent link

Insertion order affects the tree?

- Try inserting these values *in this order*: 6, 4, 9, 3, 11, 7
- Now insert same values in this order: 3, 4, 6, 7, 9, 11
- Moral: sorted order is bad, random is good.
- Alternative is to set up self-balancing trees (see AVL trees in text)

Deleting a node (outline)

- All depends on how many children the node has
- No children: no problem just delete it (by setting appropriate parent link to NULL)
- One child: still easy just move that child "up" the tree (set parent link to that child)
- Two children: more difficult
- Basic strategy: replace node's *info* with (either) largest value in its left subtree (or smallest in right subtree) – can lead to 1 more delete



Inserting an item in a heap

Implementing a heap Convenient to implement as an array Root: [1]; root children: [2,3]; their children: [4:7] ... Works because of binary completeness requirement – tree is full at all depths except leaves e.g., insertHeap algorithm Step 1; put item at end of array;

- O(1) complexity, unless array is filled up
- Step 2 until done: reheapify by array indexing;
 Have parent of array[i] at array[i/2], ∀ i>1
 - Have parent of array[1] at array[1/2], v
 O(log n) complexity to reheapify this way
- So complexity of insertHeap is O(log n) overall