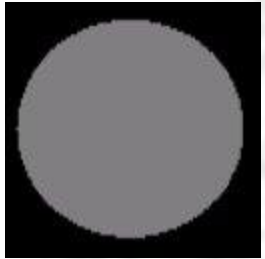
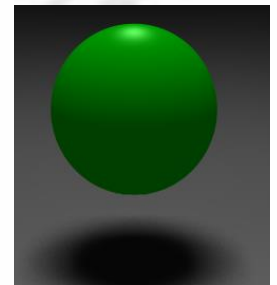
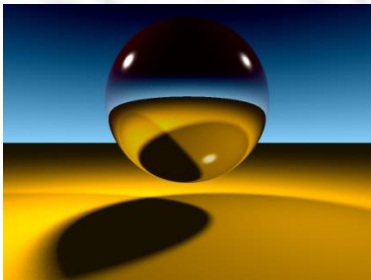
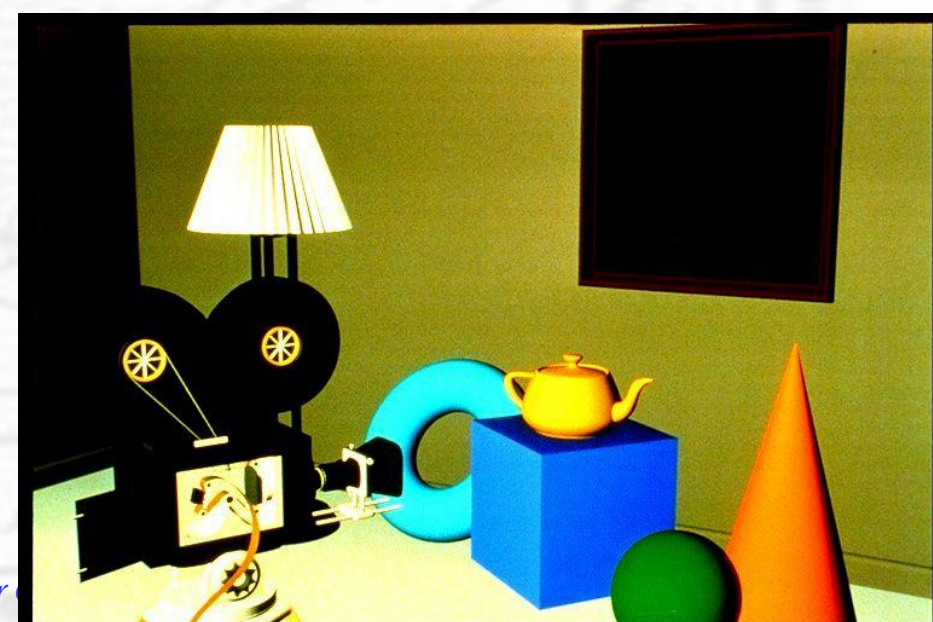
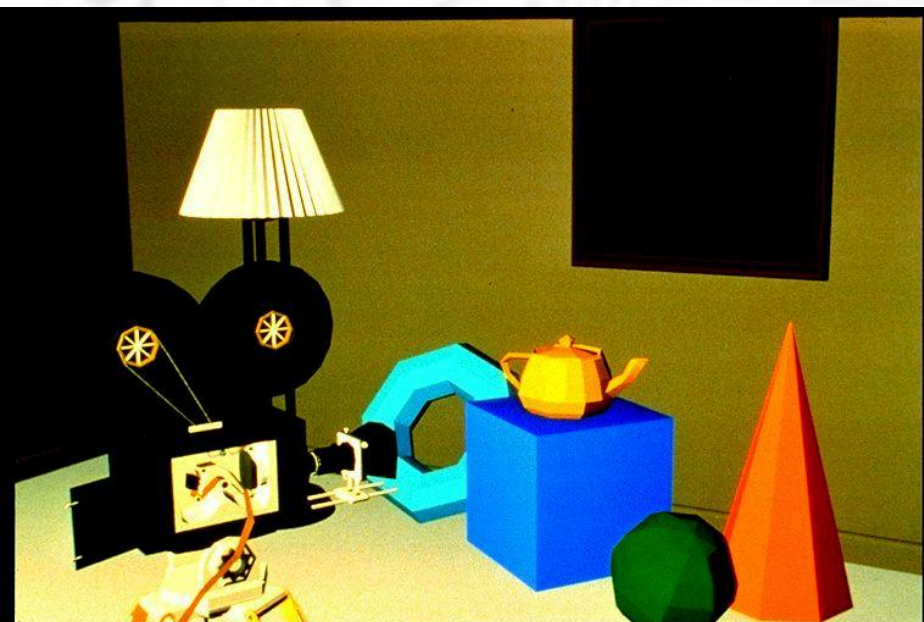
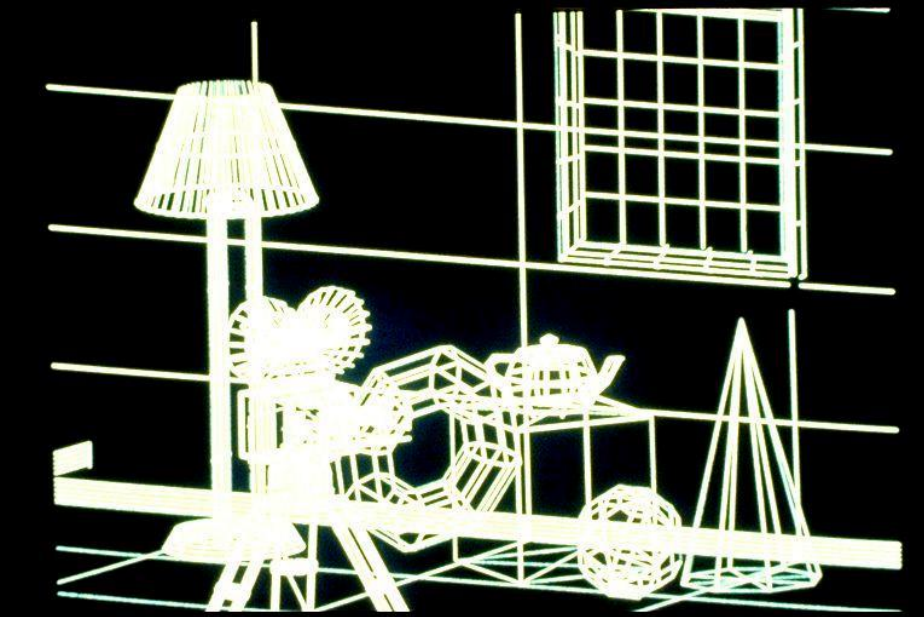


Progression in Visual Realism



FLAT SHADING











Christoph Hormann <chris_hormann@gmx.de>



Computer Graphics

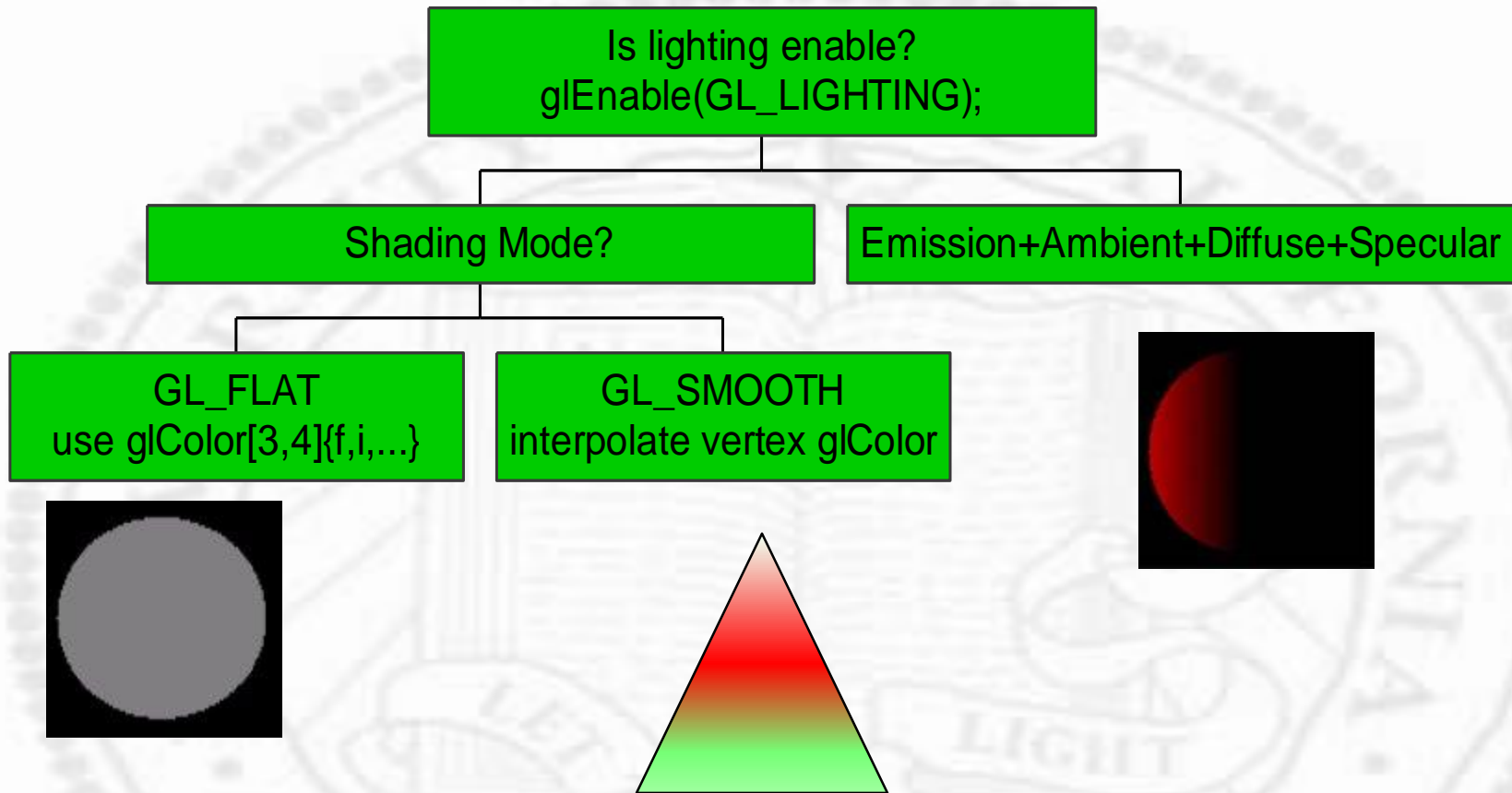
Many Things can Happen

- ❖ Hidden Surface Removal
- ❖ Flat color
- ❖ Single light
- ❖ Multiple lights
- ❖ High light
- ❖ Interpolated shading
- ❖ Texture mapping
- ❖ Shadow
- ❖ Ray tracing
- ❖ Radiosity

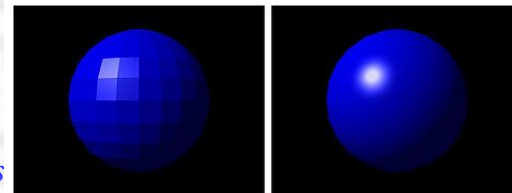
Homework #2 – Color Models

- ❖ R, G, B, (A)
- ❖ There are a lot more
 - ❑ CMY, YIQ, HSV, HLS, CIE
- ❖ Issues with half tone and dithering
 - ❑ Matching color and spatial resolution
 - ❑ For screen display and web delivery

Homework #2 – Shading Models



- ❖ Shading for smooth surfaces (Gouraud and Phong Shading)



Homework #2 –HLHS Removal

❖ Very simple, you need to do

❑ Prepare buffer

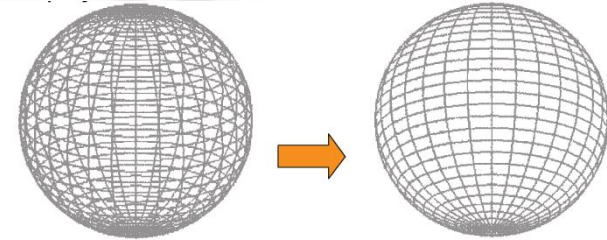
- `glutInitDisplay(GLUT_DEPTH | ...);`
 - *distance* to the view point is recorded
- `glClear(GL_DEPTH_BUFFER_BIT);`
 - clear to the far clipping plan distance (1.0)

❑ Enable depth comparison

- `glEnable(GL_DEPTH_TEST);`

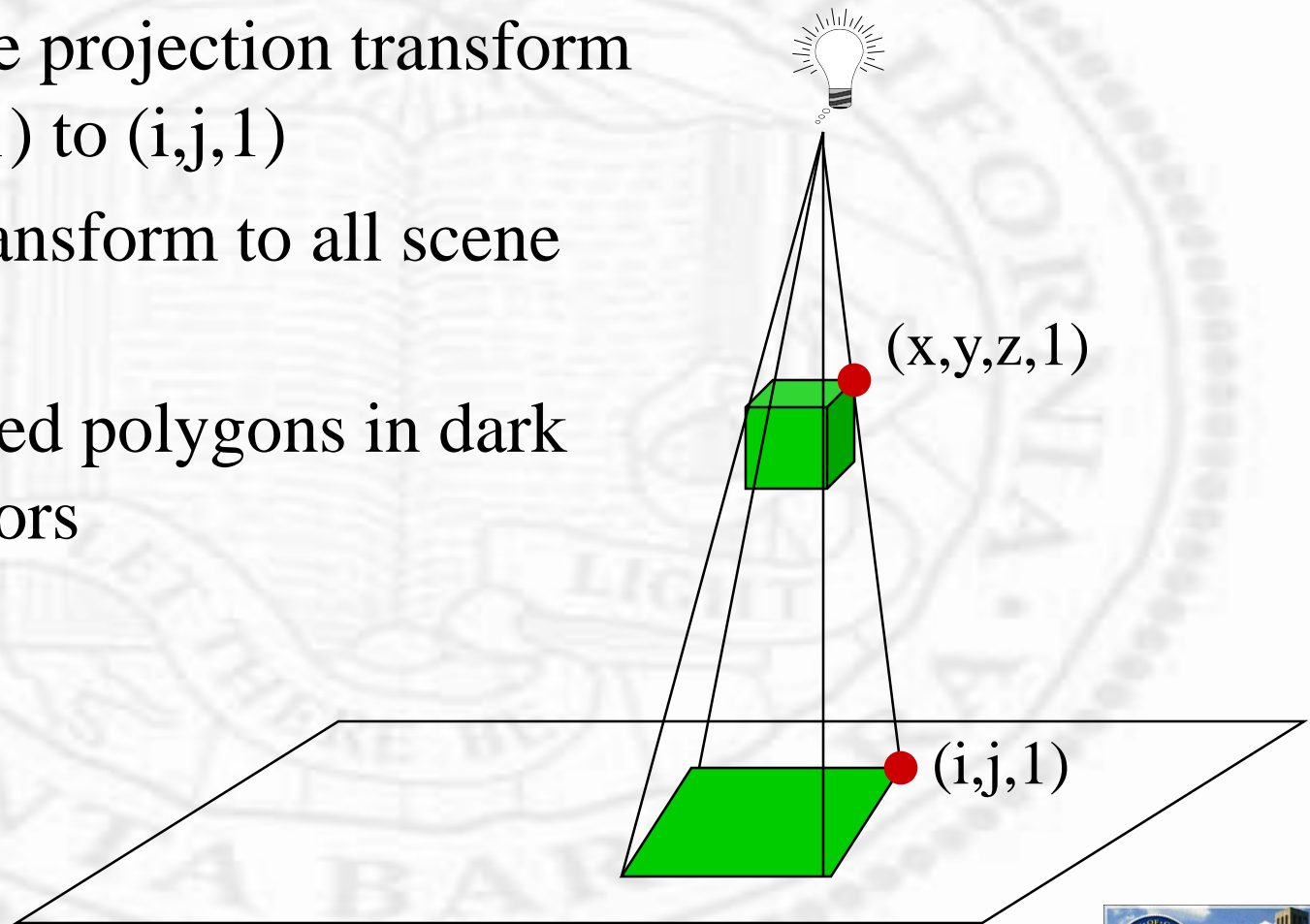
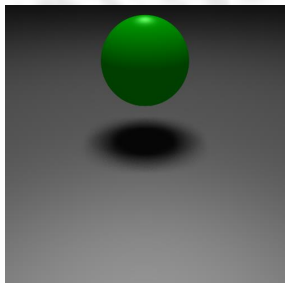
❑ Tell OpenGL how to do the depth comparison

- `glDepthFunc();` default is `GL_LESS` (in *front* of the far clipping plane)
- Visible *z* values are *negative*, but distance (depth) is *positive*



Homework #2 – (Fake) Shadow

- ❖ Figure out 3D coordinates (query OpenGL)
- ❖ Figure out the projection transform
From $(x,y,z,1)$ to $(i,j,1)$
- ❖ Apply this transform to all scene polygons
- ❖ Draw projected polygons in dark (shadow) colors



Math

$$\text{line} \quad \begin{cases} x = l_x + t(p_x - l_x) \\ y = l_y + t(p_y - l_y) \\ z = l_z + t(p_z - l_z) \end{cases}$$

$$\text{plane} \quad z = 0$$

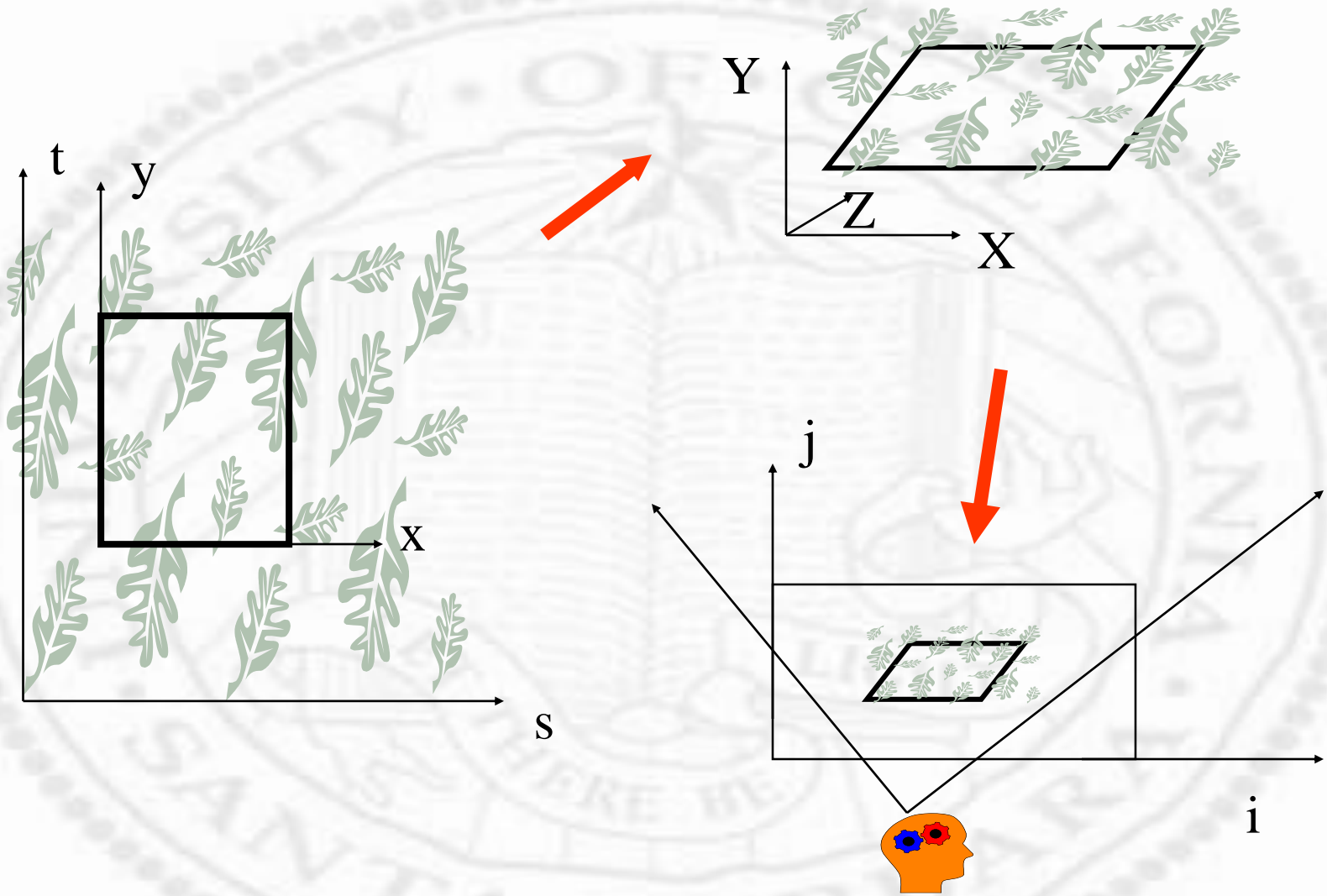
$$\Rightarrow l_z + t(p_z - l_z) = 0$$

$$\Rightarrow t = -\frac{l_z}{(p_z - l_z)}$$

$$\Rightarrow x = \frac{l_z p_x - l_x p_z}{(p_z - l_z)}, y = \frac{l_z p_y - l_y p_z}{(p_z - l_z)}$$

$$\begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} l_z & 0 & -l_x & 0 \\ 0 & l_z & -l_y & 0 \\ 0 & 0 & 1 & -l_z \end{bmatrix} \begin{bmatrix} p_x \\ p_y \\ p_z \\ 1 \end{bmatrix}$$

Homework #2 – Texture



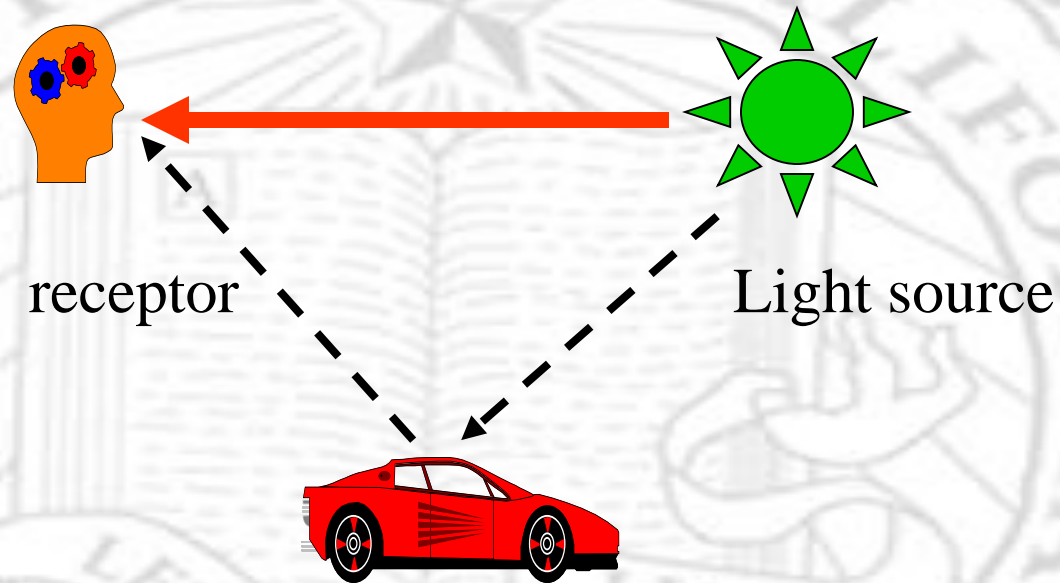
Homework #2 – Texture

- ❖ Hardest part – get images into your program (OpenGL is not for image processing)
- ❖ Taking pictures – You have a phone, right?
- ❖ Importing pictures
 - ❑ Direct (JPG) – read JPG images
 - ❑ Indirect (JPG->ppm with convert) – easy read afterward
- ❖ Nitty Gritty details



```
P3
# feep.ppm
4 4
15
0 0 0 0 0 0 0 0 0 15 0 15
0 0 0 0 15 7 0 0 0 0 0 0
0 0 0 0 0 0 0 15 7 0 0 0
15 0 15 0 0 0 0 0 0 0 0 0
```

Color Model and Color Perception



Geometry and Radiometry

- ❖ In creating and interpreting images, we need to understand two things:
 - ❑ Geometry – Where scene points appear in the image (image locations)
 - ❑ Radiometry – How “bright” they are (image values)
- ❖ **Geometric** enables us to know something about the scene location of a point imaged at pixel (u, v)
- ❖ **Radiometric** enables us to know what a pixel value implies about surface lightness and illumination

Radiometry

- ❖ Radiometry is the measurement of light
 - ❑ Actually, electromagnetic energy
- ❖ Imaging starts with light sources
 - ❑ Emitting photons – quanta of light energy
 - ❑ The sun, artificial lighting, candles, fire, blackbody radiators ...
- ❖ Light energy interact with surfaces
 - ❑ Reflection, refraction, absorption, fluorescence...
 - ❑ Also atmospheric effects (not just solid surfaces)
- ❖ Light energy from sources and surfaces gets imaged by a camera
 - ❑ Through a lens, onto a sensor array, finally to pixel values – an image!

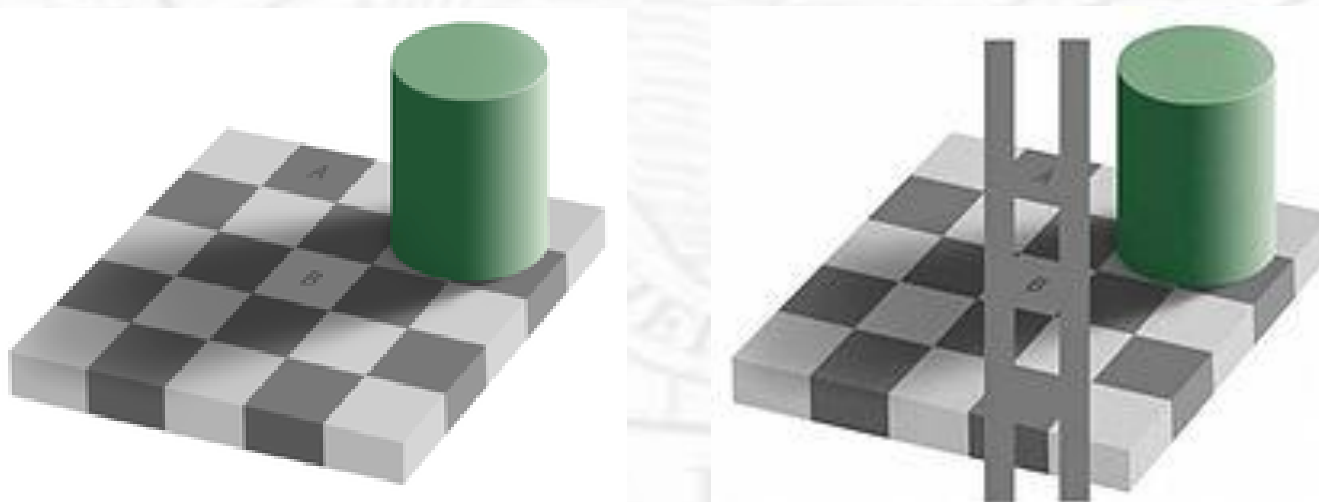
Two-Stage Approaches

- ❖ Light source + receptor
 - ❑ Various color models
 - ❑ Matching color and spatial resolution
- ❖ Light source + object + receptor
 - ❑ OpenGL model (primary ray)
 - ❑ Others (more advanced)
 - ❑ Shadow

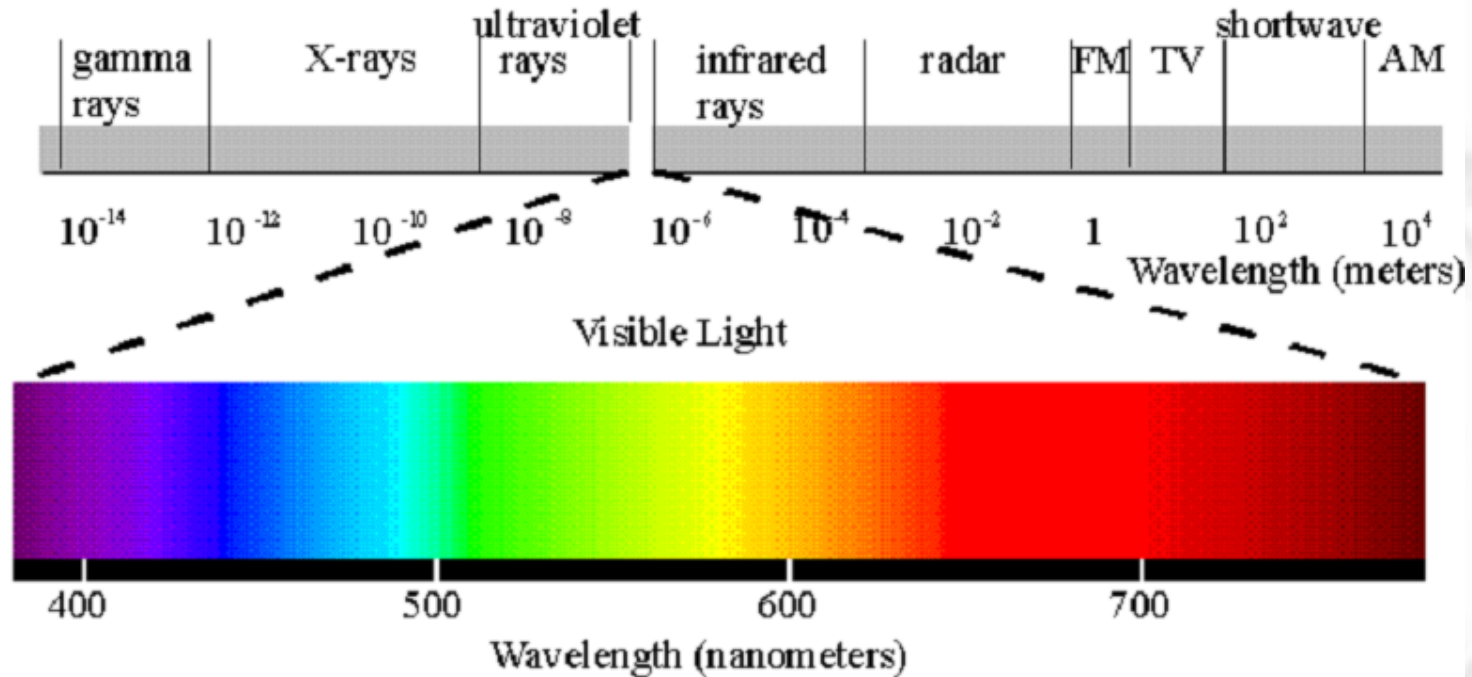
Color Perception

❖ Complicated

- ❑ Nonlinear
- ❑ Spatially variant
- ❑ Many models and interpretations



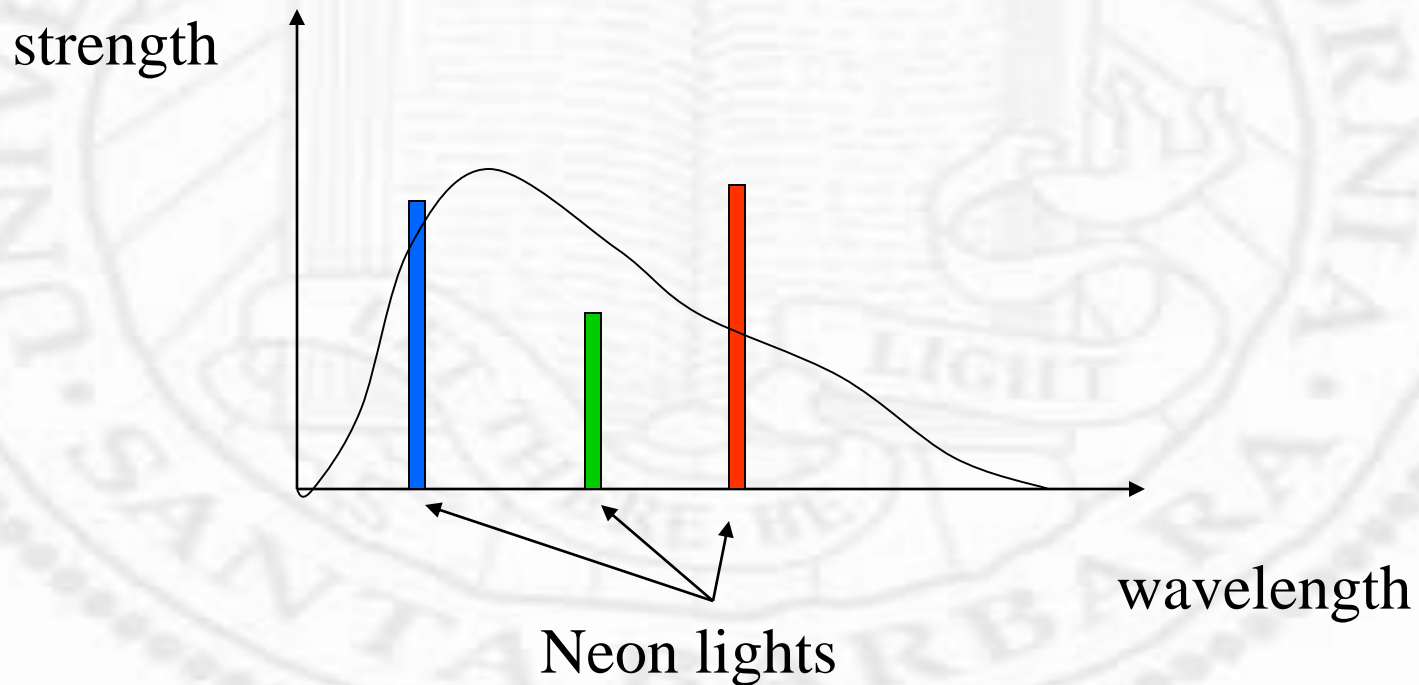
Electromagnetic (EM) Spectrum



Energy, frequency, and wavelength
are related

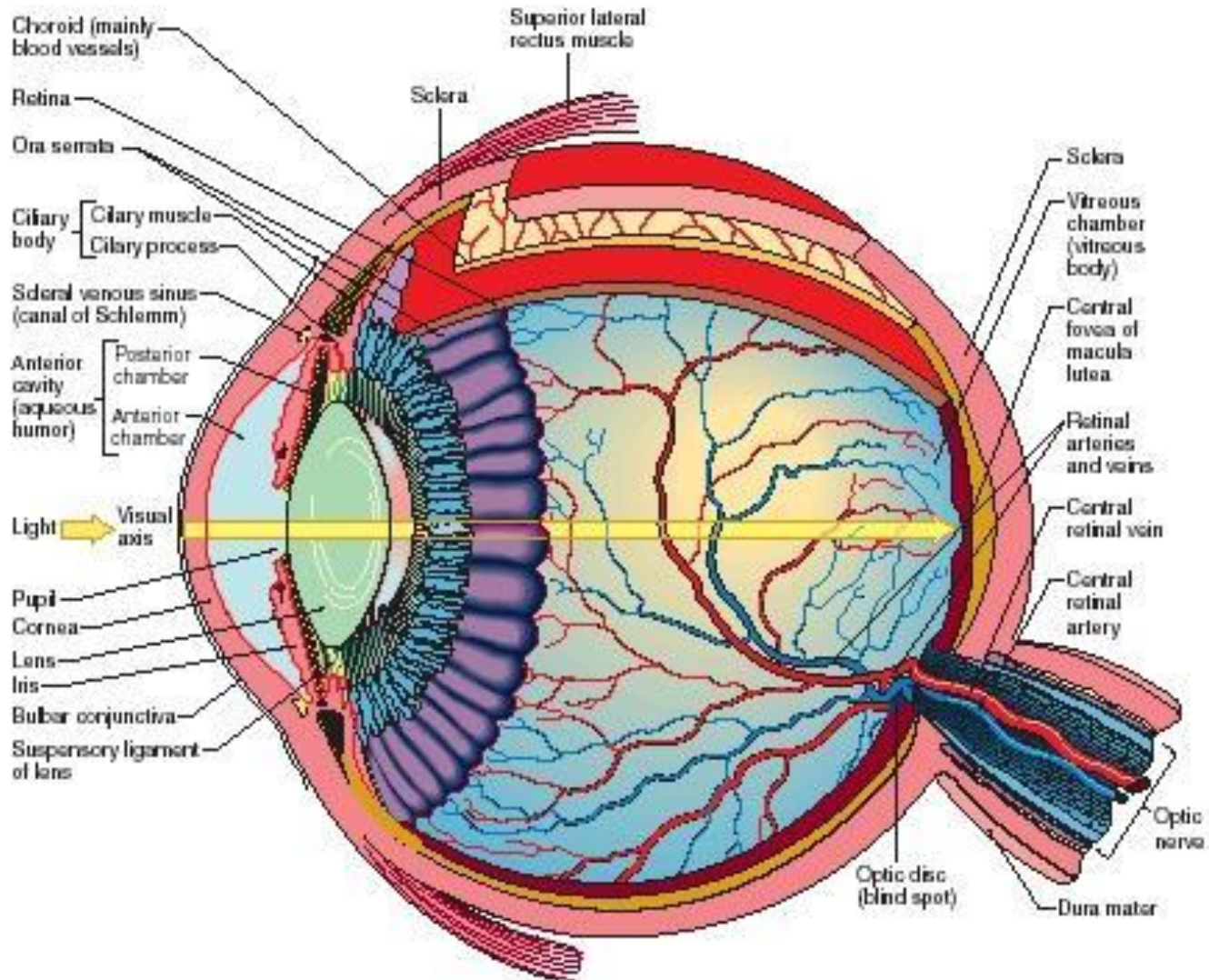
Light Sources

- ❖ Characterized by emission strength as a function of wavelength



Eye

Vertical section of the right eye, shown from the nasal side



Eye

❖ Characterized by spectrum sensitivity functions

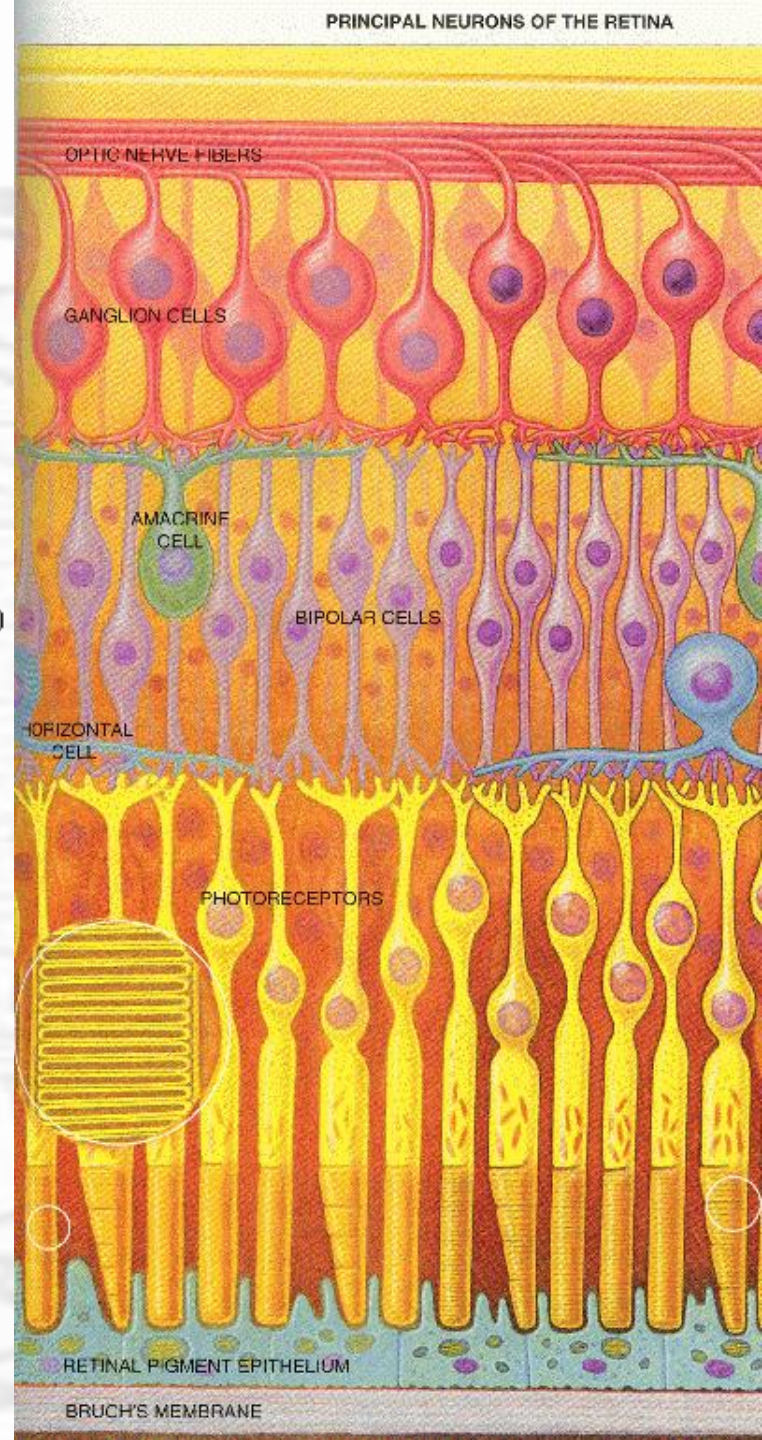
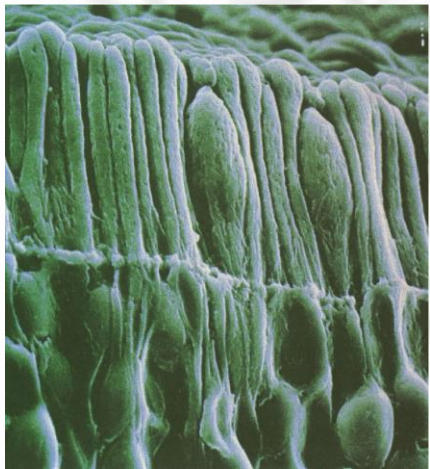
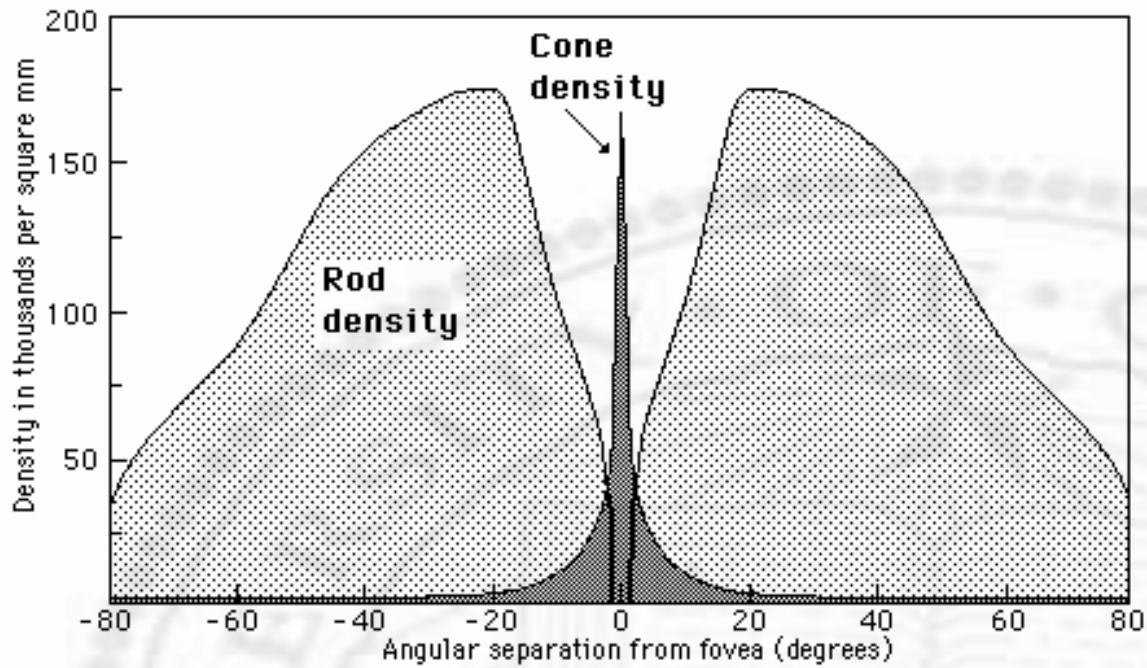
❖ Rods

- ❑ night vision
- ❑ achromatic (gray) perceptions
- ❑ lack fine details
- ❑ found mostly at periphery of retina

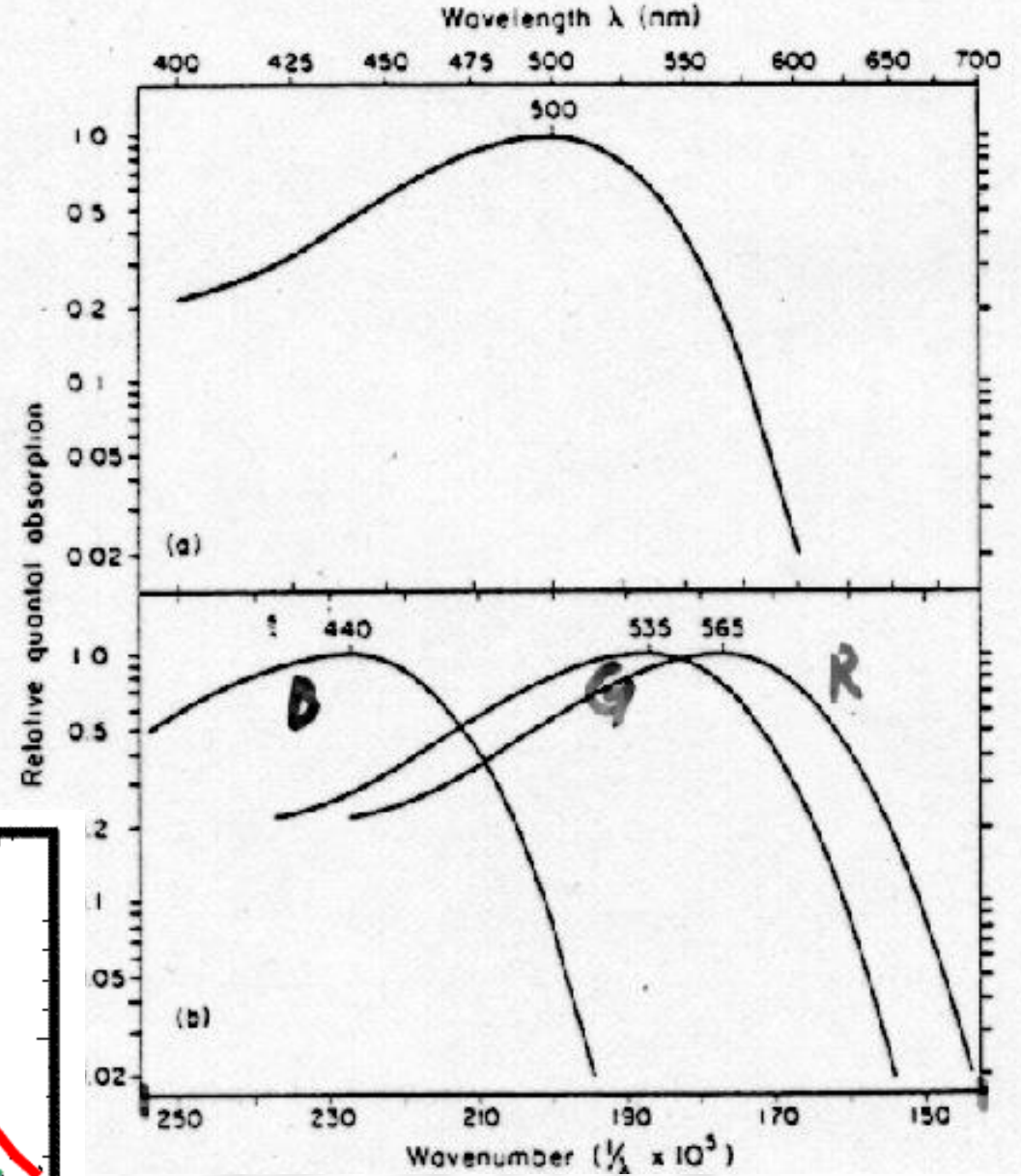
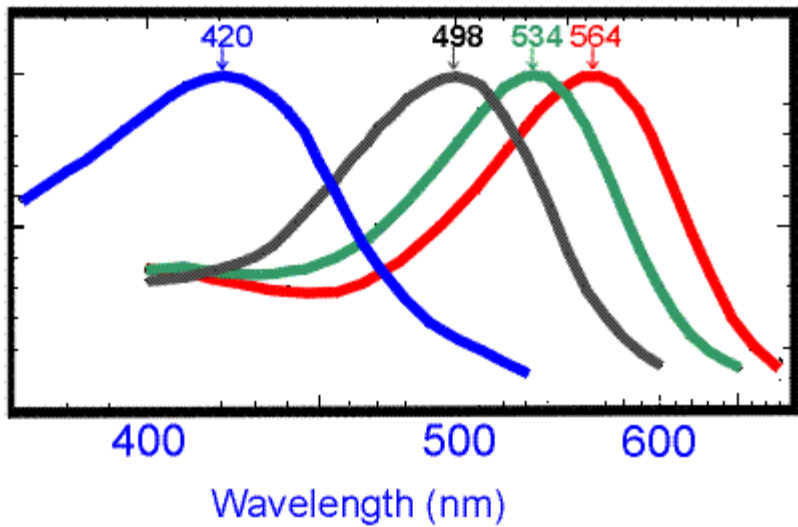
❖ Cones

- ❑ daylight, color vision
- ❑ found mostly at foveal pit

$$R, G, B = \int_{low_band}^{high_band} incident_light_strength(\lambda) \cdot eye_sensitivity(\lambda) d\lambda$$



Normalized absorbance

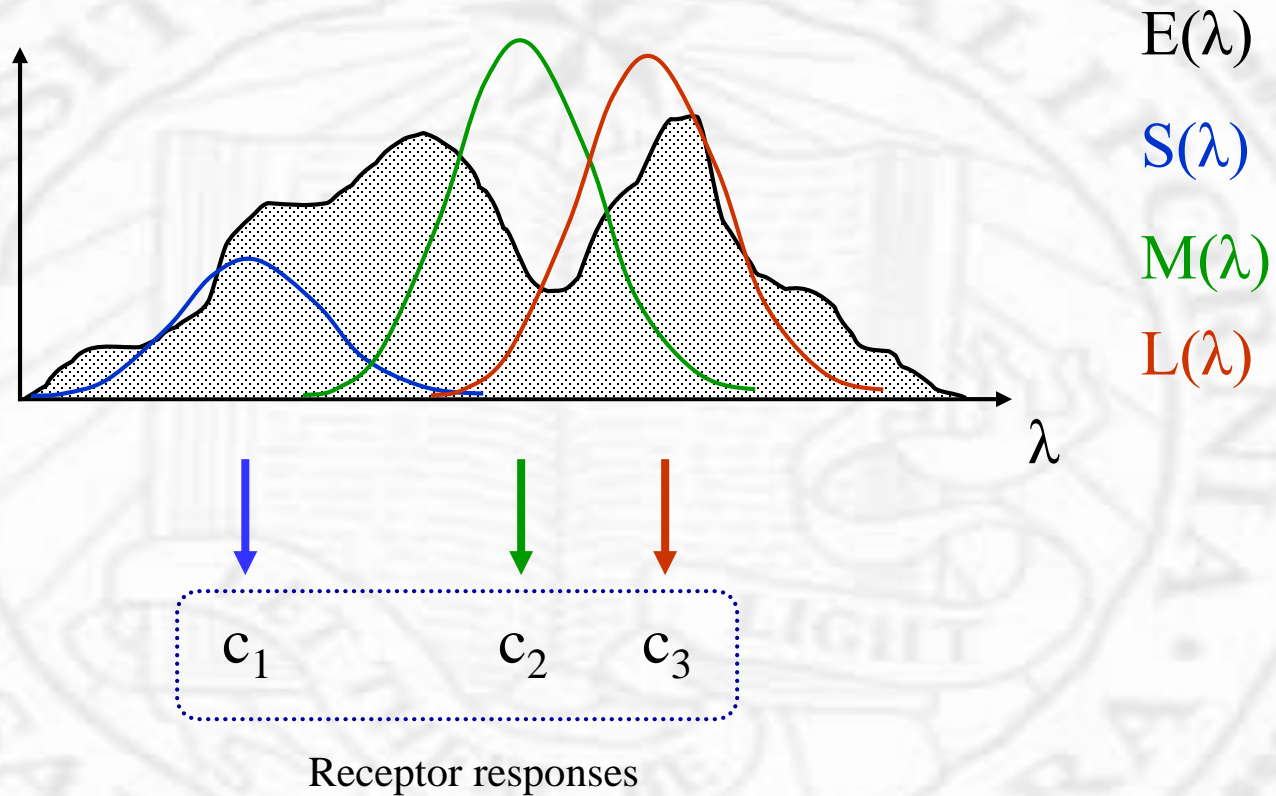


puter Graphics



After Bowmaker & Dartnall, 1980

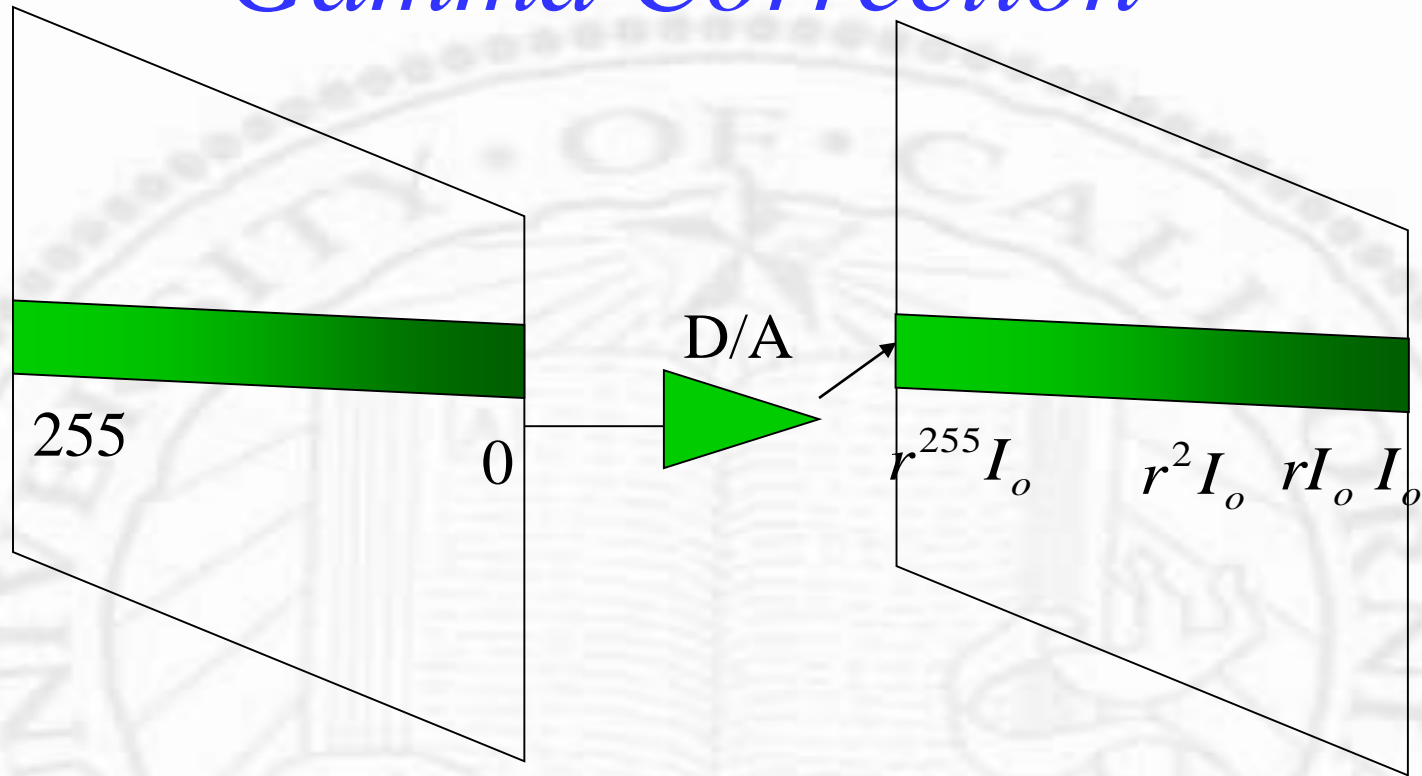
Responses to a source



Achromatic Perception

- ❖ Simple model brightness = $R + G + B$
- ❖ However, it is not a linear function, but a log function
- ❖ 50- \rightarrow 100- \rightarrow 150 does not give a linear ramp, but 50- \rightarrow 100- \rightarrow 200- \rightarrow 400 does
- ❖ But when we specify intensity of a pixel, we will like to have 0 to 255 to be a linear ramp
- ❖ Need *gamma* correction

Gamma Correction



Frame buffer

Screen

$$r^{255} I_o = 1$$

$$r = \left(\frac{1}{I_o}\right)^{\frac{1}{255}}, I_j = I_o^{\frac{225-j}{255}}$$

Gamma Correction (cont.)

- ❖ Physically, the intensity (I) of a phosphor cell is proportional to the number of incident electrons (2.2 to 2.5 for CRT)
- ❖ The number of electrons (N) in turn is proportional to control grid voltage (J)
- ❖ Control grid voltage (J) is proportional to the pixel value (V) specified

$$I = kN^\gamma$$

$$= k' J^\gamma$$

$$= k'' V^r$$

$$I_j = k'' V_j^r$$

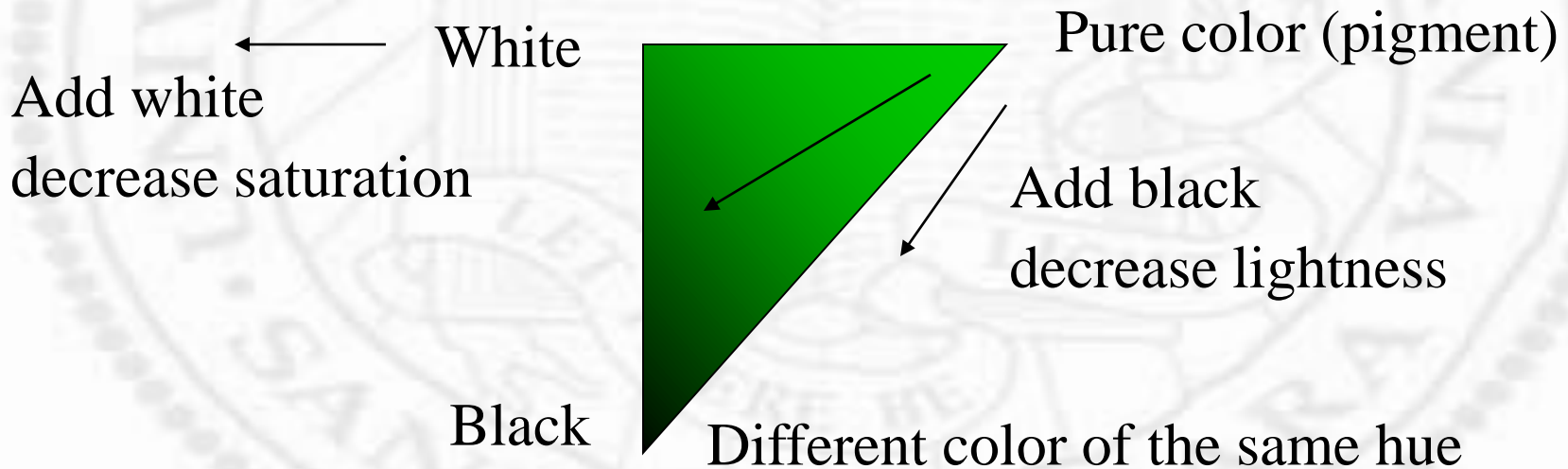
$$V_j = \text{Round}\left(\frac{I_j}{k''}\right)^{\frac{1}{r}}$$

Gamma Correction (cont.)

- ❖ Instead of using pixel value directly, a look-up table with V is stored, a process called gamma correction

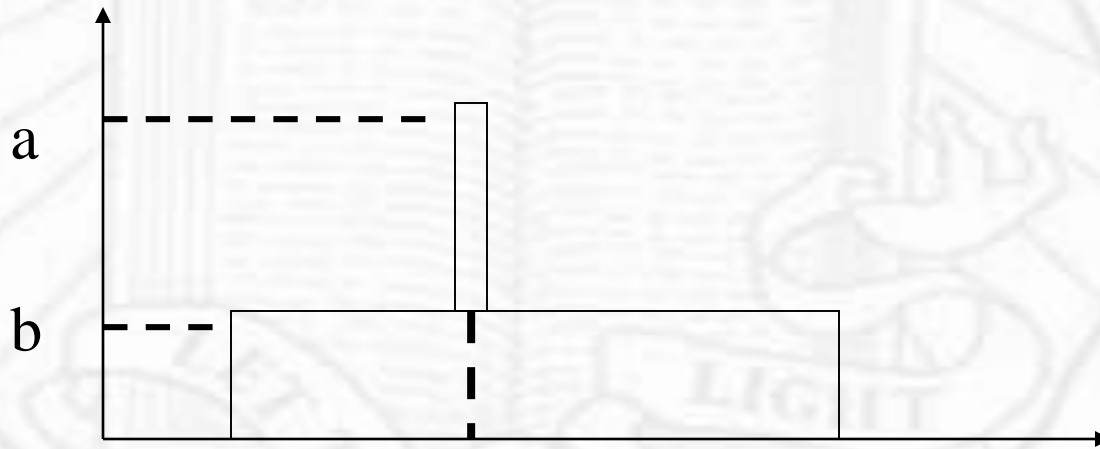
Chromatic Perception

- ❖ Many different models, old and new, motivated by different usage and conventions
- ❖ Artists and painters



Psychophysics model

- ❖ Dominant wavelength (perception of hue)
- ❖ Excitation purity (saturation)
- ❖ Luminance (amount of light)



f: perceived hue

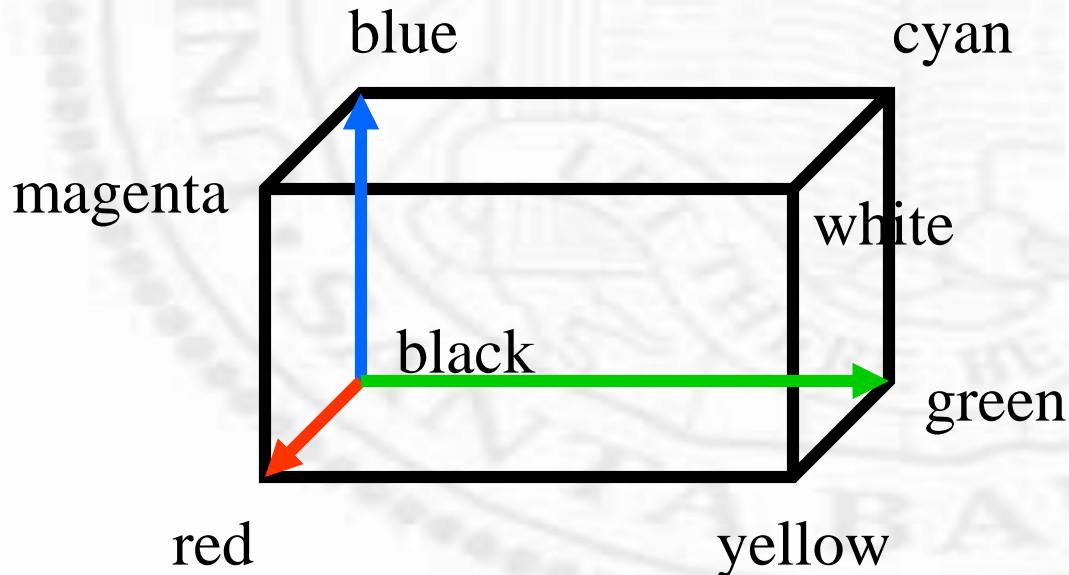
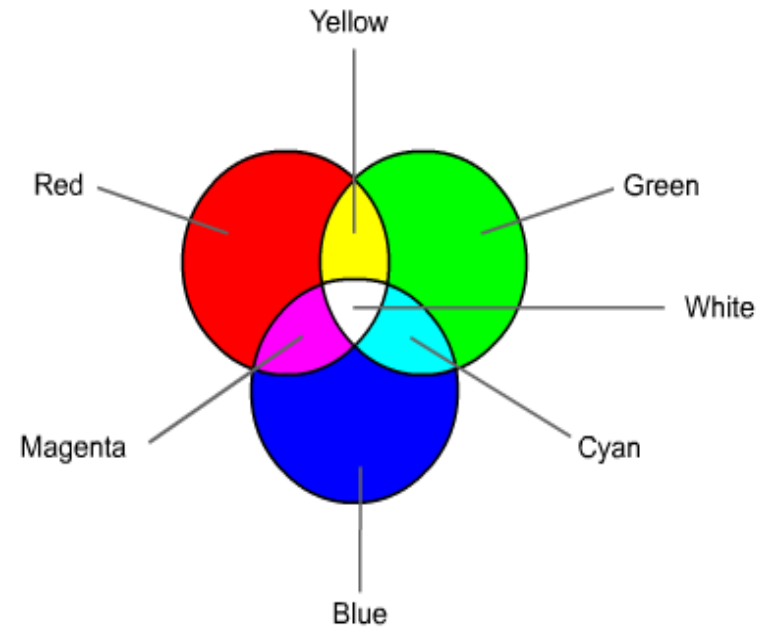
a & b: luminance

$b=0$ purity = 100%

$a=b$ purity = 0%

R-G-B model

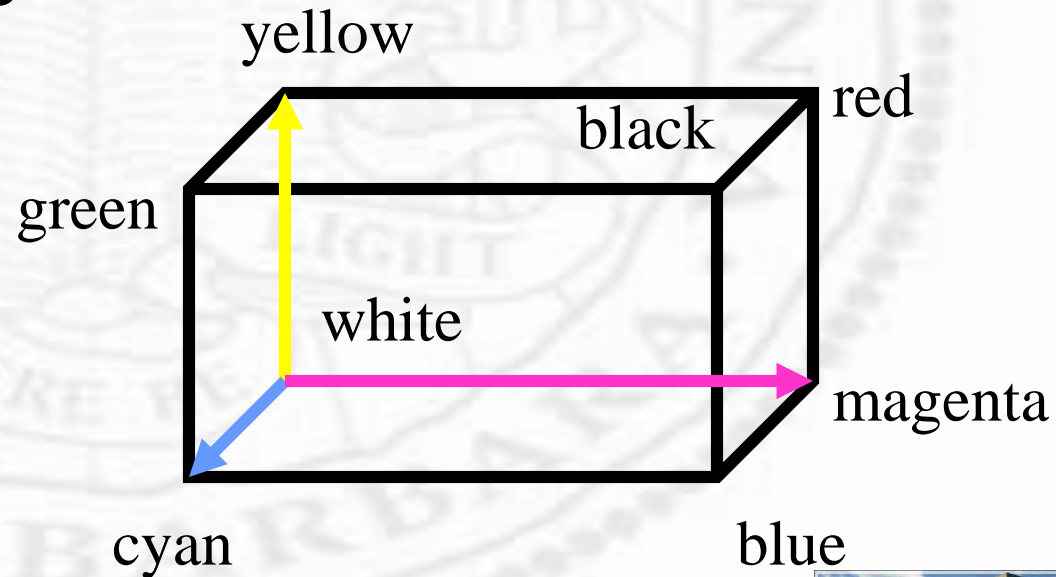
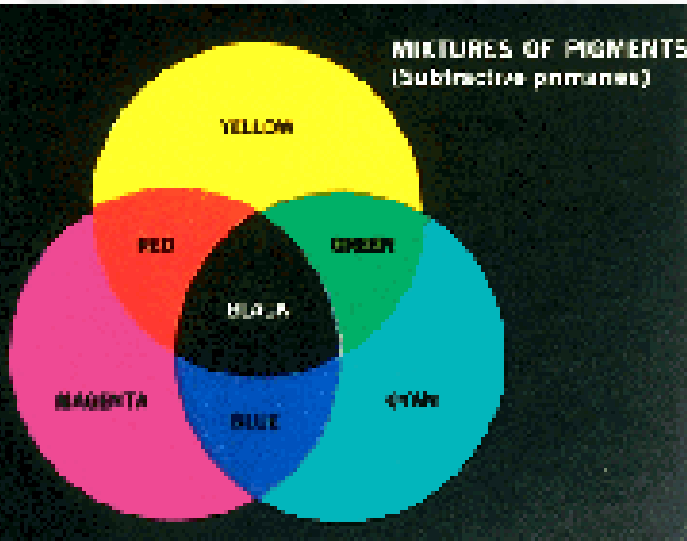
- ❖ Color CRT monitor
- ❖ Additive system



C-M-Y model

- ❖ Color printer
- ❖ Subtractive system
- ❖ cyan absorbs red
- ❖ magenta absorbs green
- ❖ yellow absorbs blue

Cyan+magenta = blue
cyan+yellow = green
magenta+yellow = red



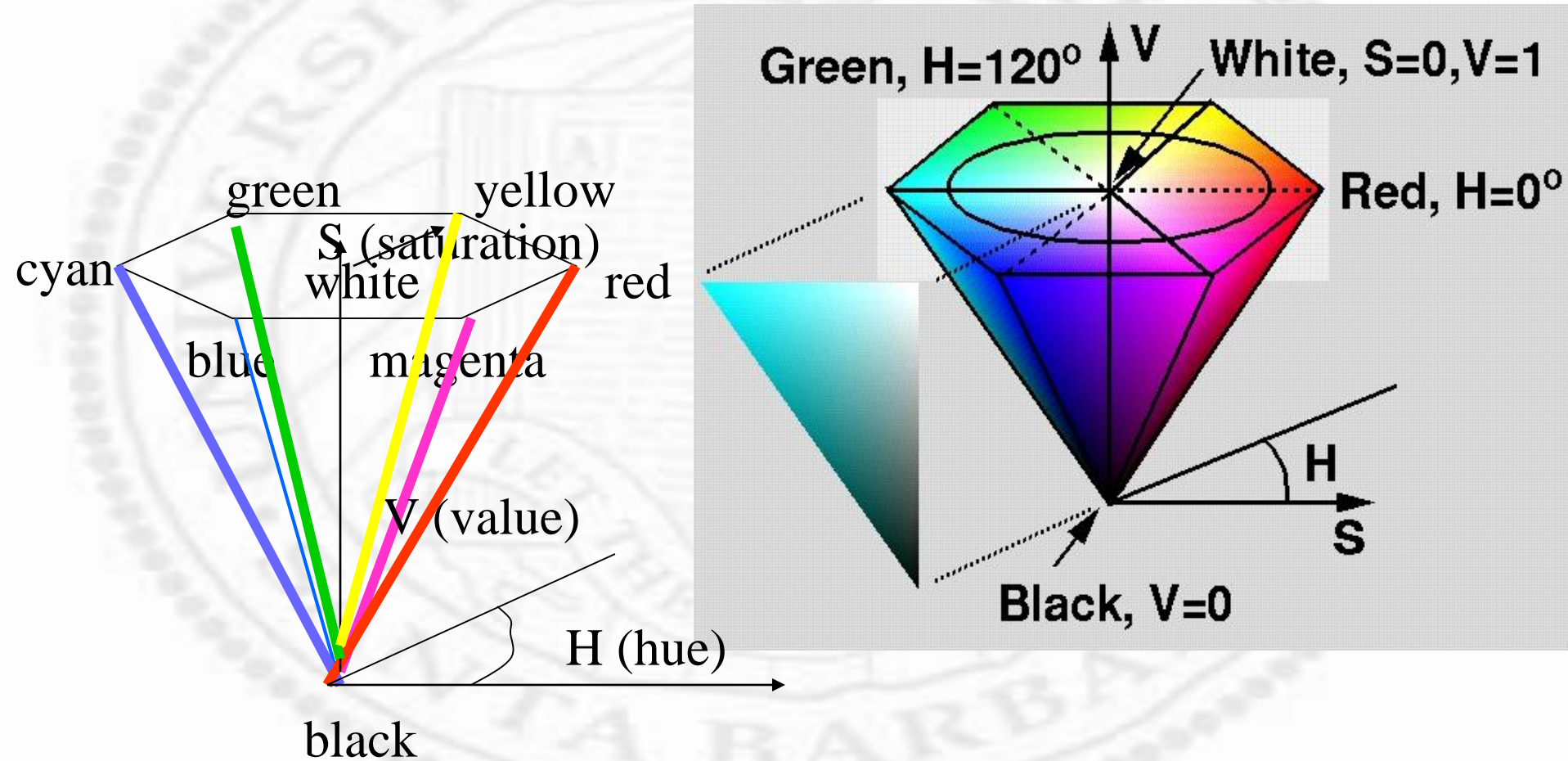
Y-I-Q model

- ❖ Commercial color TV broadcasting
- ❖ Backward compatible with B/W TV
- ❖ Y uses 4MHz, I 1.5 MHz, Q 0.6 MHz because eyes are more sensitive to monochrome than color

$$\begin{bmatrix} Y \\ I \\ Q \end{bmatrix} = \begin{bmatrix} 0.3 & 0.59 & 0.11 \\ 0.6 & -0.28 & -0.32 \\ 0.21 & -0.52 & 0.31 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

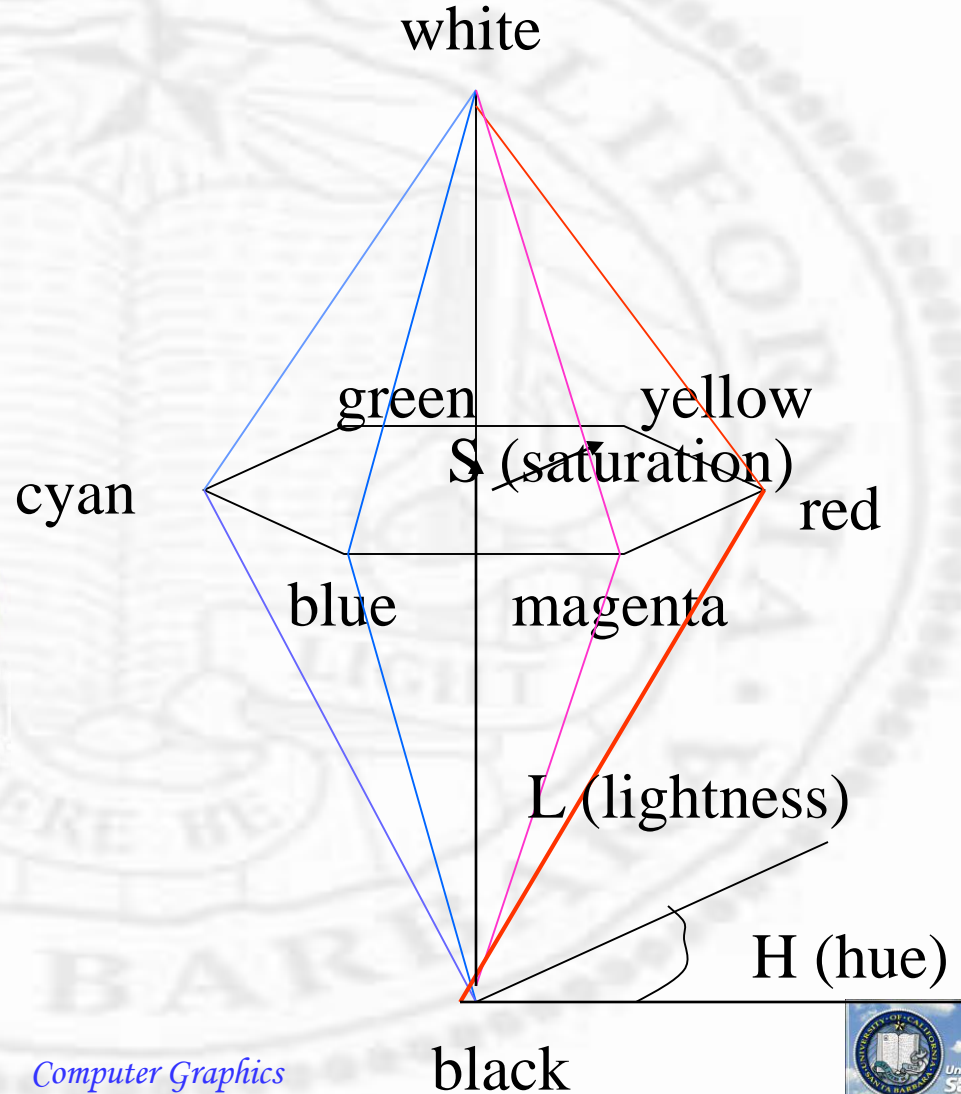
H-S-V model

❖ Emulate Artists' model in 3D

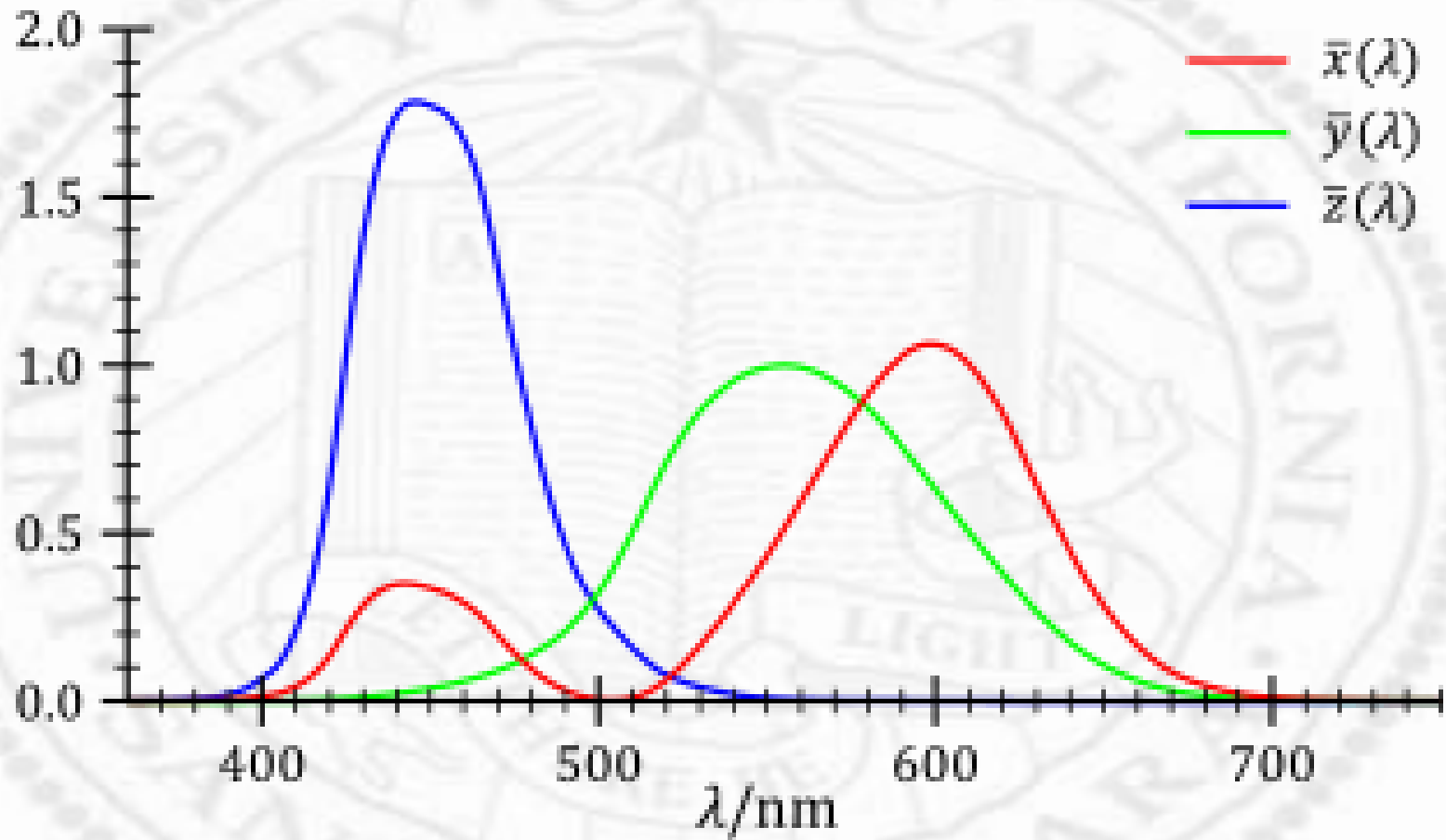


H-L-S model

- ❖ Emulate Artists' model in 3D



CIE Standard



CIE Standard

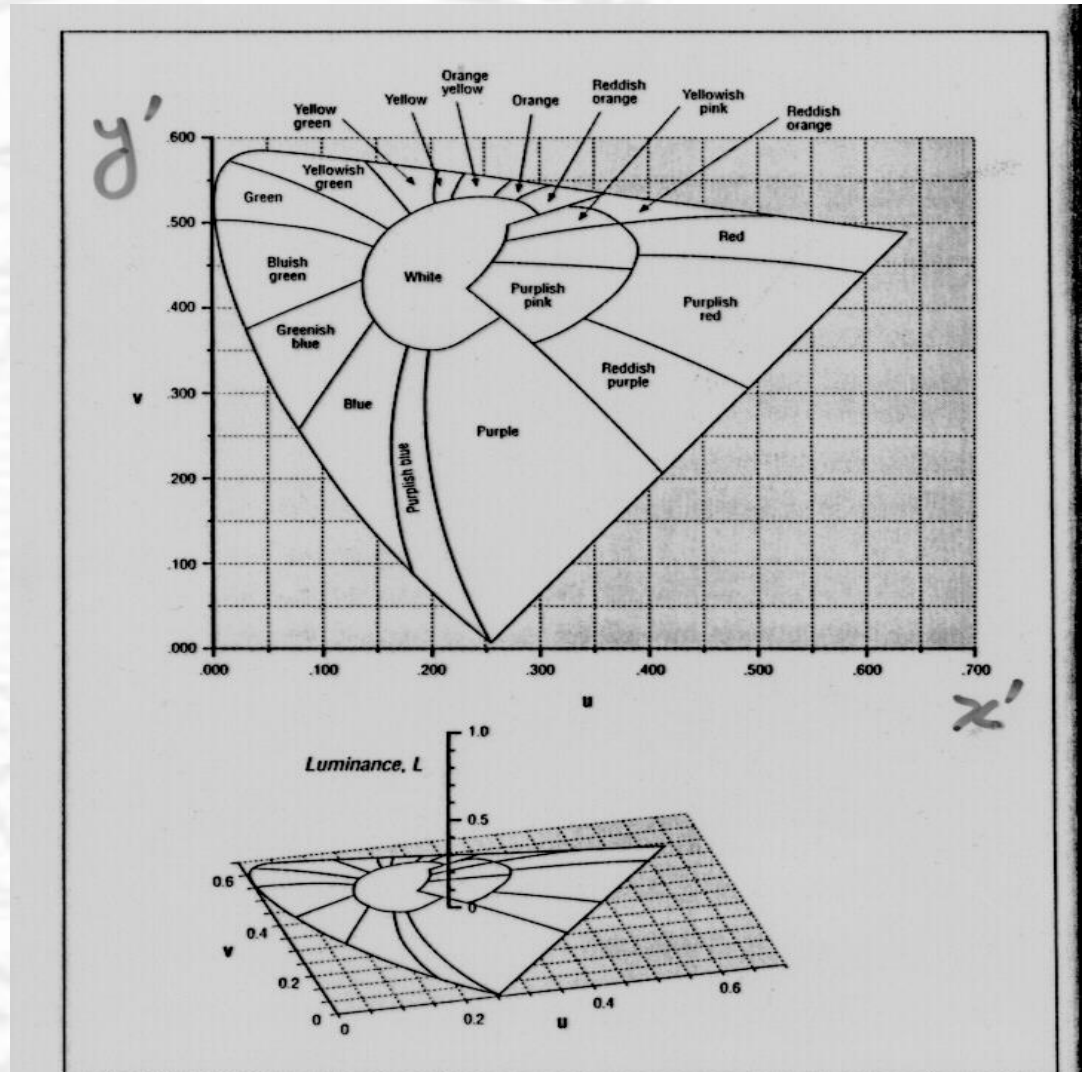
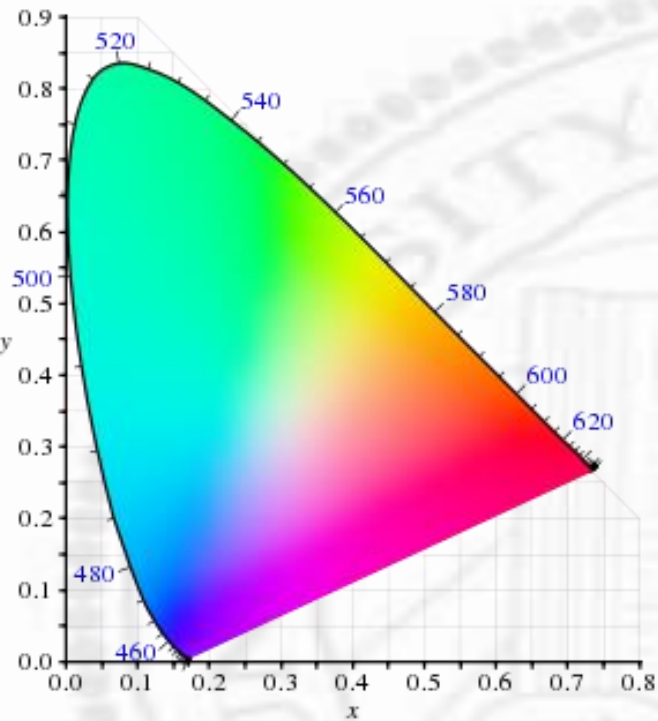
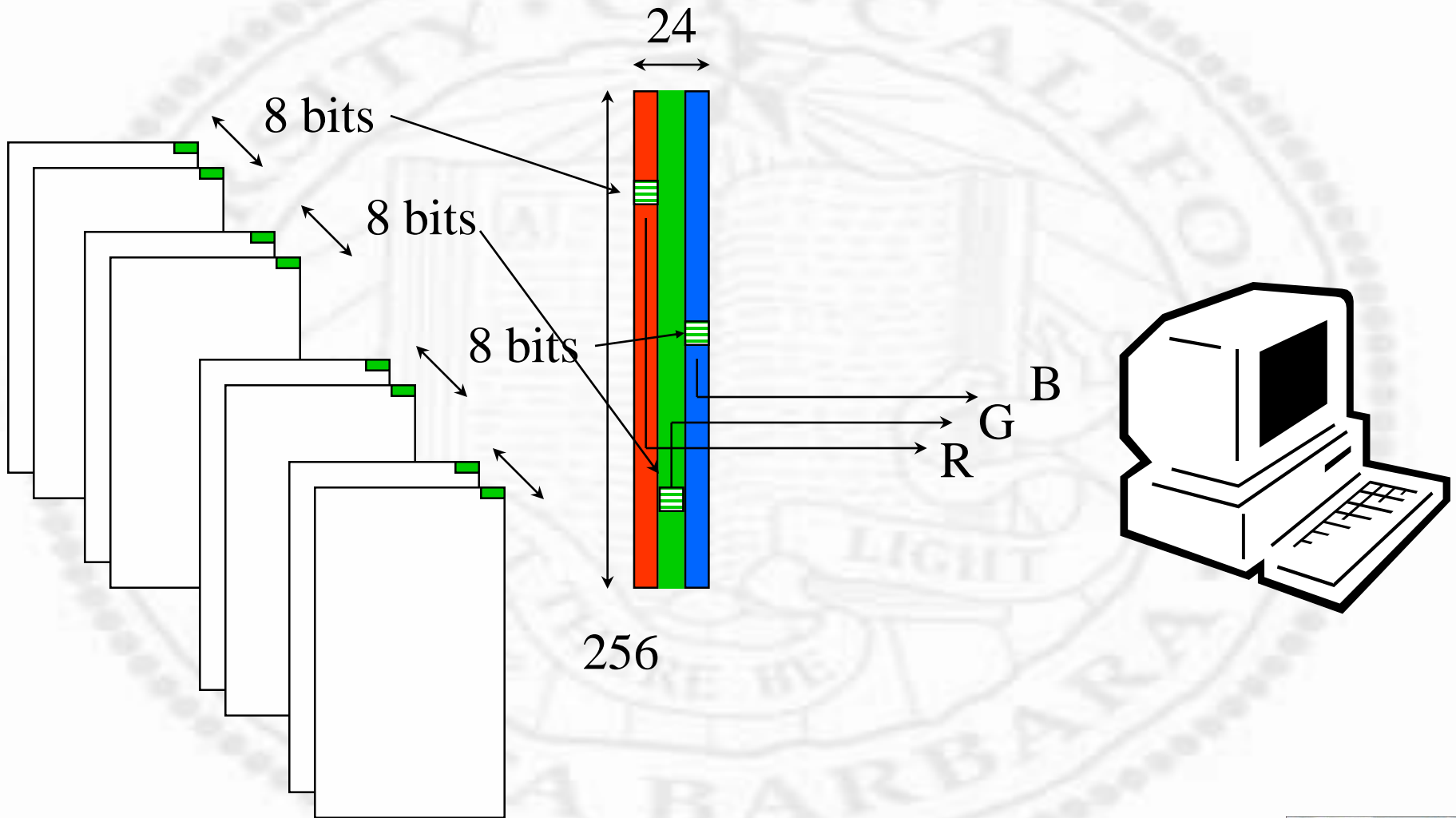


Figure 5-8. The CIE-LUV color model

OpenGL Color Models

- ❖ A color monitor model with A (alpha, transparency) - RGBA model, or
- ❖ A color-index model with a colormap (set through aux-library)

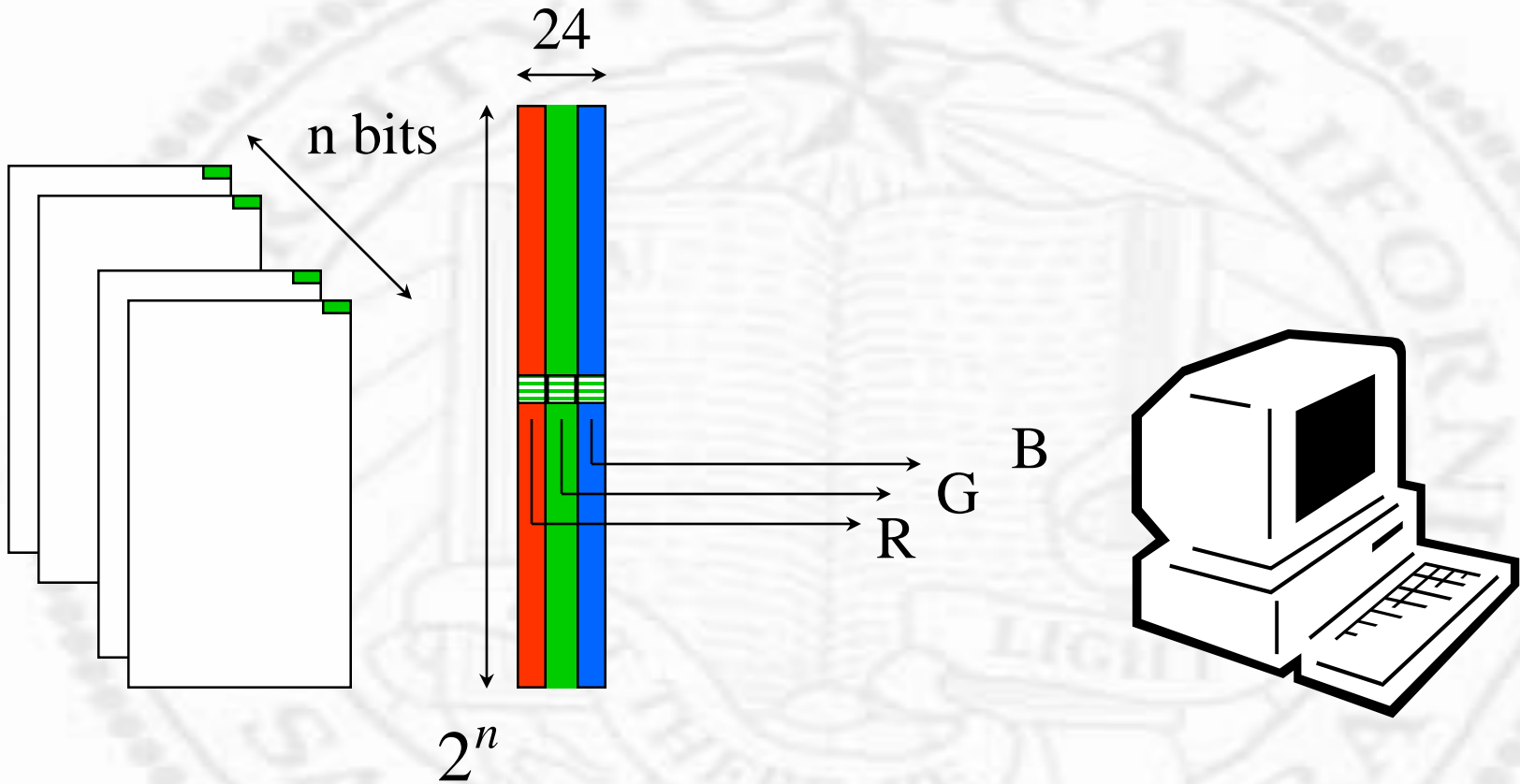
RGB Color Mode



RGBA Color Mode

- ❖ Syntax: `void glColor3f(0.0, 1.0, 0.0)` or `glColor4f(r, g, b, a);`
 - ❑ min 0.0, max 1.0, independent of underlying hardware
- ❖ Specify object *intrinsic color* (the color when lighting was not enabled)
- ❖ Other variations: `void glColor[3,4]{b,s,i,f,d,ub,us,ui}` also possible

Color-Index Mode



Color-Index Mode

- ❖ Syntax: `void glIndex { sifd } (TYPE c) or glIndex { sifd } v (TYPE *c);`
- ❖ Specify object *intrinsic color* (the color when lighting was not enabled)
- ❖ Number of indices available is usually $2^8=256$ or $2^{16}=65536$, determined by the actual hardware (video memory in a video card and spatial resolution used)

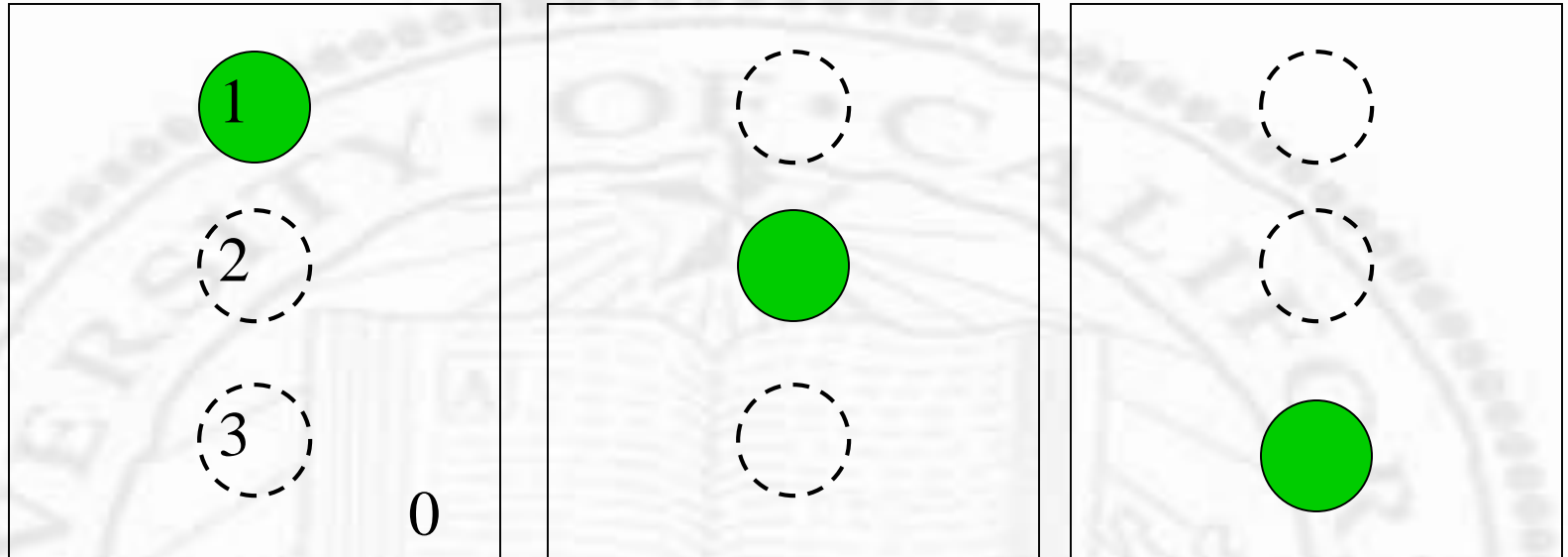
Color-Index Mode

- ❖ It might be surprising to know that OpenGL does not provide routines for manipulating color cells in a colormap
- ❖ Use aux-library void `auxSetOneColor(index,r,g,b)`
 - `r,g,b` in `[0,1]`

Choice btw RGBA and Index

- ❖ General rule: use RGBA
- ❖ RGBA better for shading, color, texture mapping, etc.
- ❖ For legacy application using color-index
 - ❑ Also applied to myriad of ‘less capable’ mobile devices
- ❖ Color-map can be useful for special effect such as animation

Example



0	white	white	white
1	green	white	white
2	white	green	white
3	white	white	green

Shade Model

- ❖ Void `glShadeModel` (`GL_FLAT` or `GL_SMOOTH`)
- ❖ Important when shade extended primitives specified by multiple vertices (e.g. polygons, triangular meshes)
- ❖ `GL_FLAT`: use the color of a particular vertex for the whole primitive
- ❖ `GL_SMOOTH`: interpolate the color of vertices
- ❖ May be troublesome in color-index mode

The “Last Mile” Issues

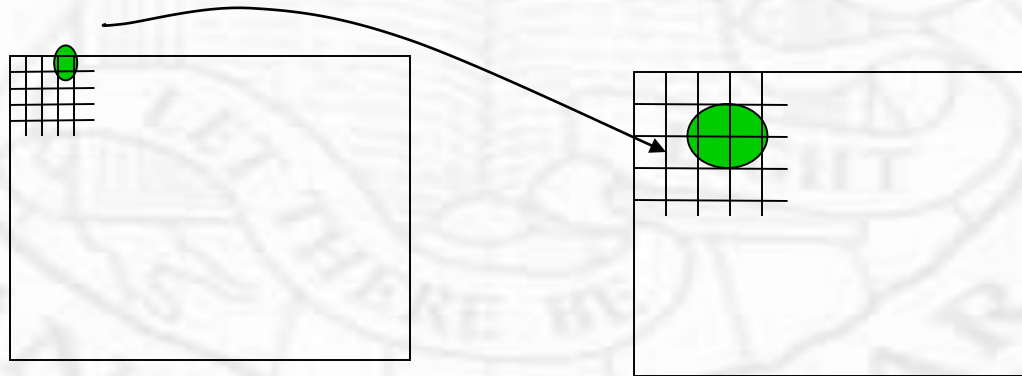
- ❖ Specification of color and spatial resolution was done in a device independent way
 - ❑ the device’s *spatial* resolution does not matter
 - ❑ the device’s *color* resolution does not matter
- To OpenGL
- ❖ In reality, the display window
 - ❑ has a fixed spatial resolution
 - ❑ a fixed color resolution (or “visual” type)
 - ❑ Printer – high spatial, low color
 - ❑ PDA, cell phone, etc. – low spatial, low color

The Last Mile Issues (cont.)

- ❖ In general, taken care of by *glut* and underlying X window systems
- ❖ Not enough *spatial* resolution
 - ❑ Down sampling with interpolation
- ❖ Not enough *color* resolution
 - ❑ half toning, and more generally
 - ❑ ditheringcan be used

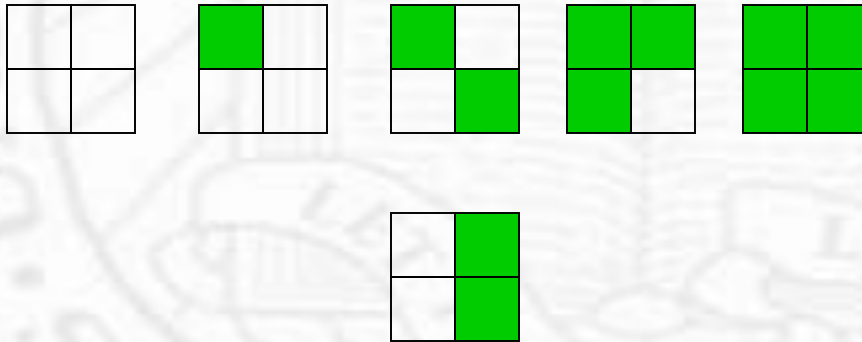
Binary Half Tone

- ❖ *High* resolution images to be produced on a low resolution device
 - ❑ e.g., a gray scale 8-bit image printed on a B/W paper
- ❖ Trade spatial resolution for color resolution



Binary Half Tone

- ❖ With a $k \times k$ square, $k^2 + 1$ intensity levels can be approximated
- ❖ Try to avoid artifacts



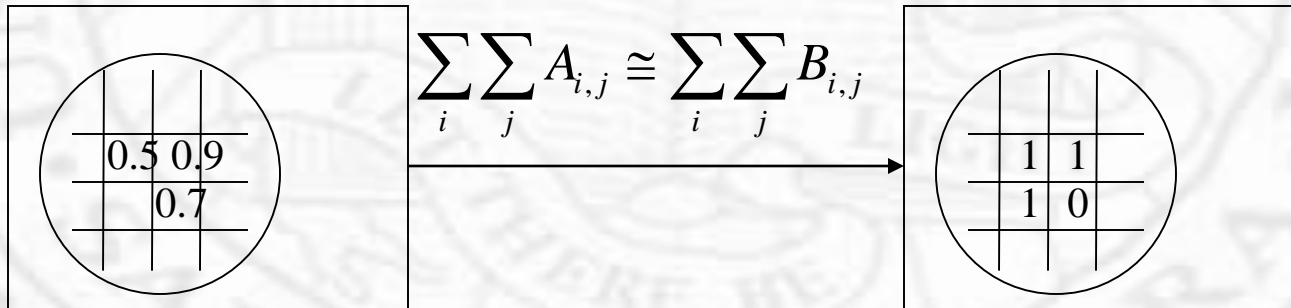
Dithering

- ❖ When trading spatial resolution for color resolution is *not* satisfactory
- ❖ Binary dithering
 - ❑ input: $A[0..m-1][0..n-1]$ of $[0..1]$;
 - ❑ output: $B[0..m-1][0..n-1]$ of $[0 \text{ or } 1]$;
- ❖ Color dithering
 - ❑ input: $A[0..m-1][0..n-1]$ of 2^m ;
 - ❑ output: $B[0..m-1][0..n-1]$ of 2^n ; $m > n$

Binary dither

❖ Human perception

- ❑ Eye integrates luminous stimuli over a solid angle of about 2 degrees
- ❑ As long as the average intensity over a 2-deg neighborhood is similar



Binary Dither

❖ Simple thresholding

if $A(i,j) > 0.5$ then

$$B(i,j) = 1$$

else

$$B(i,j) = 0$$

❖ Thresholding + perturbation

if $A(i,j) + N(i,j) > 0.5$ then

$$B(i,j) = 1$$

else

$$B(i,j) = 0$$

Ordered Dither (cont.)

❖ An area based approach

$$x = i \text{ mode } c, \quad y = j \text{ mod } c$$

If $a(i,j) > D(x,y)$ then

$$B(i,j) = 1$$

else

$$B(i,j) = 0$$

D is called a magic square, filled with permutation of numbers from 0 to c^2-1

Error Diffusion

❖ a point-based approach

for $i=0$ to $m-1$ do

for $j=0$ to $n-1$ do

if $A(i,j) > 0.5$ do

$B(i,j) = 1$

else

$B(i,j) = 0$

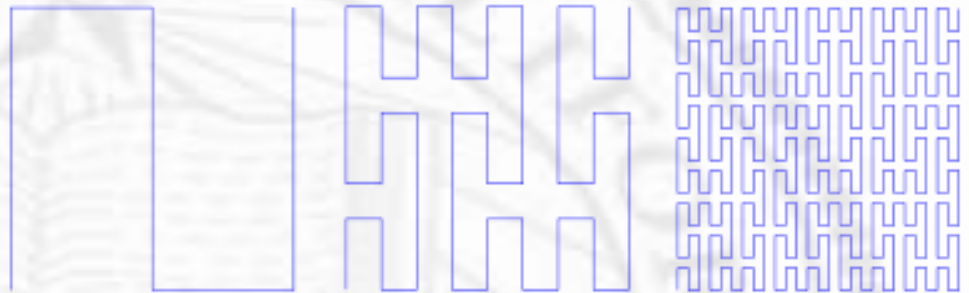
$A(i, j+1) += \alpha \cdot (A(i, j) - B(i, j));$

$A(i-1, j+1) += \beta \cdot (A(i, j) - B(i, j));$

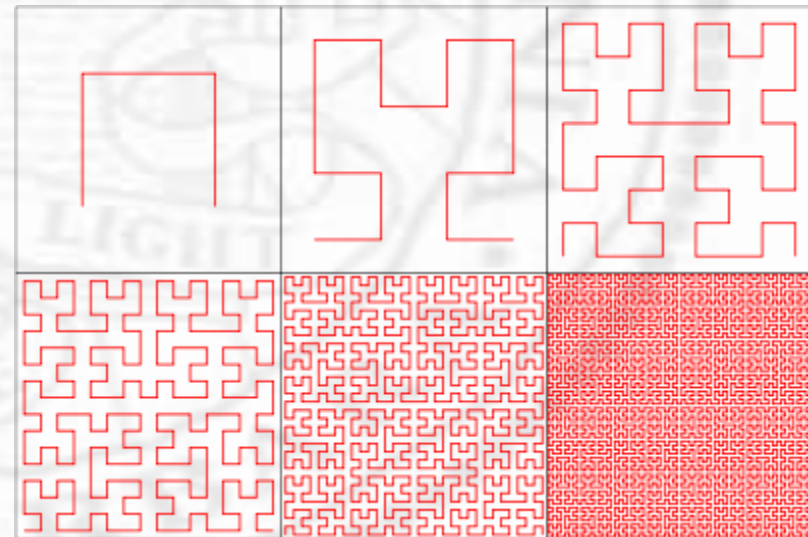
$A(i+1, j) += \gamma \cdot (A(i, j) - B(i, j));$

$A(i+1, j+1) += \delta \cdot (A(i, j) - B(i, j));$

$\alpha + \beta + \gamma + \delta \leq 1$



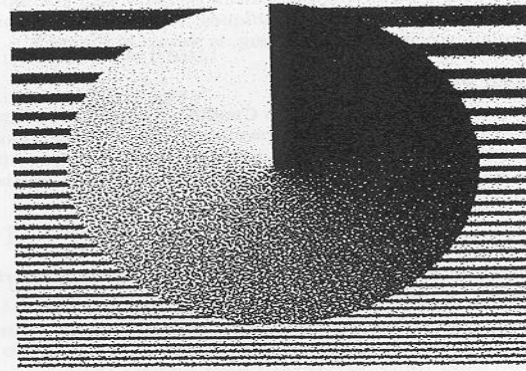
Peano curve



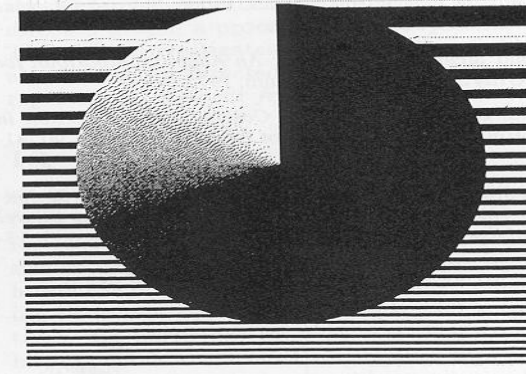
Hilbert curve



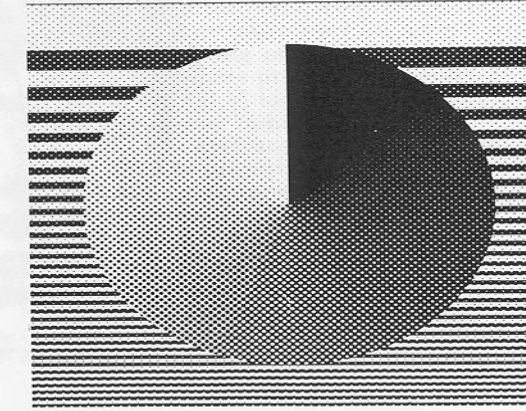
(A)



(B)



(C)



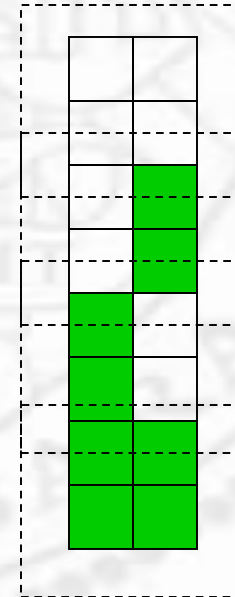
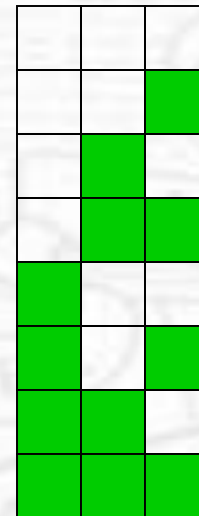
— The two test images at 75 dpi dithered with three different algorithms: (A) Space filling curve algorithm (Hilbert curve), using clusters of 32 pixels -Steinberg algorithm; (C) Clustered-dot ordered dither algorithm, using a matrix of order 8.

Color Dither

- ❖ Bit cut
- ❖ Median cut
- ❖ Quadtree
- ❖ etc.
 - ❑ input: $A[0..m-1][0..n-1]$ of 2^m ;
 - ❑ output: $B[0..m-1][0..n-1]$ of 2^n ; $m > n$

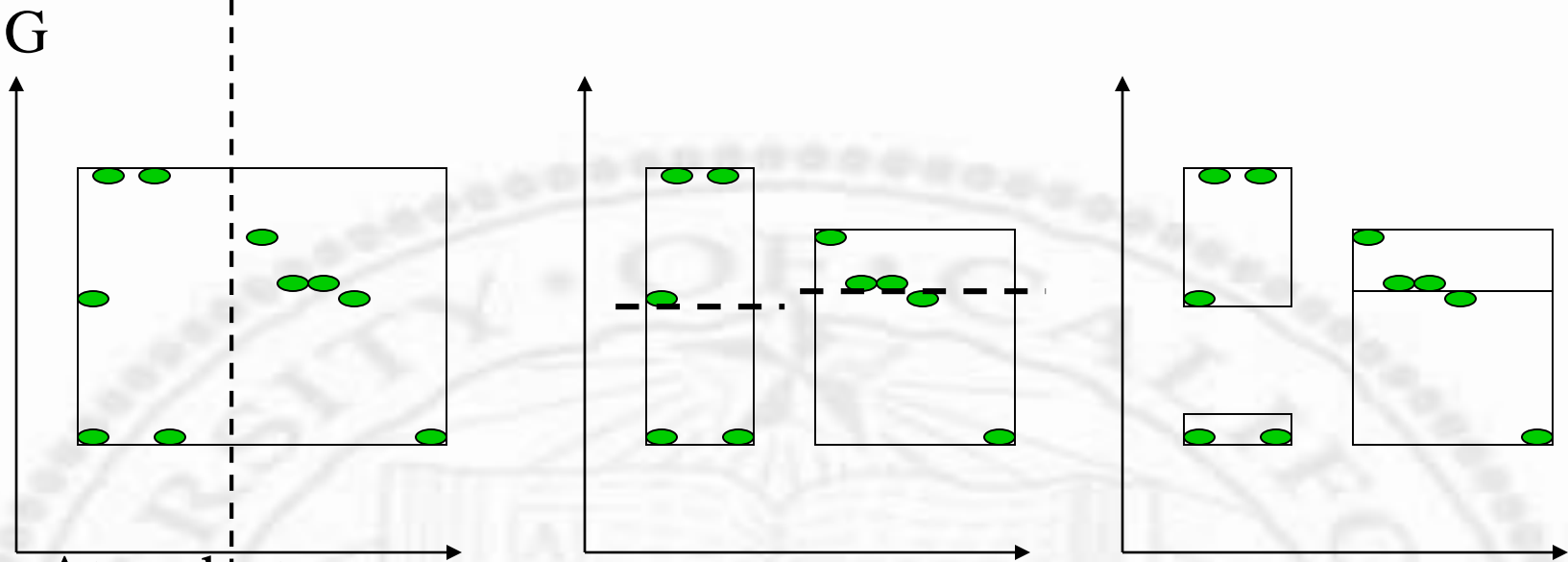
Bit cut (Uniform quantization)

- ❖ 2^m to 2^n by knocking out the lower $(m-n)$ bits
 - ❑ do not adapt to different image contents
 - ❑ produce poor results with severe blocking and contouring effects

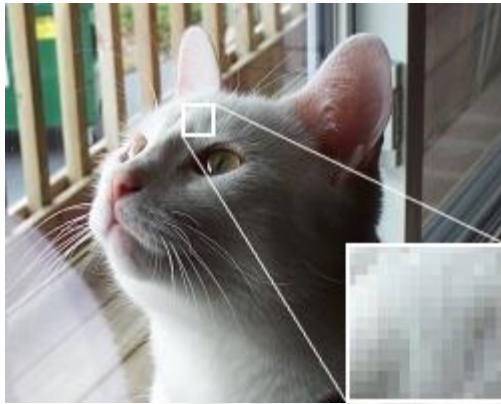


Median Cut

- ❖ The quantization should be adaptive depending on the image content
- ❖ Usually an image will not have pixel colors distributed uniformly over all visible spectrum
- ❖ Reserve more bits for colors which appear more frequently in an image



- ❖ At each step
 - ❑ select the axis with the largest spread
 - ❑ compute median and divide into two groups
- ❖ Recursion until $C = 2^n$ boxes
- ❖ Use average colors in each box to build lookup table



Original photo



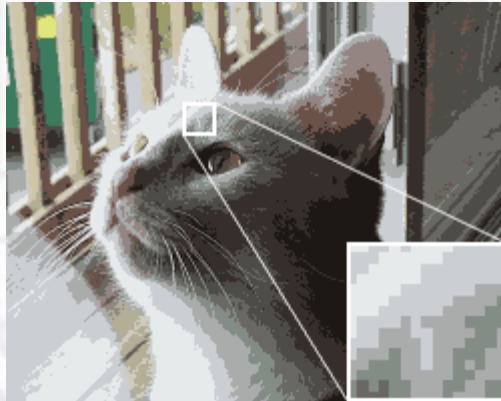
Original image using the web-safe color palette with no dithering applied. Note the large flat areas and loss of detail



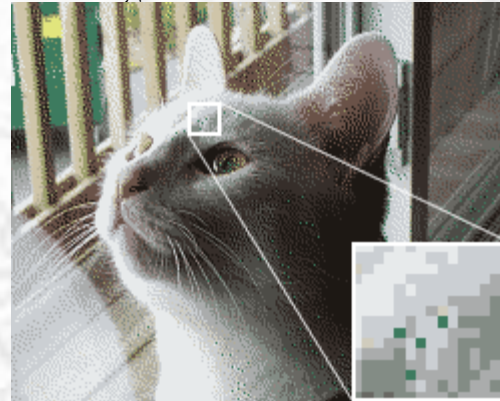
Original image using the web-safe color palette with **Floyd-Steinberg dithering**. Note that even though the same palette is used, the application of dithering gives a better representation of the original



Original image using the web-safe color palette with **Floyd-Steinberg dithering**. Note that even though the same palette is used, the application of dithering gives a better representation of the original



Depth is reduced to a 16-color optimized palette in this image, with no dithering. Colors appear muted, and color banding is pronounced



This image also uses the 16-color optimized palette, but the use of dithering helps to reduce banding.