# **Learning Ensembles**

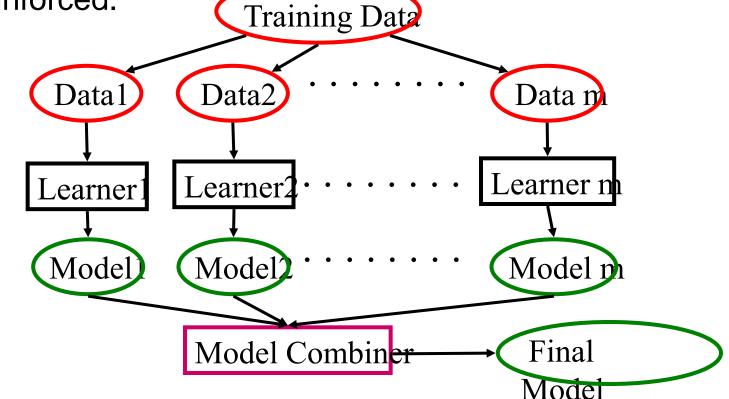
290N UCSB, 2015

#### **Outlines**

- Learning Assembles
- Random Forest
- Adaboost

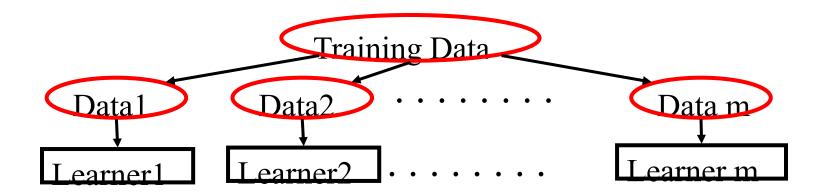
# **Learning Ensembles**

- Learn multiple classifiers separately
- Combine decisions (e.g. using weighted voting)
- When combing multiple decisions, random errors cancel each other out, correct decisions are reinforced.



# **Homogenous Ensembles**

- Use a single, arbitrary learning algorithm but manipulate training data to make it learn multiple models.
  - Data1 ≠ Data2 ≠ ... ≠ Data m
  - Learner1 = Learner2 = ... = Learner m
- Methods for changing training data:
  - Bagging: Resample training data
  - Boosting: Reweight training data
  - DECORATE: Add additional artificial training data





- Create ensembles by repeatedly randomly resampling the training data (Brieman, 1996).
- Given a training set of size *n*, create *m* sample sets
  - Each *bootstrap sample set* will on average contain 63.2% of the unique training examples, the rest are replicates.
- Combine the *m* resulting models using majority vote.
- Decreases error by decreasing the variance in the results due to *unstable learners*, algorithms (like decision trees) whose output can change dramatically when the training data is slightly changed.

## **Random Forests**

- Introduce two sources of randomness: "Bagging" and "Random input vectors"
  - Each tree is grown using a bootstrap sample of training data
  - At each node, best split is chosen from random sample of *m* variables instead of all variables M.
- m is held constant during the forest growing
- Each tree is grown to the largest extent possible
- Bagging using decision trees is a special case of random forests when m=M

#### **Random Forests**

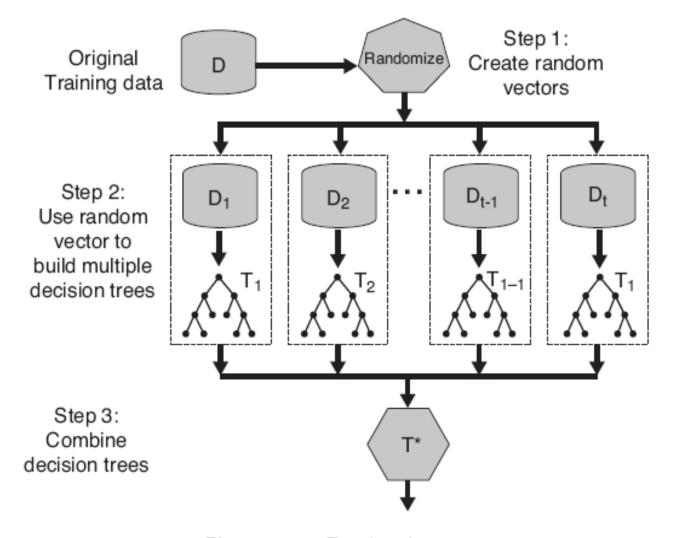


Figure 5.40. Random forests.

# **Random Forest Algorithm**

- Good accuracy without over-fitting
- Fast algorithm (can be faster than growing/pruning a single tree); easily parallelized
- Handle high dimensional data without much problem

# **Boosting: AdaBoost**

Yoav Freund and Robert E. Schapire. A decisiontheoretic generalization of on-line

#### learning and an application to boosting. Journal of Computer and System Sciences,

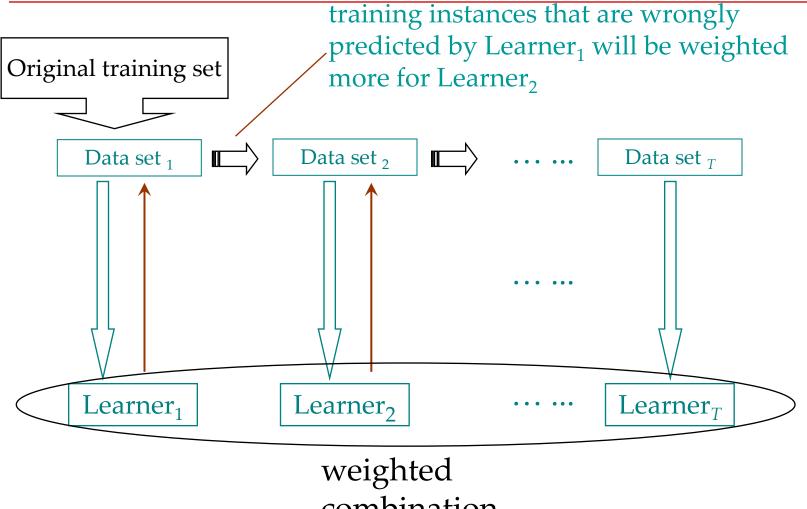
55(1):119–139, August 1997.

Simple with theoretical foundation

# **Adaboost - Adaptive Boosting**

- Use training set re-weighting
  - Each training sample uses a weight to determine the probability of being selected for a training set.
- AdaBoost is an algorithm for constructing a "strong" classifier as linear combination of "simple" "weak" classifier T  $f(x) = \sum_{t=1}^{T} \alpha_t h_t(x)$
- Final classification based on weighted sum of weak classifiers

# AdaBoost: An Easy Flow

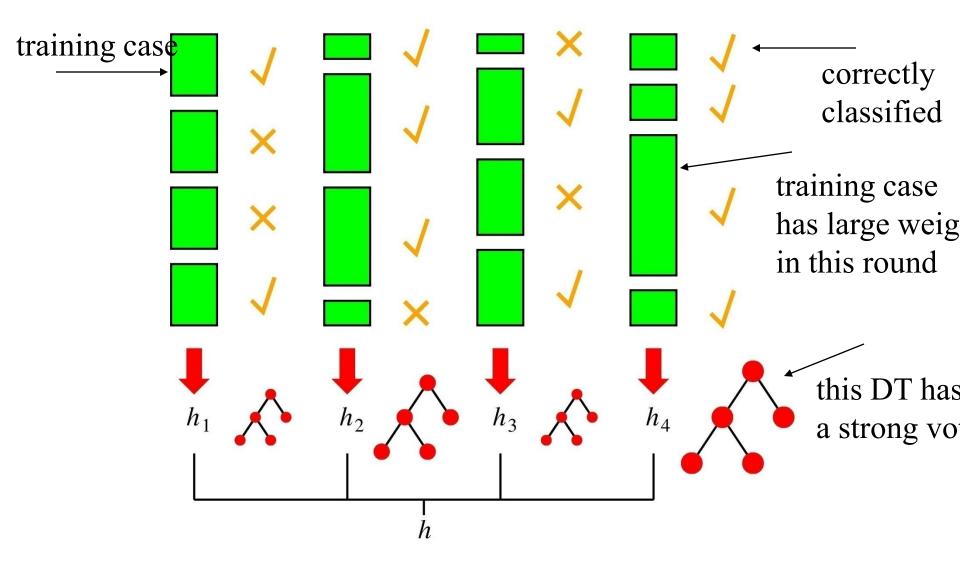


combination

# **Adaboost Terminology**

- $h_t(x)$ ... "weak" or basis classifier
- $H(x) = sign(f(x)) \dots$  "strong" or final classifier
- Weak Classifier: < 50% error over any distribution
- Strong Classifier: thresholded linear combination of weak classifier outputs

#### And in a Picture

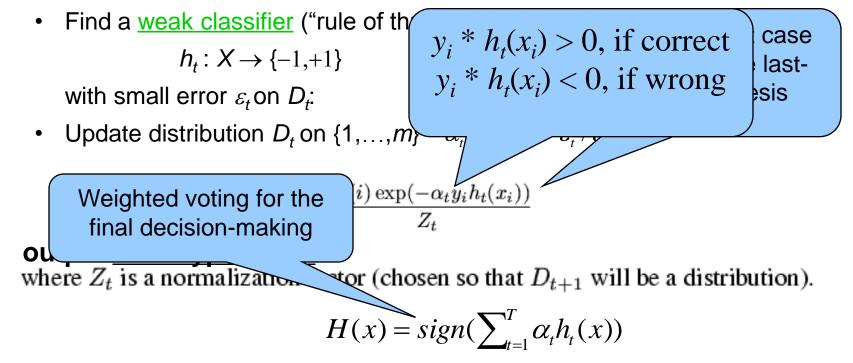


# AdaBoost.M1

- Given <u>training set</u> X={(x<sub>1</sub>,y<sub>1</sub>),
- *y<sub>i</sub>*∈{-1,+1} correct label
- Initialize distribution D<sub>1</sub>(i)=1/m;
- for t = 1, ..., T:

Each training sample has a weight, which determines the probability of being selected for training the component classifier

(weight of training cases)



# Reweighting

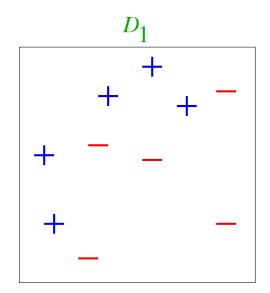
#### Effect on the training set

Reweighting formula:

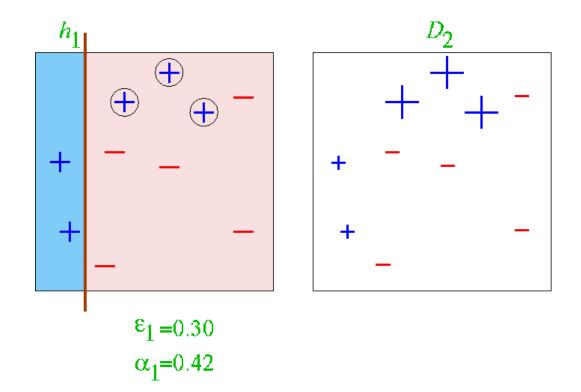
$$\begin{split} D_{t+1}(i) &= \frac{D_t(i)exp(-\alpha_t y_i h_t(x_i))}{Z_t} \\ &= exp(-\alpha_t y_i h_t(x_i)) \left\{ \begin{array}{cc} < 1, & y_i = h_t(x_i) \\ > 1, & y_i \neq h_t(x_i) \end{array} \right. \\ &= y_i \neq h_t(x_i) \\ &= y_i \neq h_t(x_i) \\ \end{array} \end{split}$$

⇒ Increase (decrease) weight of wrongly (correctly) classified examples



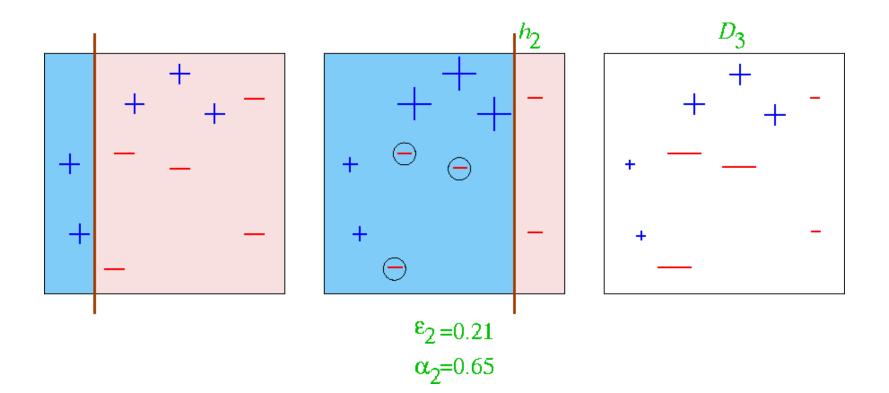






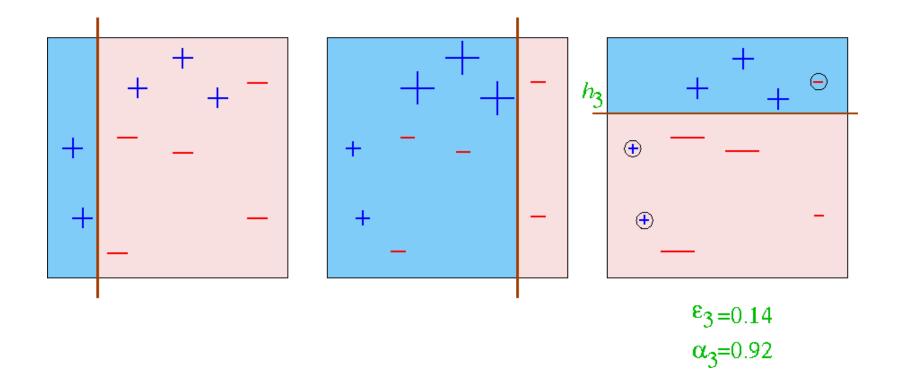
Weak classifier: if  $h_1 < 0.2 \rightarrow 1$  else -1





Weak classifier: if  $h_2 < 0.8 \rightarrow 1$  else -1





Weak classifier: if  $h_3 > 0.7 \rightarrow 1$  else -1

## **Final Combination**

+

if  $h_1 < 0.2 \rightarrow 1$  else -1 if  $h_2 < 0.8 \rightarrow 1$  else -1 = sign 0.42 H final + 0.65 + 0.92 if  $h_3 > 0.7 \rightarrow 1$  else -1 ++= +

# **Pros and cons of AdaBoost**

#### Advantages

- Very simple to implement
- Does feature selection resulting in relatively simple classifier
- Fairly good generalization

#### Disadvantages

- Suboptimal solution
- Sensitive to noisy data and outliers



- Duda, Hart, ect Pattern Classification
- Freund "An adaptive version of the boost by majority algorithm"
- Freund "Experiments with a new boosting algorithm"
- Freund, Schapire "A decision-theoretic generalization of on-line learning and an application to boosting"
- Friedman, Hastie, etc "Additive Logistic Regression: A Statistical View of Boosting"
- Jin, Liu, etc (CMU) "A New Boosting Algorithm Using Input-Dependent Regularizer"
- Li, Zhang, etc "Floatboost Learning for Classification"
- Opitz, Maclin "Popular Ensemble Methods: An Empirical Study"
- Ratsch, Warmuth "Efficient Margin Maximization with Boosting"
- Schapire, Freund, etc "Boosting the Margin: A New Explanation for the Effectiveness of Voting Methods"
- Schapire, Singer "Improved Boosting Algorithms Using Confidence-Weighted Predictions"
- Schapire "The Boosting Approach to Machine Learning: An overview"
- Zhang, Li, etc "Multi-view Face Detection with Floatboost"

## **AdaBoost: Training Error Analysis**

• Suppose 
$$f(x) = \sum_{t=1}^{T} \frac{\text{Equivalent}}{\alpha_t h_t(x)} \quad H(x) = \operatorname{sign}(f(x))$$
  
if  $H(x_i) \neq y_i$  then  $y_i f(x_i) \leq 0$  implying that  $\exp(-y_i f(x_i)) \geq 1$ . Thus,  

$$\begin{bmatrix} H(x_i) \neq y_i \end{bmatrix} \leq \exp(-y_i f(x_i)).$$
  
• Therefore, training error is:  

$$\frac{1}{m} |\{i : H(x_i) \neq y_i\}| \leq \frac{1}{q} \quad \{i : H(x_i) \neq y_i\} \text{ is a vector which} \\ i \text{-th element is } [H(x_i) \neq y_i].$$
  
• As:  

$$D_{T+1}(i) = \frac{\exp(-\sum_t \alpha_t y_i)}{m \prod_t Z} \quad \{i : H(x_i) \neq y_i\} \text{ is the sum of all the} \\ \text{element in the vector} \\ \text{Finally:} \quad \sum_{\substack{t=1 \\ m \ t \in T}} D_{T+1}(i) = 1, \quad \frac{1}{m} \sum_{t=1}^{m} \sum_{t=1}^{T'_i \mathcal{T}(X_i)} = \prod_t Z_t$$

# AdaBoost: How to choose $\alpha_{\tau}$

